



**University of
Zurich^{UZH}**

BEoRN : a fast and flexible framework to simulate the 21cm signal during cosmic dawn and reionisation

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Structure of the presentation

- 1- Introducing BEoRN : publicly available and user-friendly python 21cm code
- 2- What type of cosmic dawn and reionisation signals are expected given current constraints from high- z observation ?
- 3- Description of the Halo Model (HM) approach for 21cm
- 4- Cosmological forecast for SKA using the Halo Model

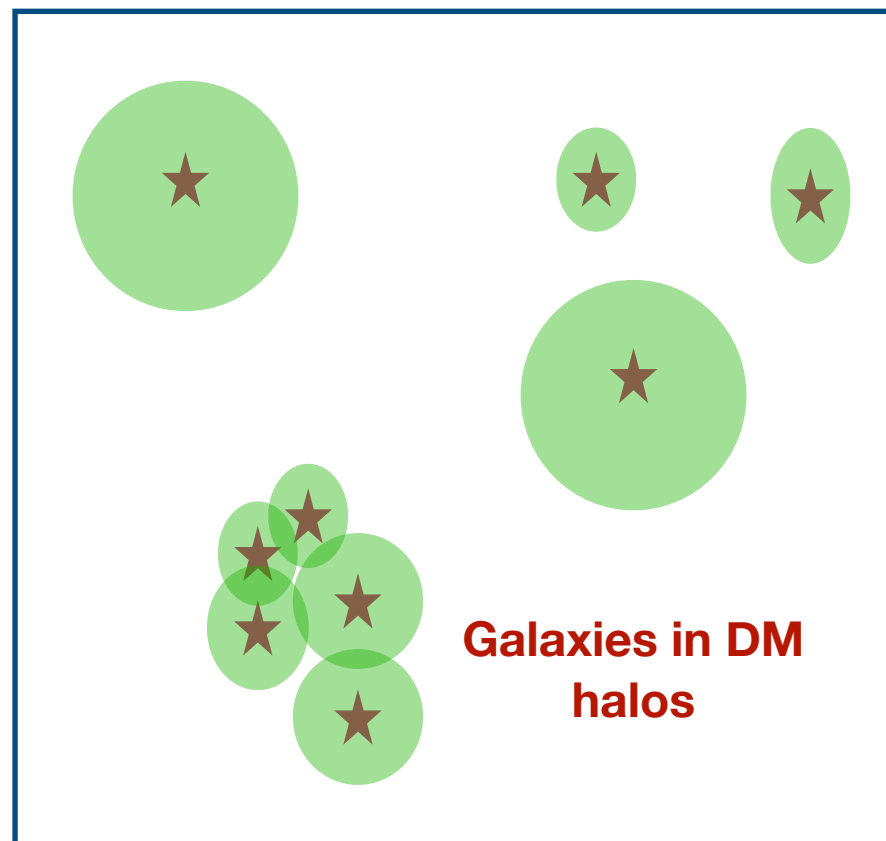
Modelling the 21cm signal : BEO RN

(**B**ubbles during the **E**POCH of **R**eionisation **N**umerical simulator)

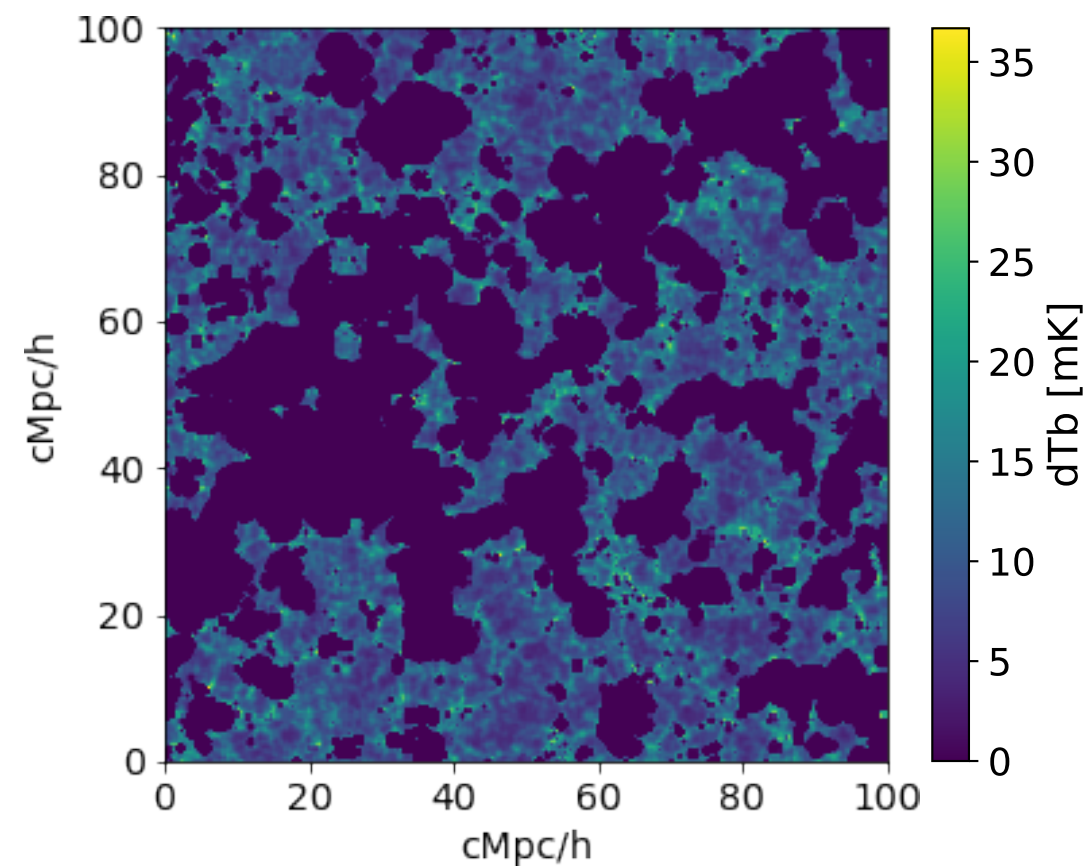
Methodology : based on source distribution and 1D radial profiles

Radial profiles (xHII, Tk, ly-alpha)

Cosmological volume

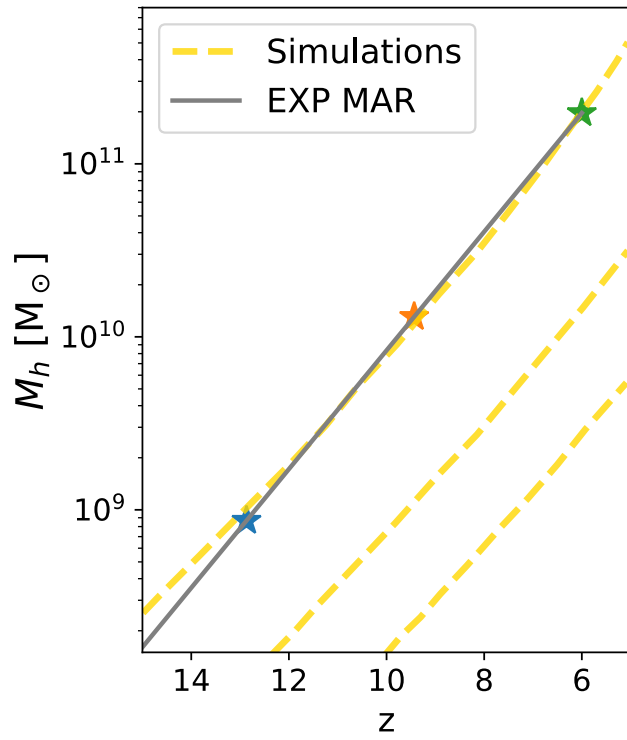


Ionisation, temperature,
dTb maps

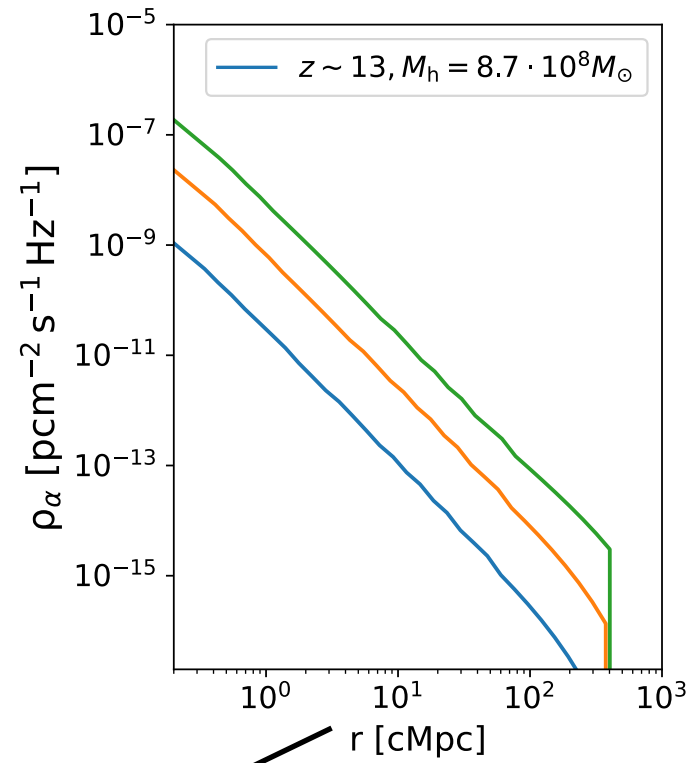


1D radial profiles

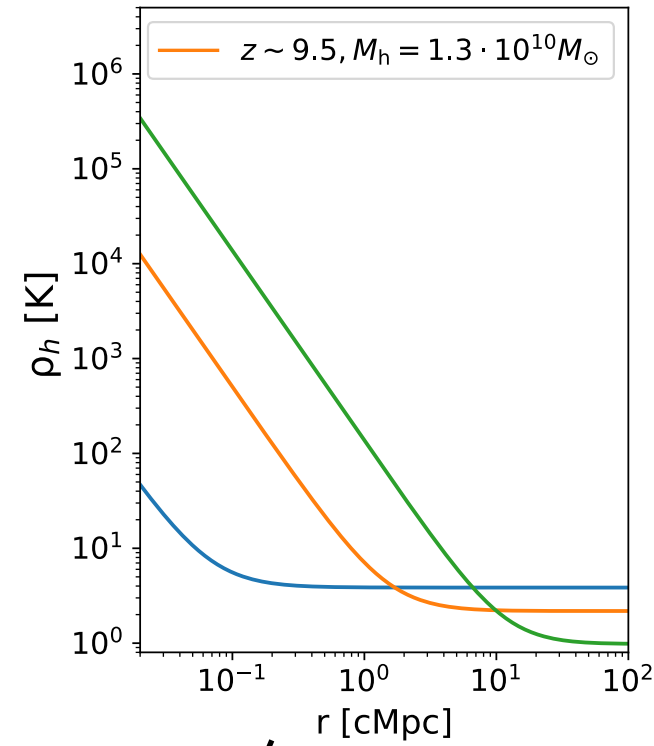
Halo growth



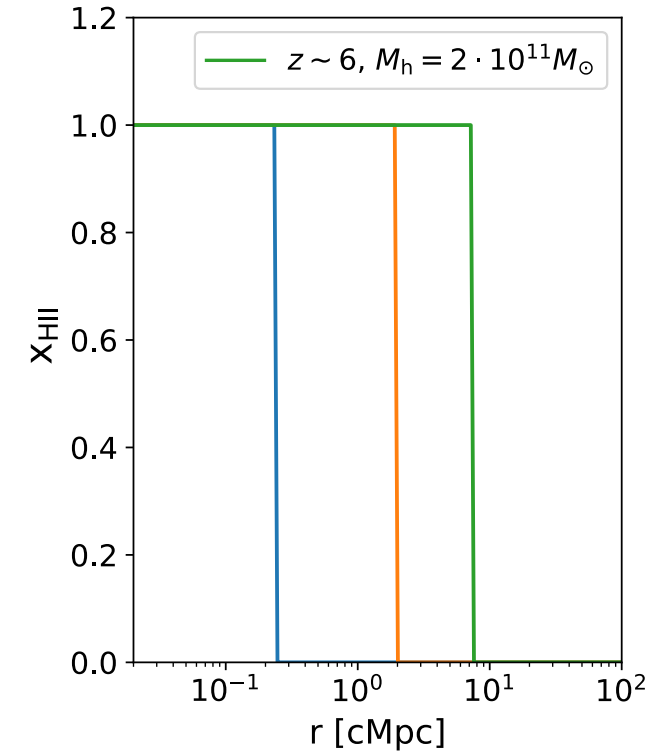
Ly-a flux



Temperature (Tk)



Ionisation (xHII)



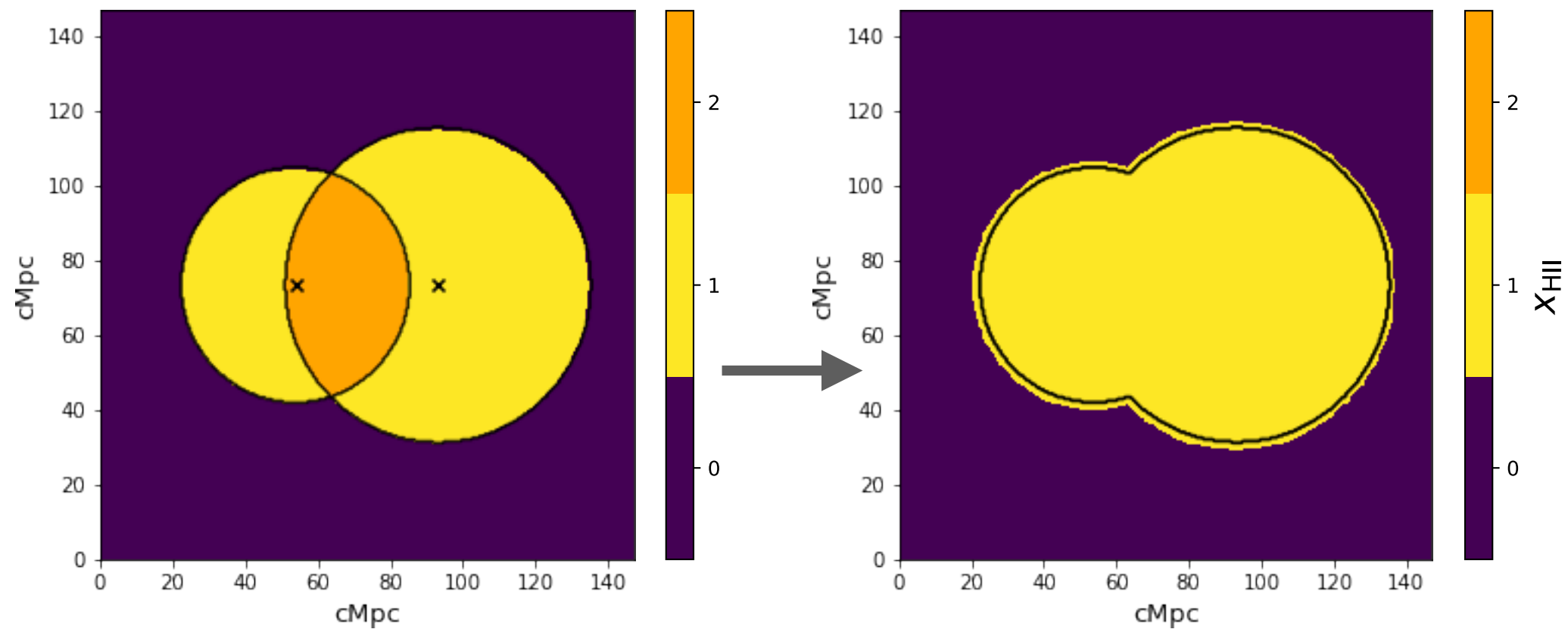
$$\rho_{\alpha}(r|M_h, z) = \frac{1}{4\pi r^2} \sum_{n=2}^{n_m} f_n \epsilon_{\alpha}(v') f_*(M_h(z')) \dot{M}_h(z')$$

$$\frac{3}{2} \frac{d\rho_h(r|M_h, z)}{dz} = \frac{3\rho_h(r|M_h, z)}{(1+z)} - \frac{\rho_{\text{xray}}(r|M_h, z)}{k_B(1+z)H(z)}$$

$$\frac{dV}{dt} = \frac{\dot{N}_{\text{ion}}(t)}{\bar{n}_H^0} - \alpha_B \frac{C}{a^3} \bar{n}_H^0 V,$$

Overlap of 1D radial profiles

- **Ionisation bubbles:** Redistribute “overionised” pixels to the nearest grid points



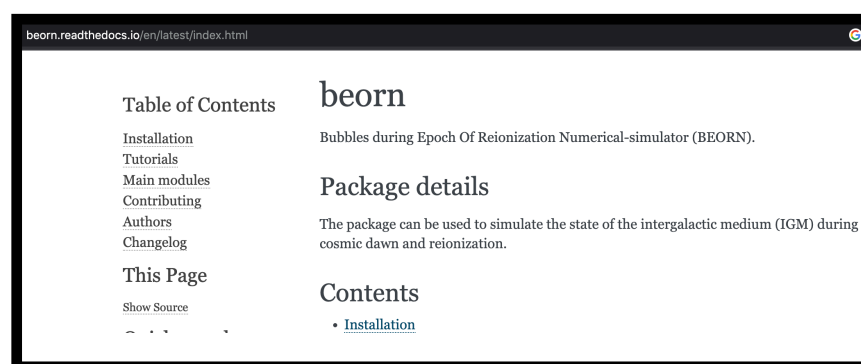
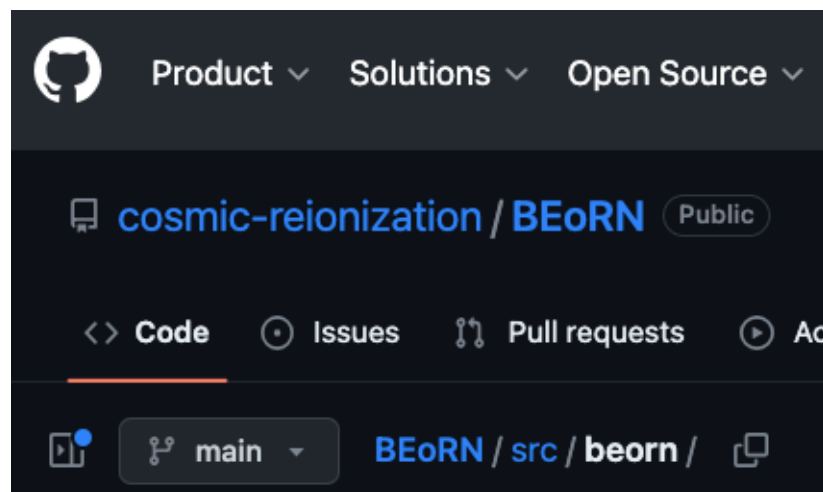
BEoRN

(***B**ubbles during the **E**POCH of **R**eionisation **N**umerical simulator*)

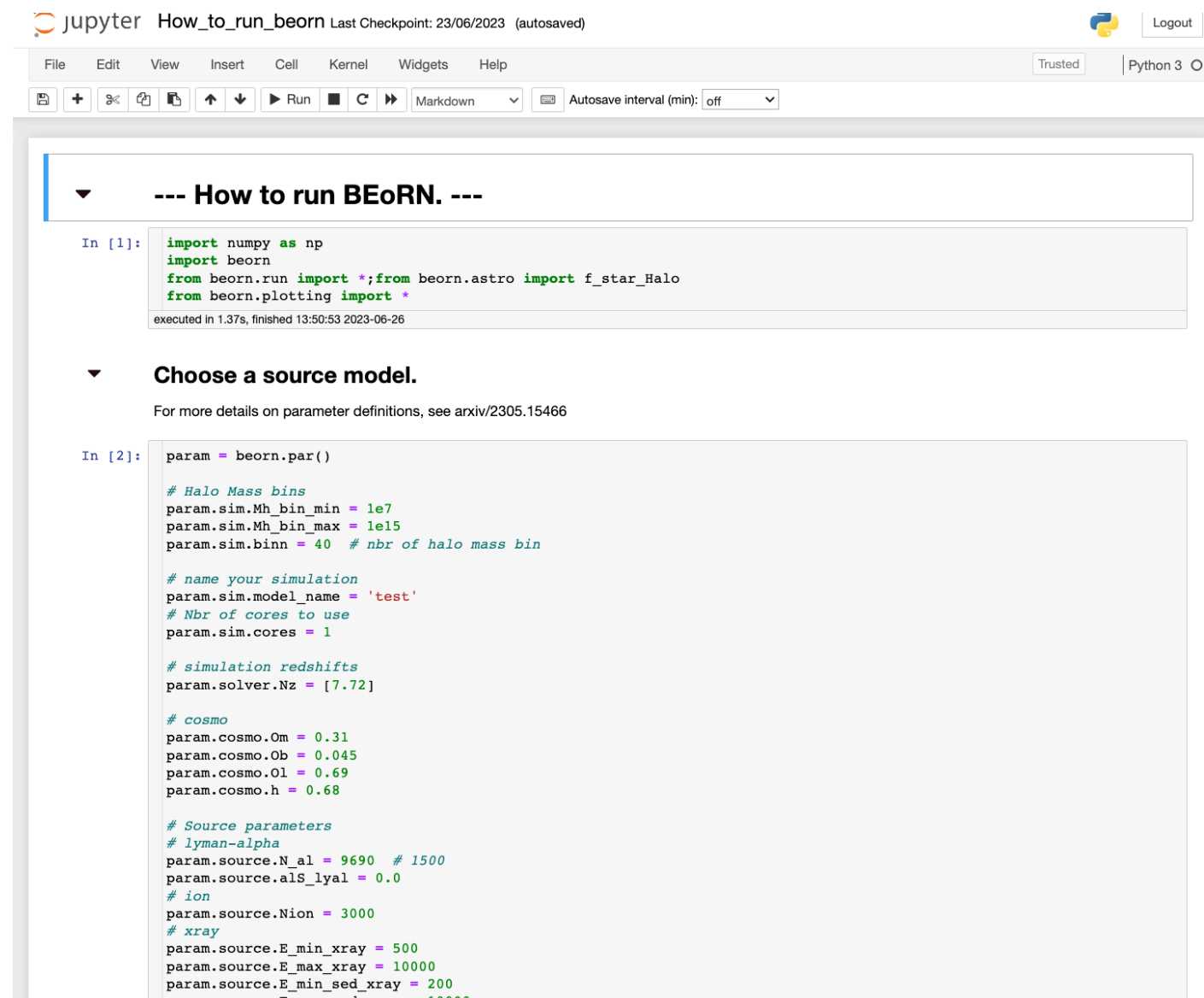
Publicly available, flexible, user-friendly

<https://github.com/cosmic-reionization/BEoRN>

Readthedoc and example Jupyter notebook



(in development)



2- What kind of cosmic dawn and reionisation signals can we expect given current constraints from high- z observations ?

Realistic simulation of the 21cm signal

Pipeline :

1. Run N-body

N-body sim :

Lbox: 147cMpc

2048³ particles

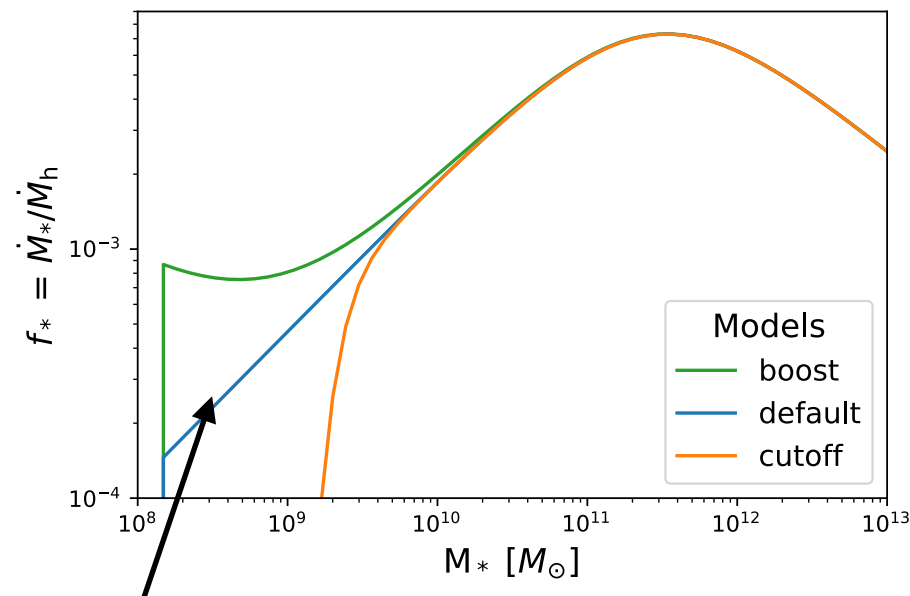
Mpart = 10⁷ Msol/h

2. Calibrate astrophysical parameters (f^* , f_{esc} , x-ray amplitude) to observation (UV luminosity fct, estimate of xHII, low-z HMXB observation)

3. Run BEoRN

3 realistic scenarios : source parameters

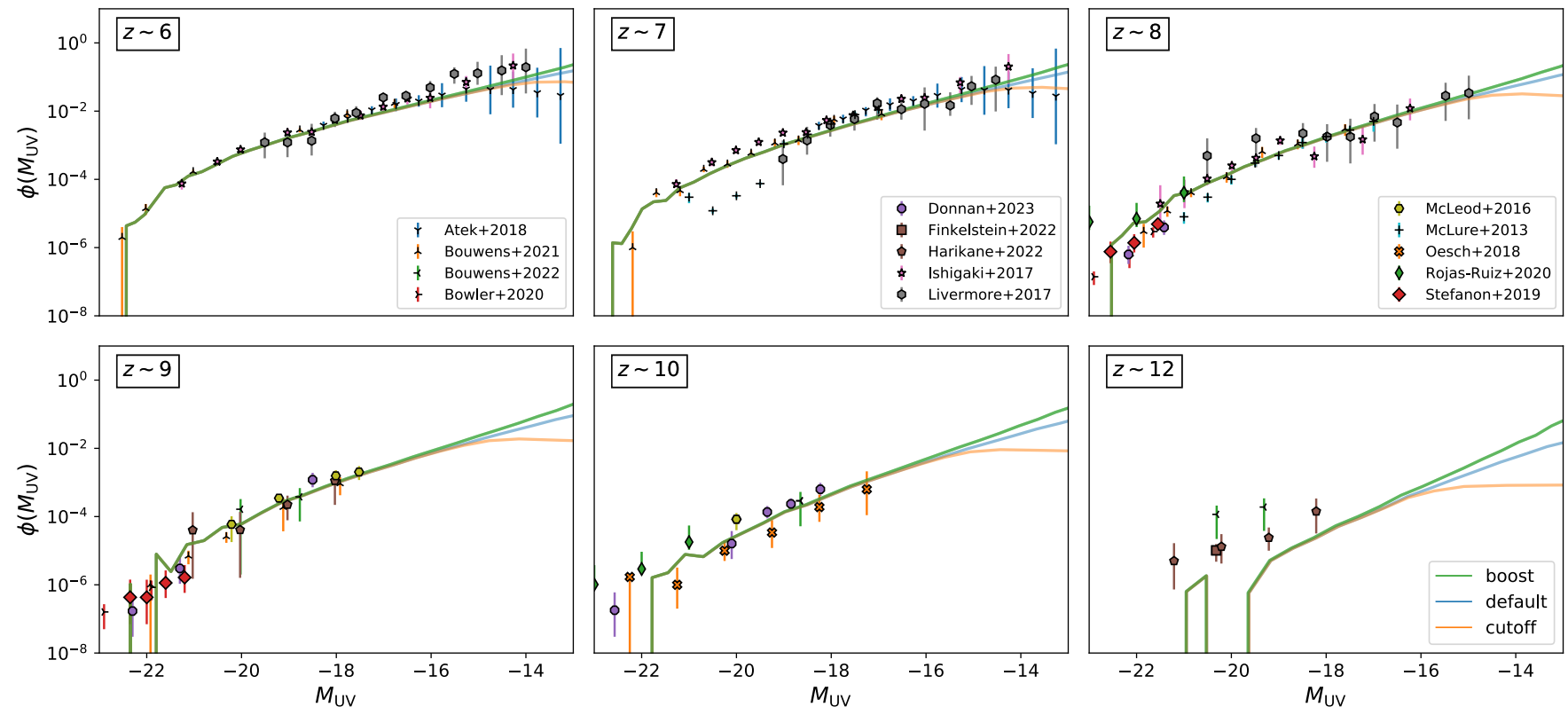
Stellar-to-halo



The UV **luminosity function** constraints the **stellar-to-halo relation**

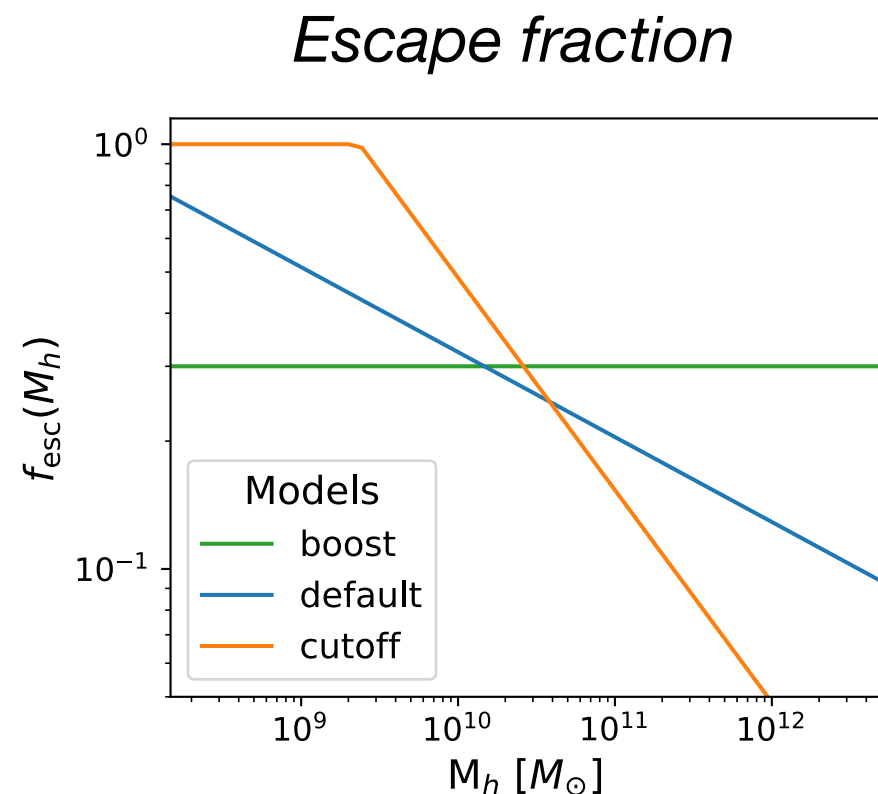
Luminosity function : theory vs data

Unconstrained
at small scales

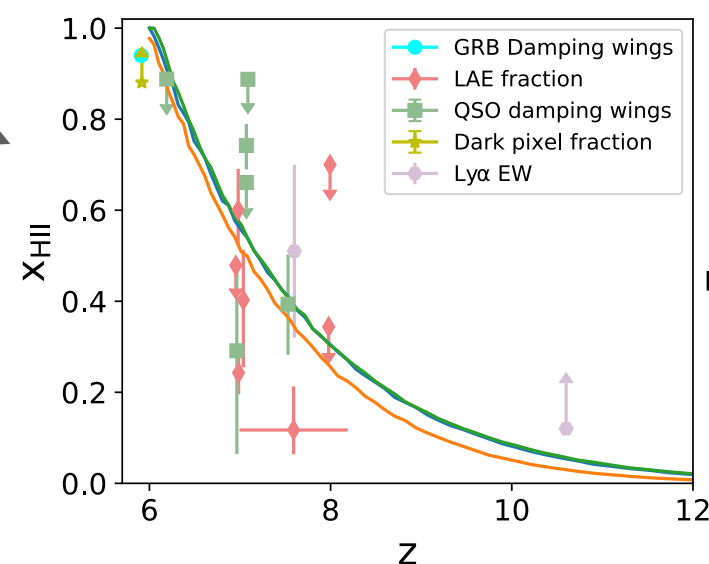


3 realistic scenarios : source parameters

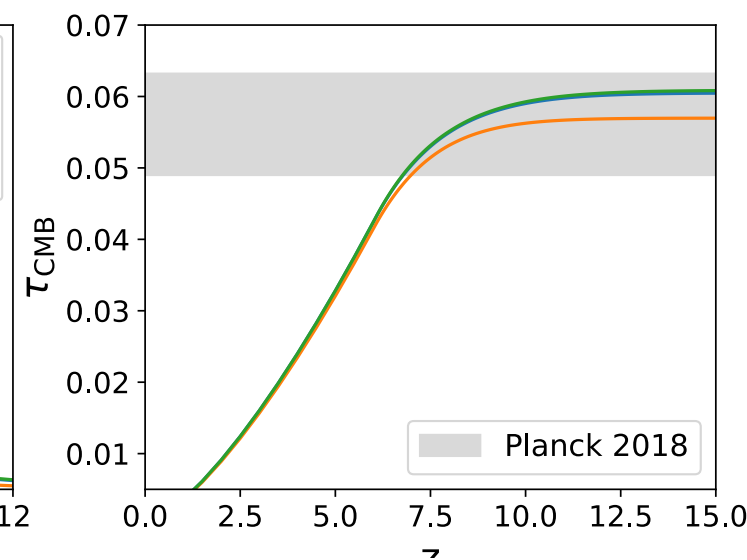
Estimates of xHII: put constraints on the **escape fraction** of ionising photons



Reionisation history



CMB

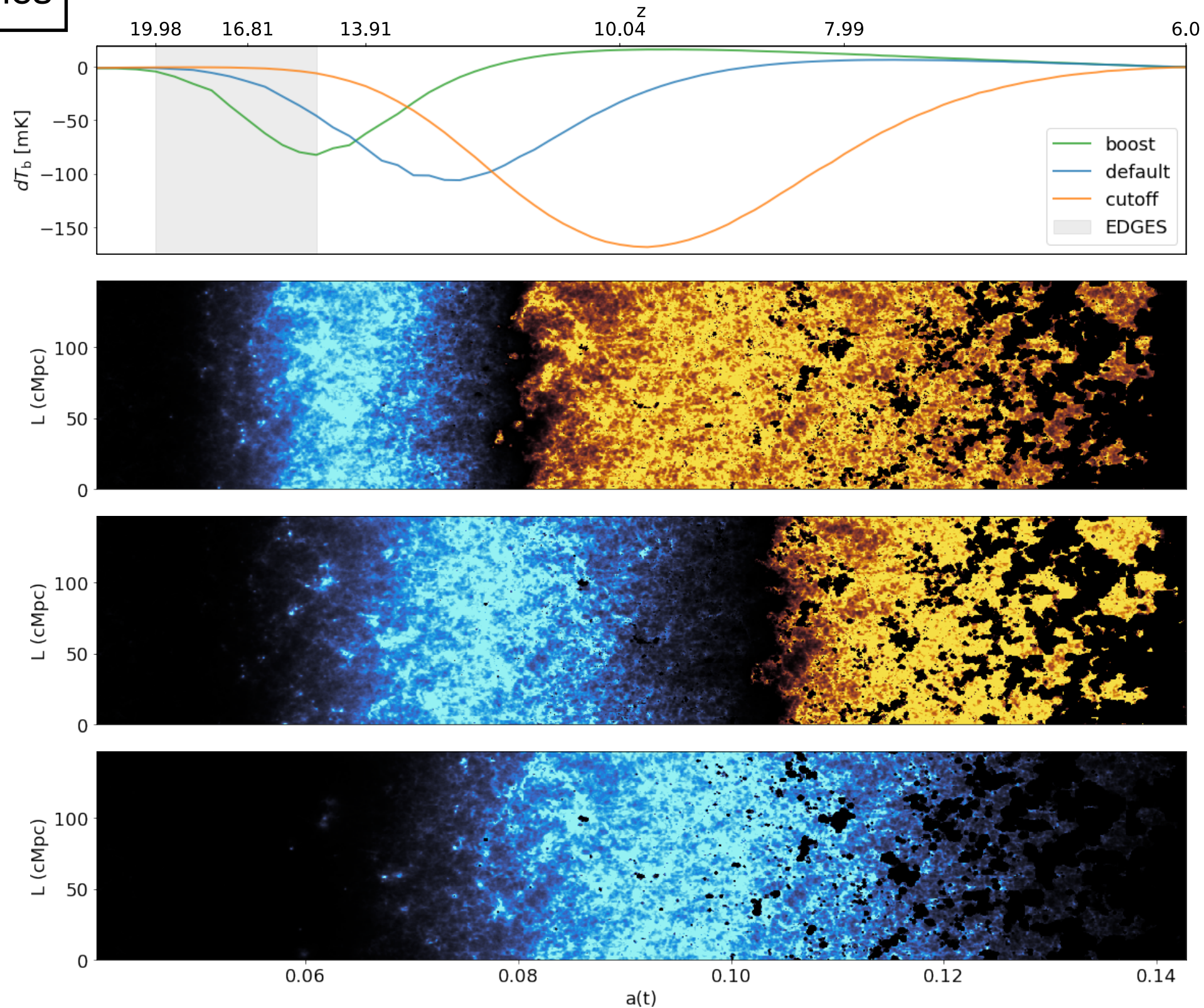


X-ray parameters : $c_X = 10^{40.5} \text{ erg s}^{-1} \text{ yr } M_{\odot}^{-1}$

The true normalisation of the x-ray spectrum is highly uncertain \rightarrow we vary $f_X = 0.1, 1, 5$ (cutoff, default, boost)

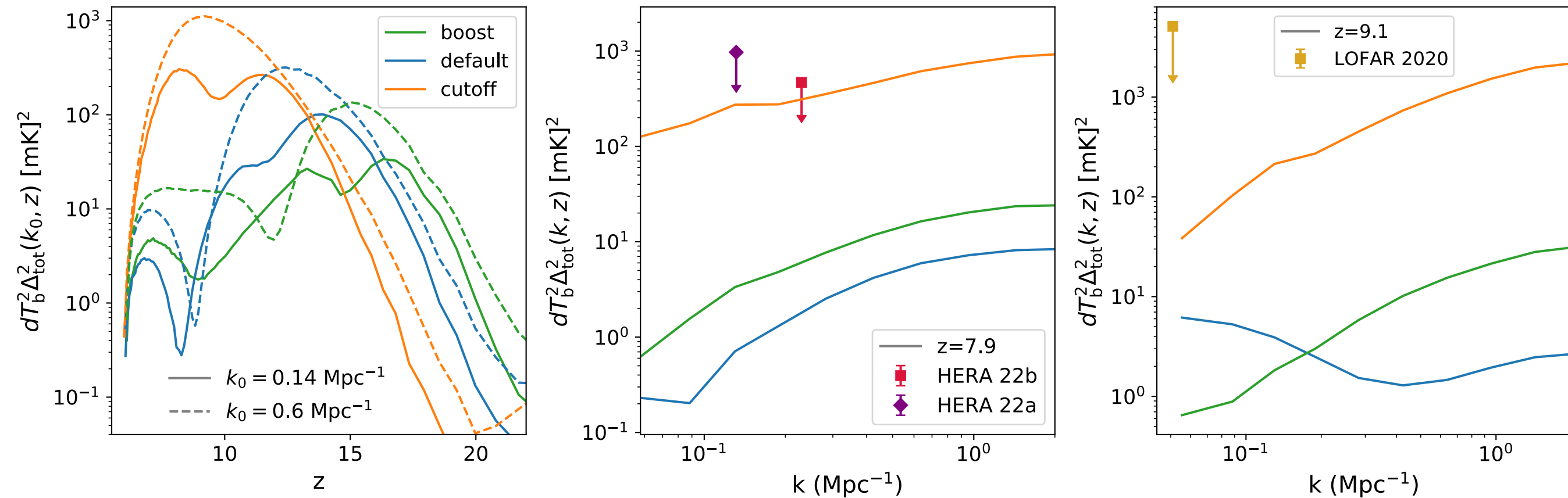
3 realistic scenarios for the Cosmic Dawn

Lightcones



3 realistic scenarios for the Cosmic Dawn

21cm signal (Power spectrum)



—> Large variety of 21cm signal still allowed by current observation

3- Halo Model approach for 21cm

*(A fast analytical method to compute the 21cm
power spectrum in ~sec)*

The Halo model (HM) implementation of BEoRN

(Analytical calculation of the 21cm PS)

How it works :

1- Express dT_b perturbations as a function of **matter** (b), **Ly- α** (α), **Tk** (T) and **xHII** (r) perturbations

$$dT_b \propto (1 - x_{\text{HII}})(1 + \delta_b)(1 - \frac{T_\gamma}{T_k})(\frac{x_\alpha}{1 + x_\alpha})$$

$$dT_b = \bar{T}_{21}(1 + \delta_{21})$$

$$x_\alpha = \bar{x}_\alpha(1 + \delta_\alpha)$$

$$T_k = \bar{T}_k(1 + \delta_T)$$

$$x_{\text{HII}} = \bar{x}_{\text{HII}}(1 + \delta_r)$$

To first order in **Ly- α** (α) and **Tk** (T):

$$\begin{aligned} \longrightarrow \delta_{21} = & \beta_r \delta_r + \beta_b \delta_b + \beta_T \delta_T + \beta_\alpha \delta_\alpha \\ & + \beta_r \beta_b \delta_r \delta_b + \beta_r \beta_T \delta_r \delta_T + \beta_r \beta_\alpha \delta_r \delta_\alpha - \delta_{dv} \end{aligned}$$

Halo model (HM) implementation of BEoRN

(Analytical calculation of the 21cm PS)

How it works :

2- Compute auto and cross PS using HM formalism,
replacing NFW by **1D radiation flux profiles** :

$$P_{21}^{(\text{lin})} = P_{r,r} + P_{b,b} + P_{T,T} + P_{\alpha,\alpha} \\ + 2(P_{r,b} + P_{r,T} + P_{r,\alpha} + P_{b,T} + P_{b,\alpha} + P_{T,\alpha})$$

X, Y Individual fields :

(b) : matter

(a) : Ly- α ,

(T) : Tk

(r) : xHII

$$P_{XY}^{1h}(k, z) = \frac{\beta_X \beta_Y}{(\bar{\rho} f_{\text{coll}})^2} \int dM \frac{dn}{dM} \tilde{f}_*^2 M^2 |u_X| |u_Y|,$$

$$P_{XY}^{2h}(k, z) = \frac{\beta_X}{(\bar{\rho} f_{\text{coll}})} \int dM \frac{dn}{dM} \tilde{f}_* M |u_X| b_X \\ \times \frac{\beta_Y}{(\bar{\rho} f_{\text{coll}})} \int dM \frac{dn}{dM} \tilde{f}_* M |u_Y| b_Y \times P_{\text{lin}}$$

$$P_{XY}(k, z) = P_{XY}^{1h}(k, z) + P_{XY}^{2h}(k, z),$$

Ingredients :

-P_{lin}

-b_X : halo matter bias

-u_X : 1D profiles

-dn/dM : HMF

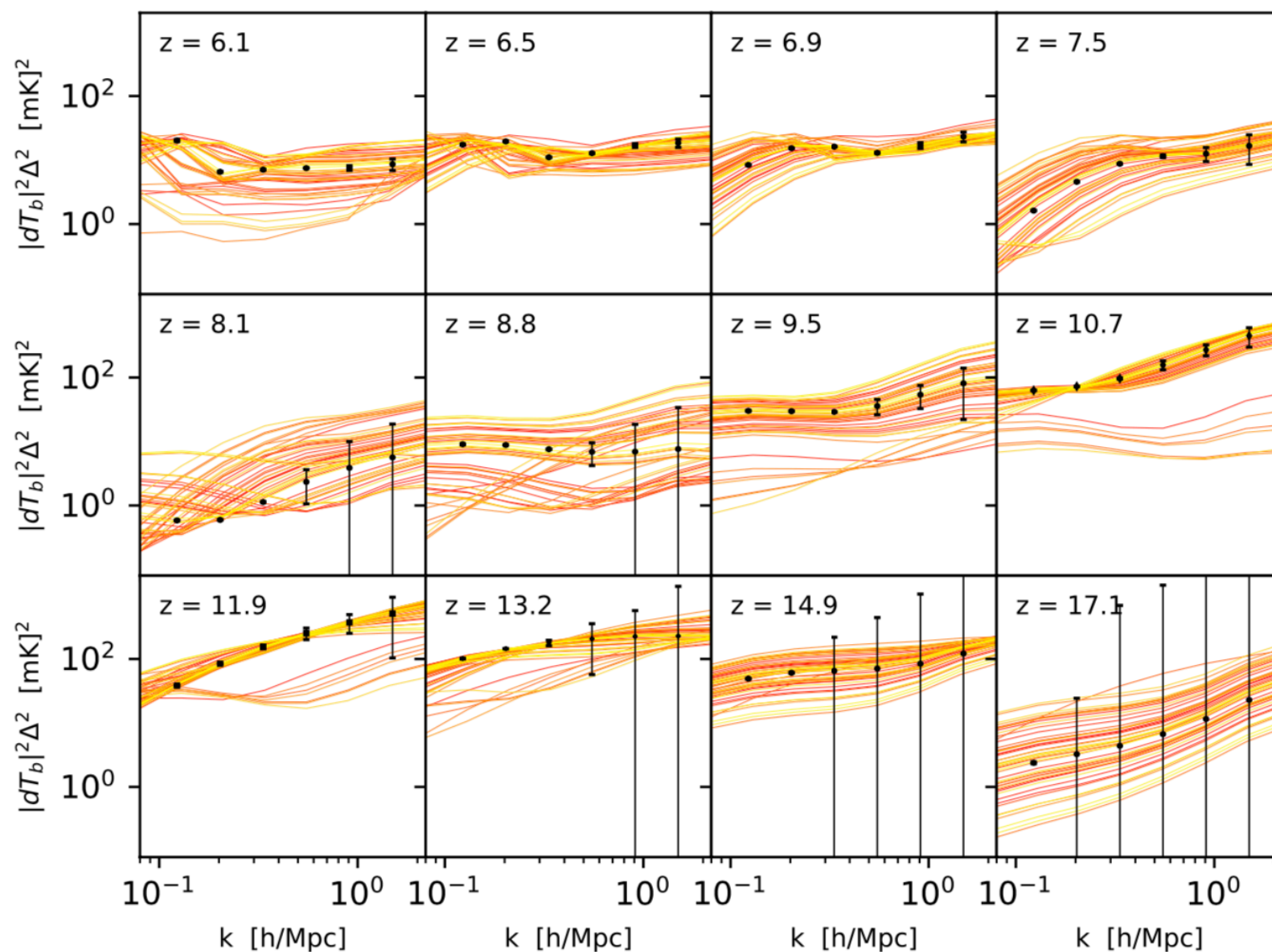


Computes P21 in ~20 sec

4- Cosmological forecast for SKA using the HM approach

Results : Cosmological forecast for SKA using the HaloModel

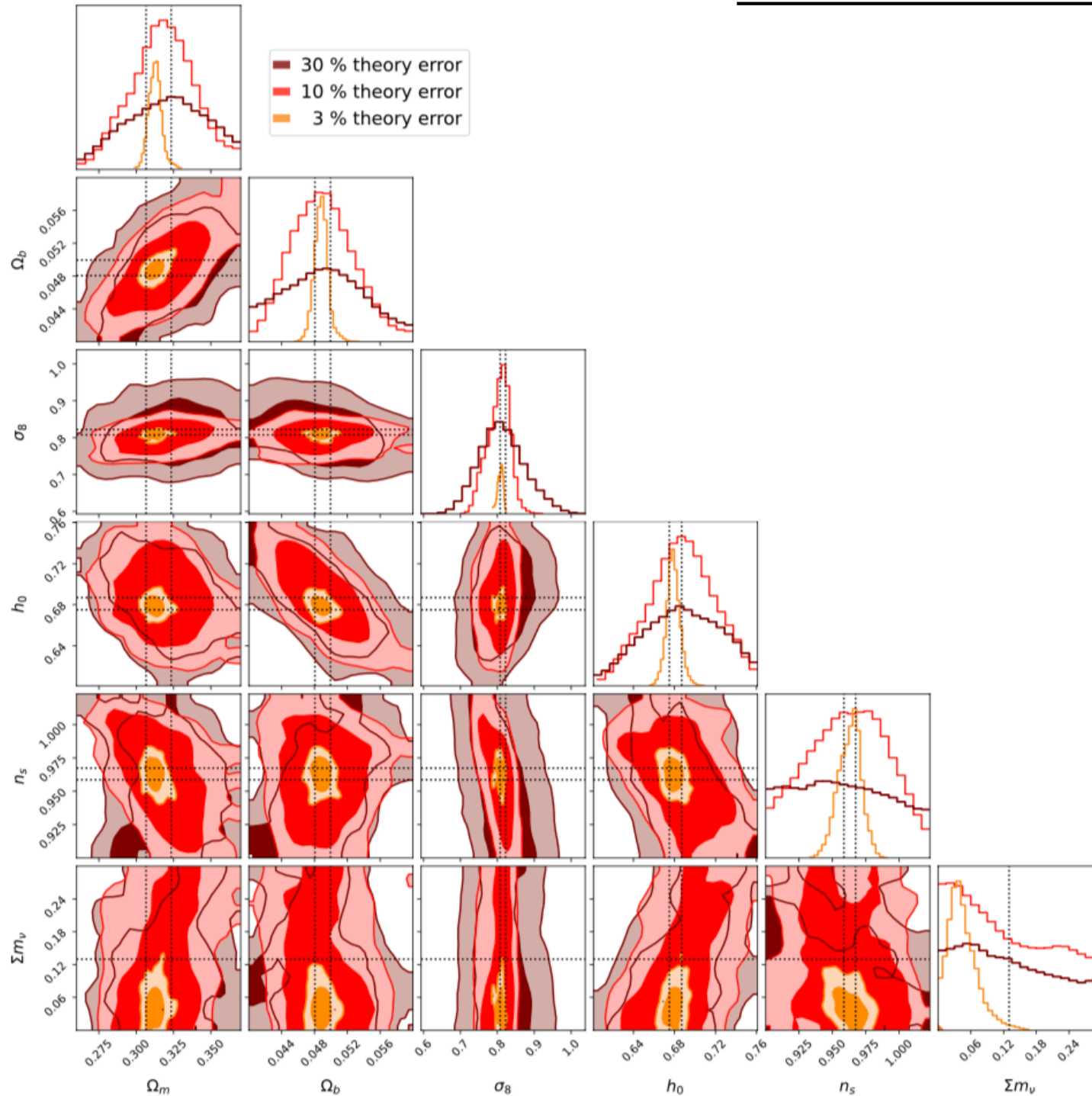
Mock Power Spectrum data (1000h):



- Foreground : scale cut
(keep $0.1 < k < 1.5$ h/Mpc)
- Instrumental noise (SKA-low
512 antennae)
- Sample variance

Results : Cosmological forecast for SKA using the HaloModel

MCMC inference :



-Add a “theory” error

$$\sigma_{\text{tot}}^2 = \sigma_{\text{obs}}^2 + \sigma_{\text{th}}^2, \quad \sigma_{\text{th}} = c_{\text{th}} P_{\text{obs}}$$

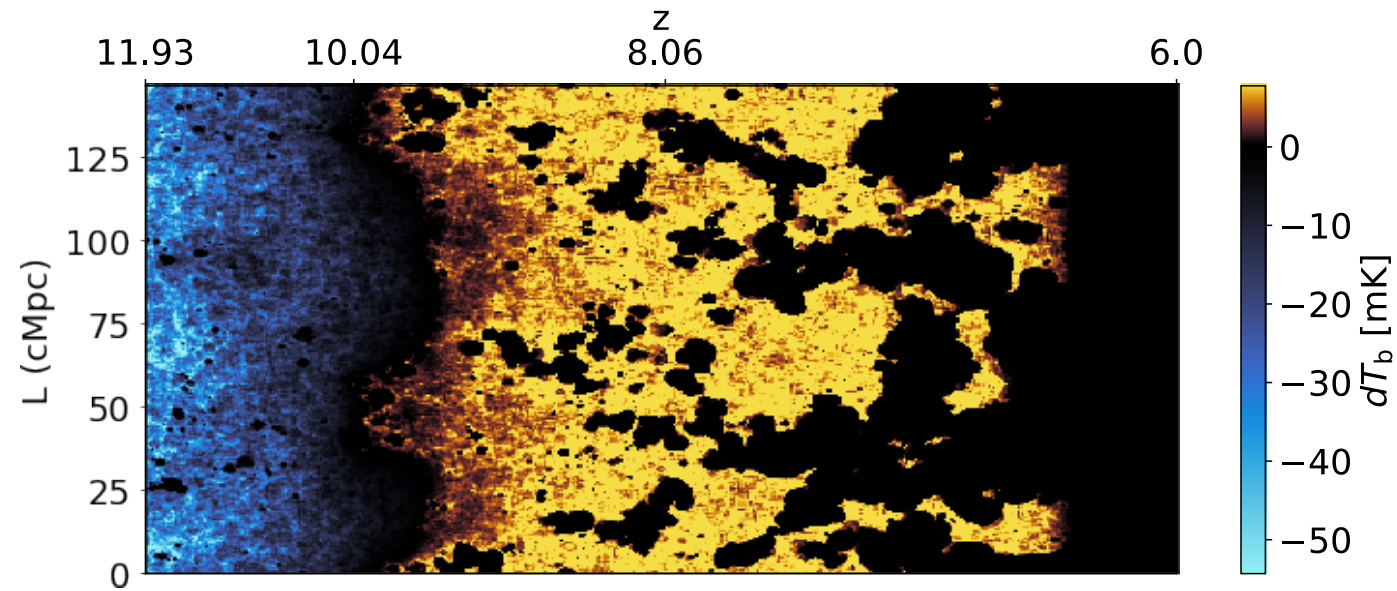
-Vary 13 parameters (cosmo + astro)

Parameter name	Acronym	mock value	prior range
Matter abundance	Ω_m	0.315	[0.27, 0.37]
Baryon abundance	Ω_b	0.049	[0.04, 0.06]
Scalar amplitude	$A_s [10^{-9}]$	2.07	[1.0, 3.5]
Hubble parameter	h	0.68	[0.6, 0.8]
Spectral index	n_s	0.963	[0.90, 1.02]
Neutrino masses	$\Sigma m_\nu [\text{eV}]$	0.06	[0.0, 0.5]
Amplitude of f_*	$f_{*,0}$	0.1	[0.01, 1.0]
Slope of f_*	γ_2	0.5	[-0.79, -0.19]
Truncation of f_*	$M_t [M_\odot/h]$	10^8	[3.2e6, 3.2e9]
Amplitude of f_{esc}	$f_{\text{esc},0}$	0.1	[0.01, 1.0]
Slope of f_{esc}	α_{esc}	0.5	[0, 1]
Ampl. of X-ray rad.	f_X	1.0	[0.01, 10]
Min X-ray energy	$E_{\text{min}} [\text{keV}]$	0.5	[0.3, 2.0]

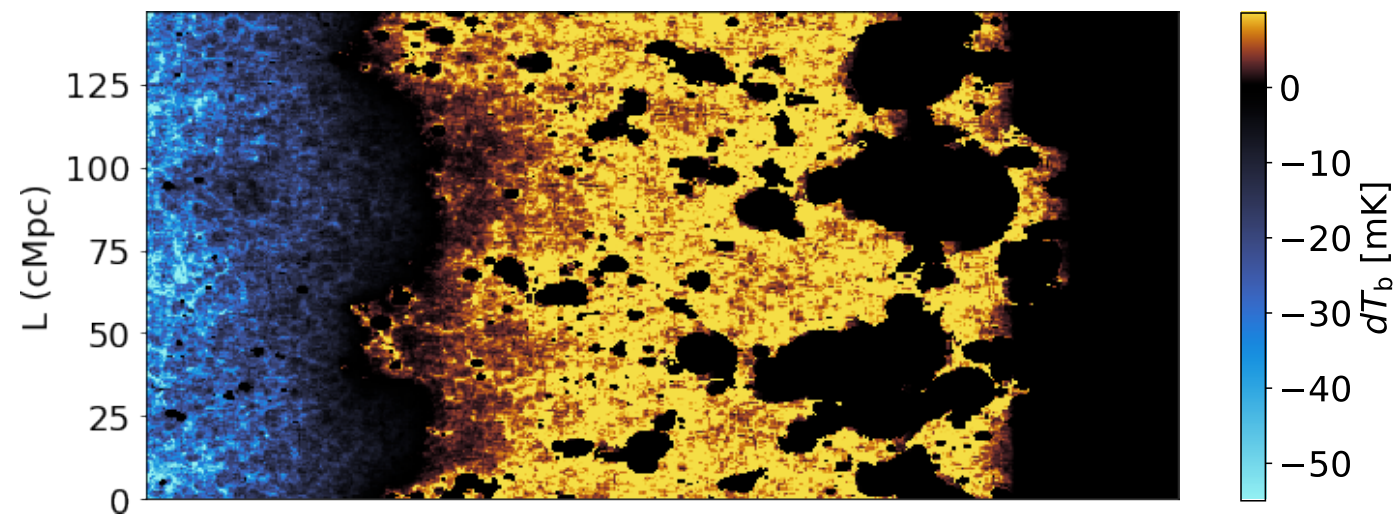
Conclusions

- BEO RN is publicly available and user friendly :
<https://github.com/cosmic-reionization/BEO RN>
- The 21-cm clustering signal is a powerful complementary probe with other high- z observations
- Assuming 3% theory error, we can expect to get constraints competitive with Planck, an independent estimate of h_0 and S_8 in a new redshift range, and a direct constraint on neutrino masses.

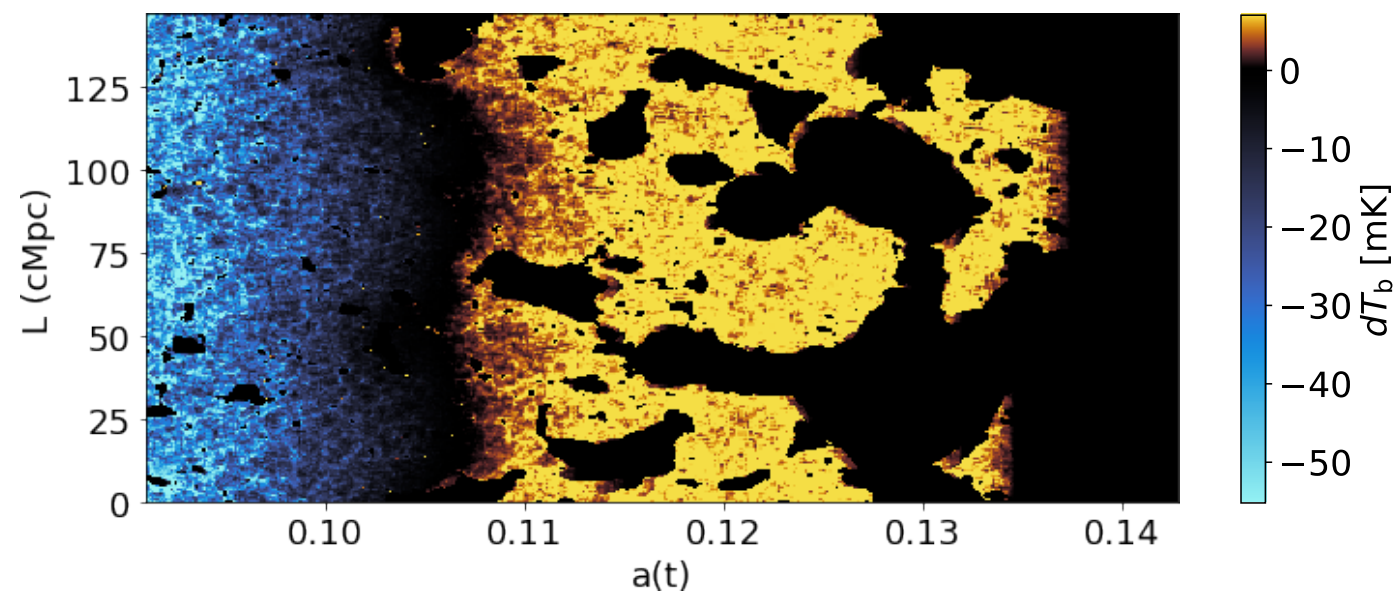
Comparison between bubble, sem-num, and excursion set :



Bubbles (BEoRN)

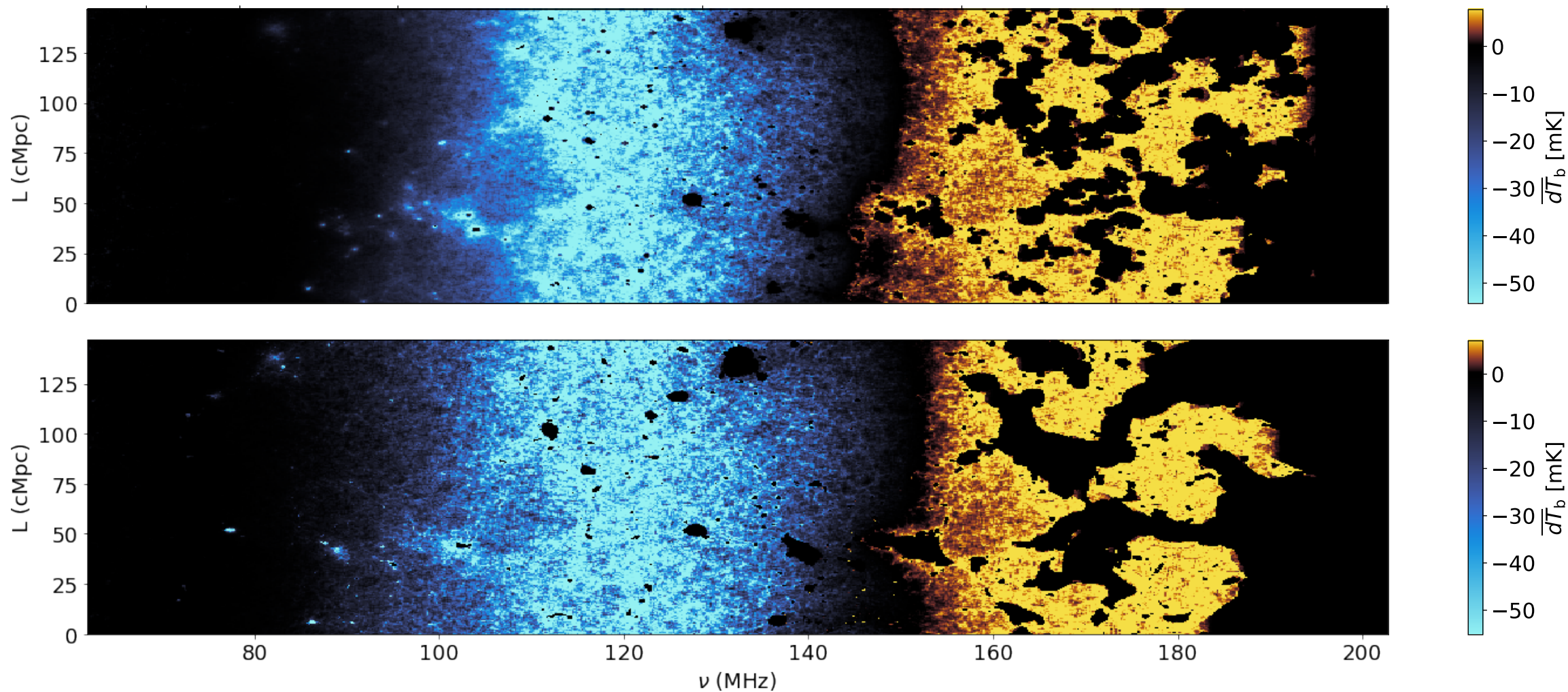
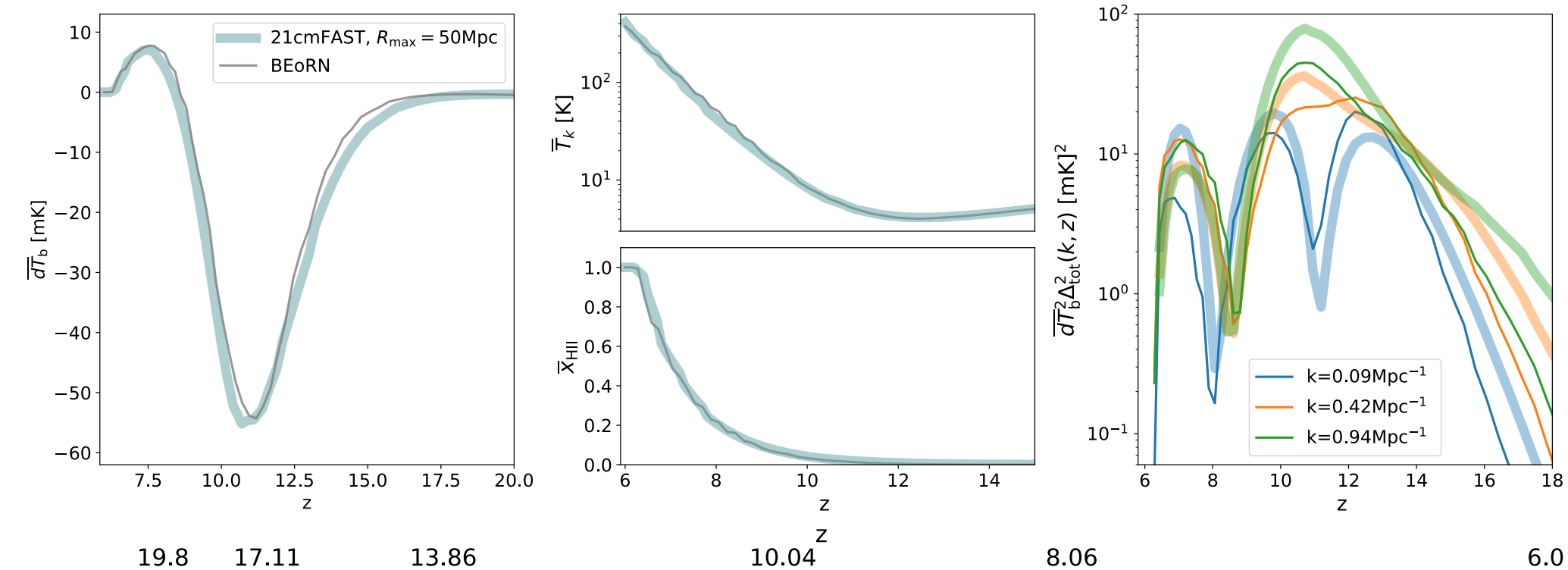


**Sem-Num (halo based,
Majumdar 2014)**

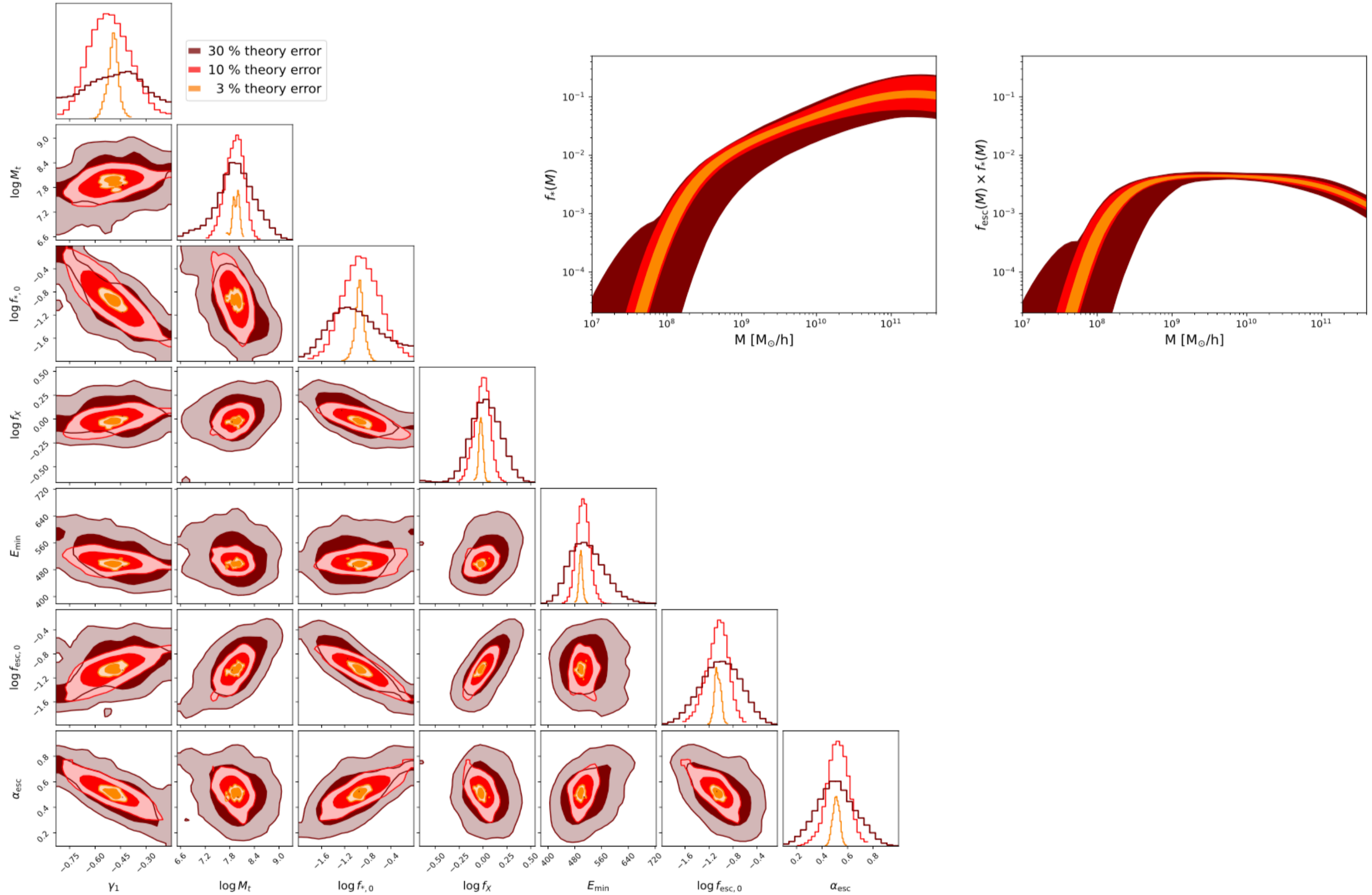


Excursion Set (21cm FAST)

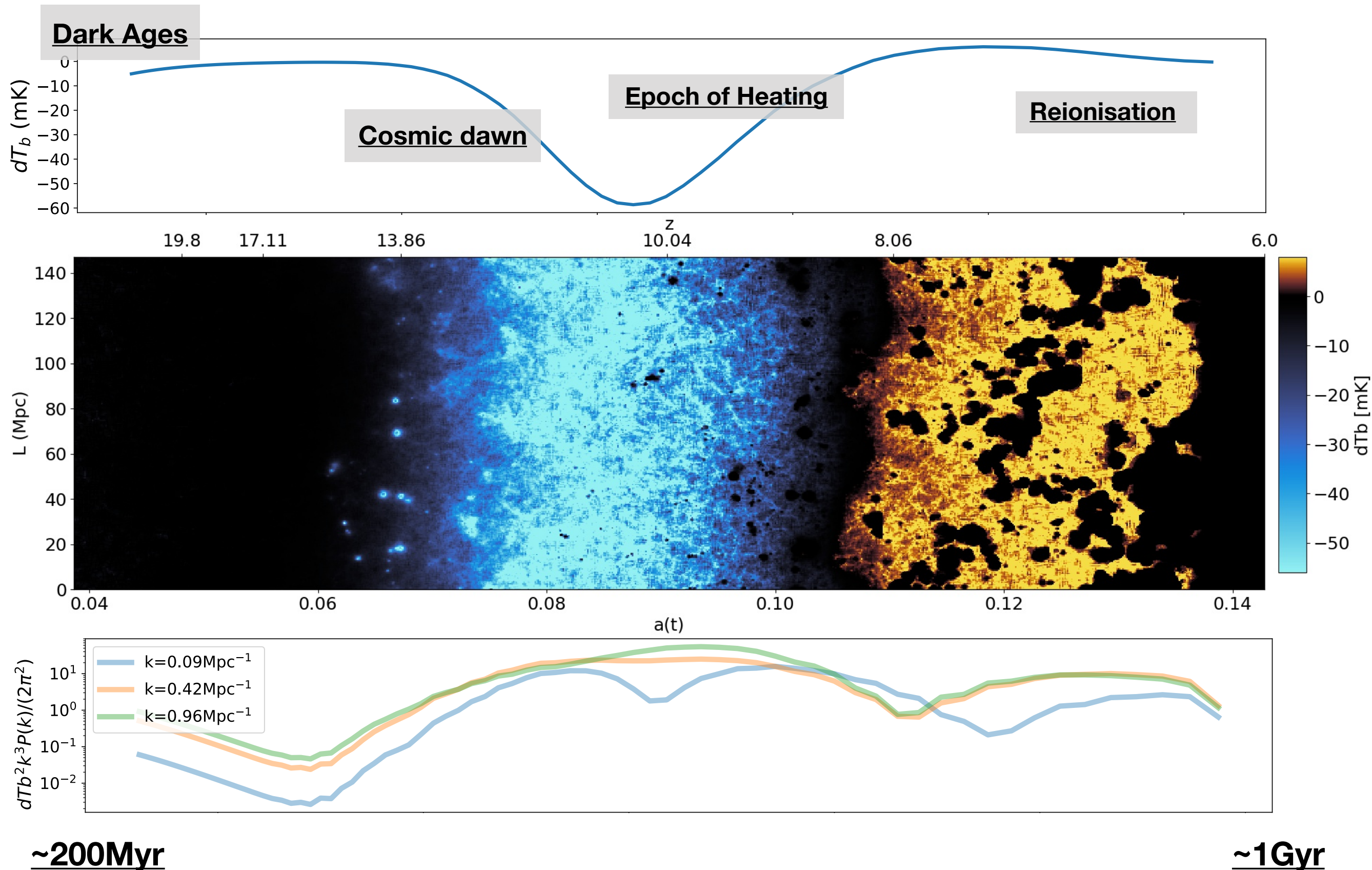
Comparison BEO RN/21cmFAST



SKA forecast on astrophysics (marginalising over cosmology)



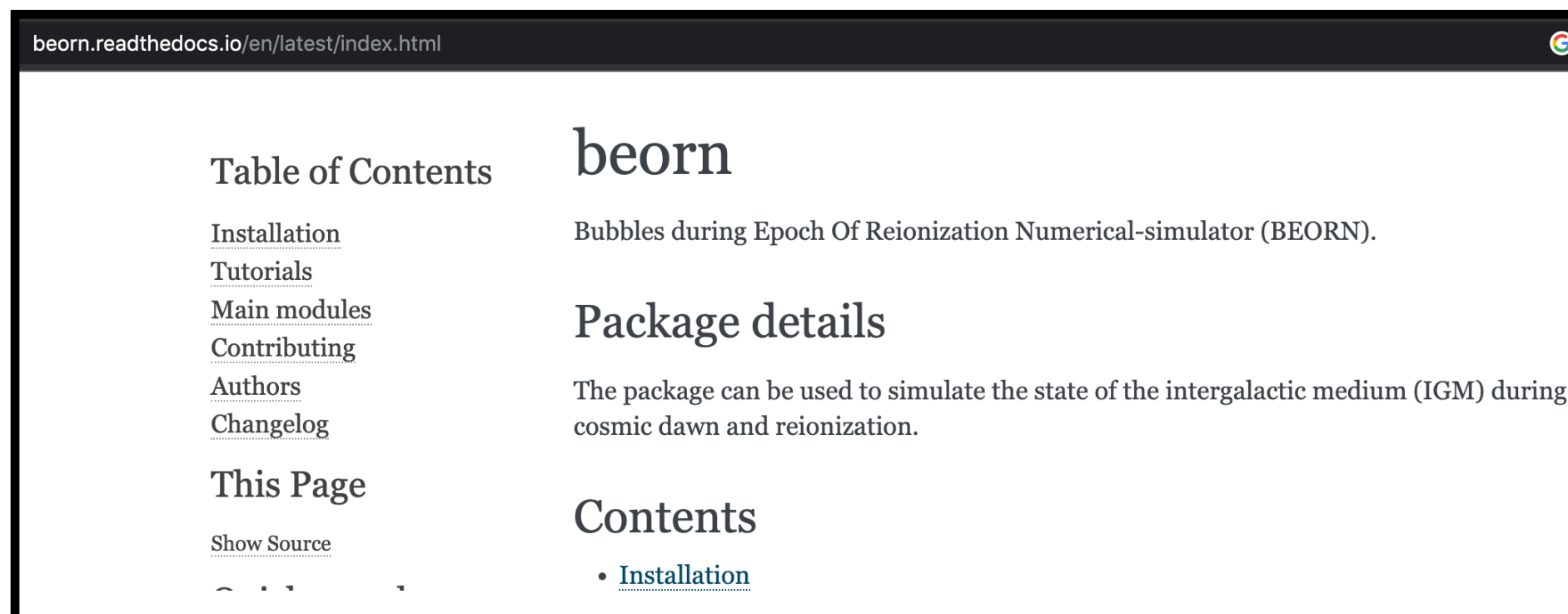
Final product : 3D dT_b maps, power spectrum



BEoRN

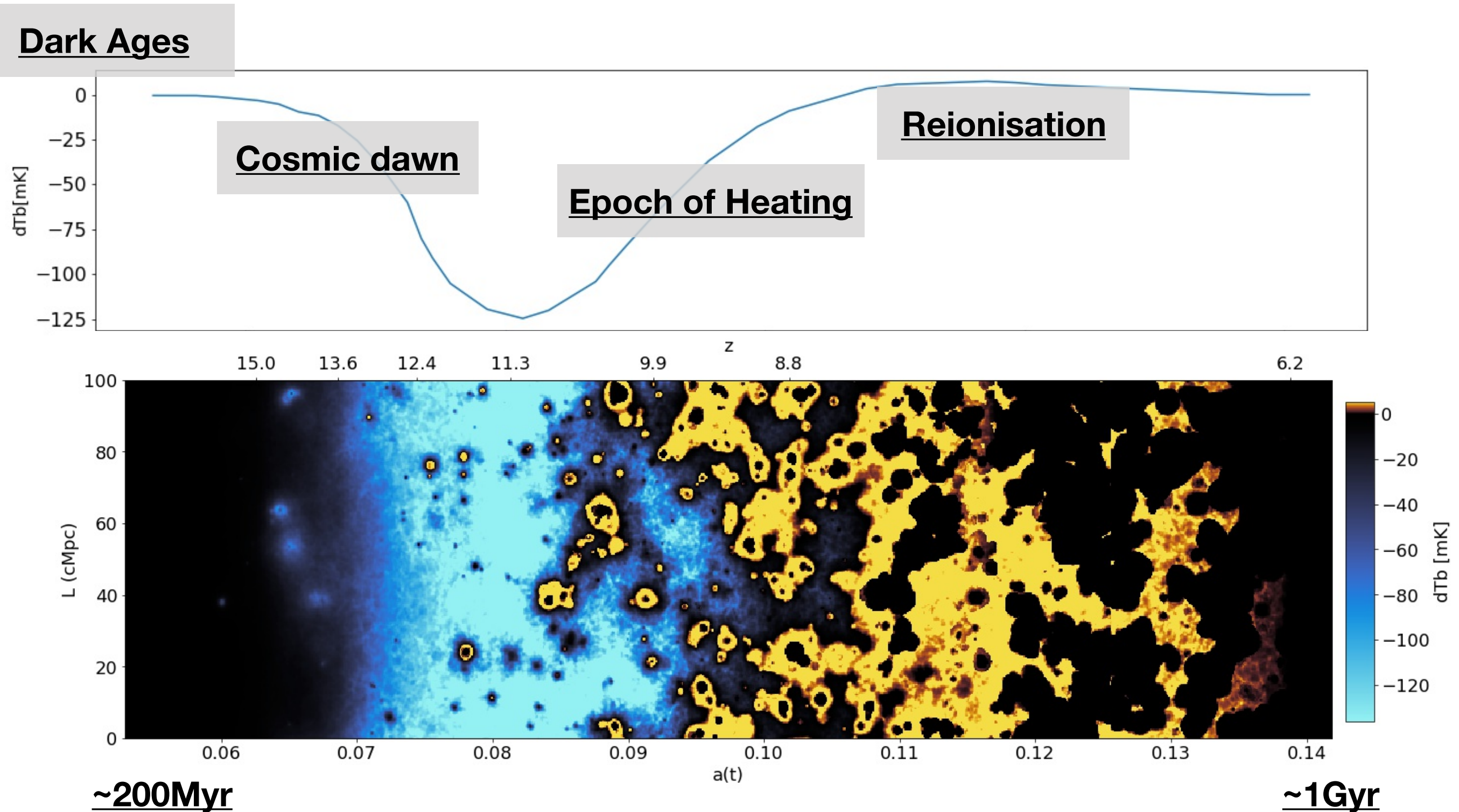
(**B**ubbles during the **E**POCH of **R**eionisation **N**umerical simulator)

Publicly available, flexible, user-friendly



(in development)

Outcome of the code



To go further

- Need Fast gravity solver/halo finder algorithms
- More accurate galactic SED (pop.II/pop.III stars)
- Modelling of X-ray sources (Qasars/ HMXBs)
- Constraints on the ionising photon escape fraction.

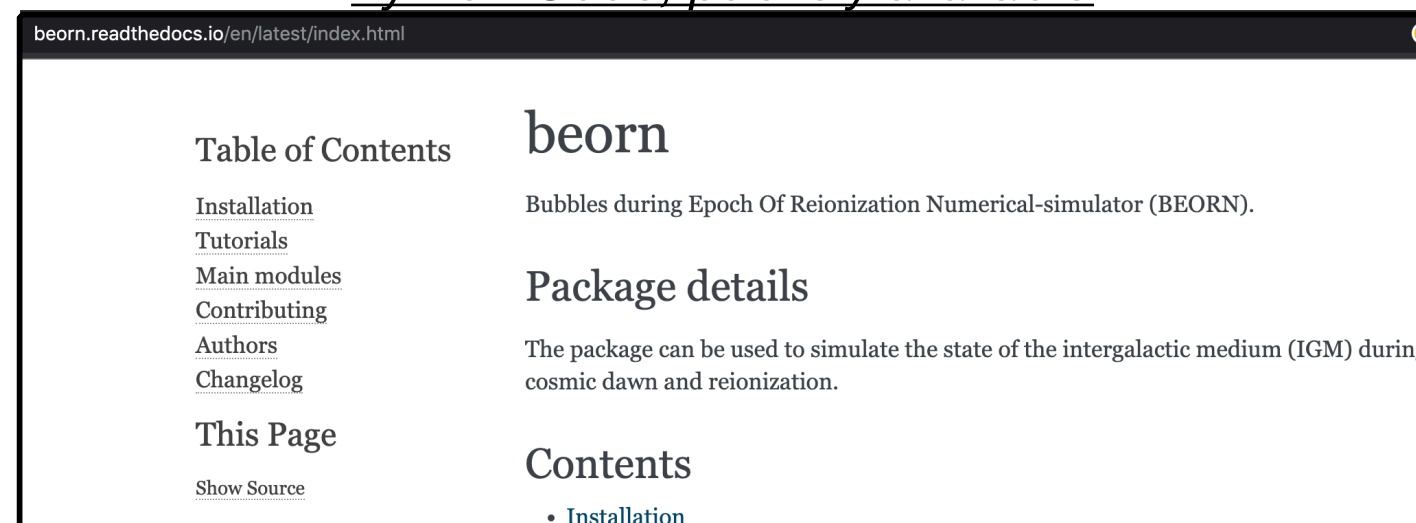
Modelling the 21cm signal : BEO RN

(**B**ubbles during the **E**POCH of **R**eionisation **N**umerical simulator)

Methodology :

1. Use N-body or LPT solver to evolve the non-linear matter field
2. Identify DM halos
3. Populate halos with galactic sources
4. Compute 1D profiles for temperature, ionisation and Ly- α flux
5. Paint the profiles on 3D grids.

Python Code, publicly available



(in development)