



Fast Simulation of Cosmological Neutral Hydrogen with a Halo Model Approach

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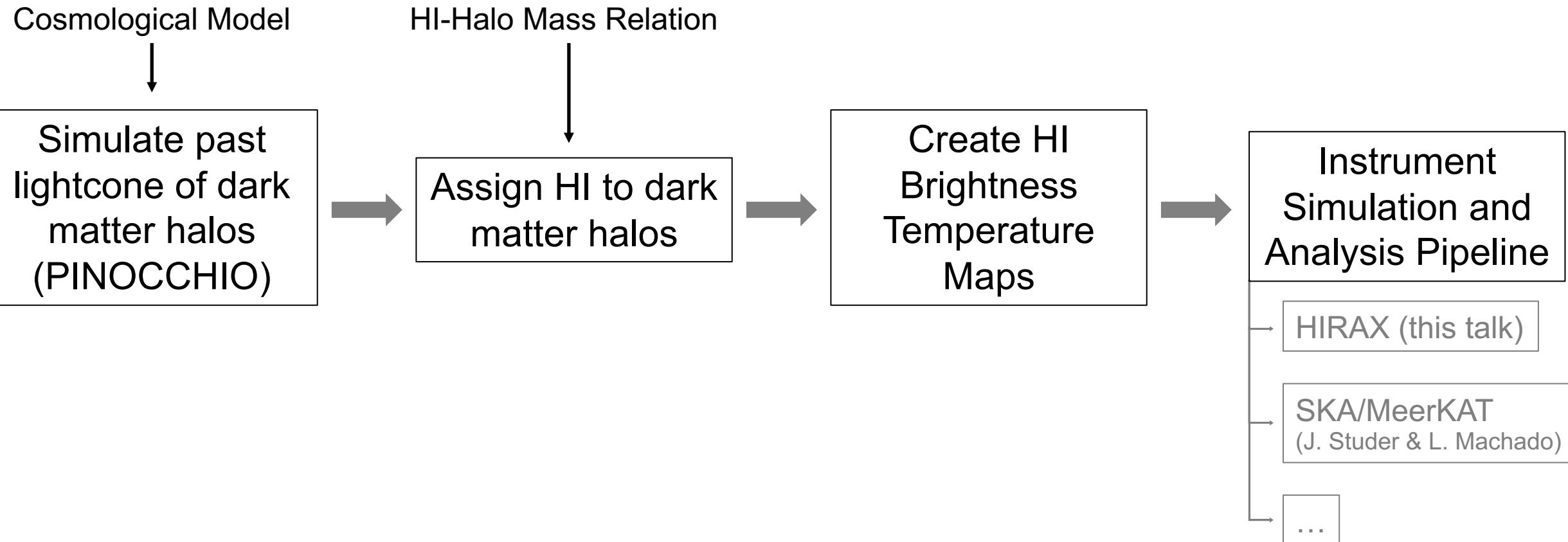
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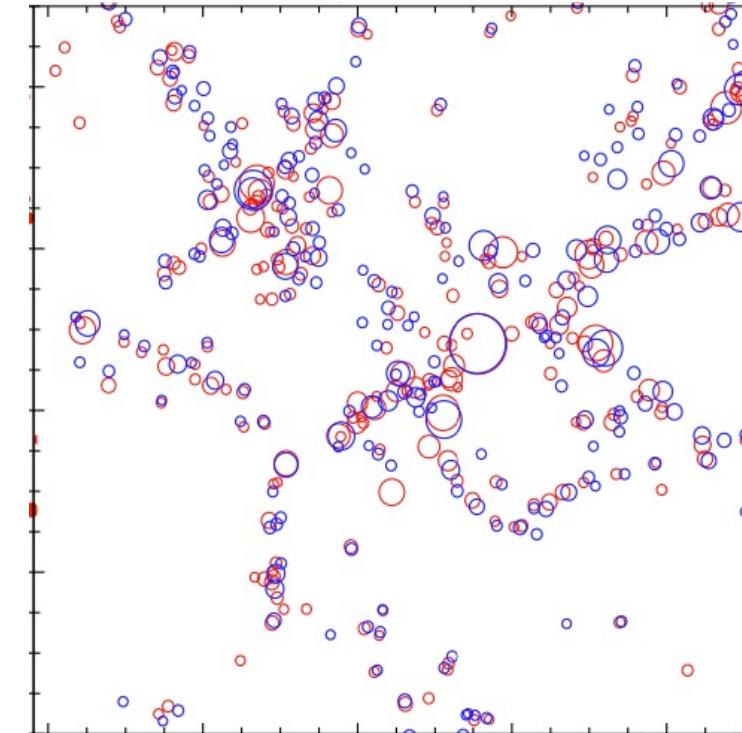
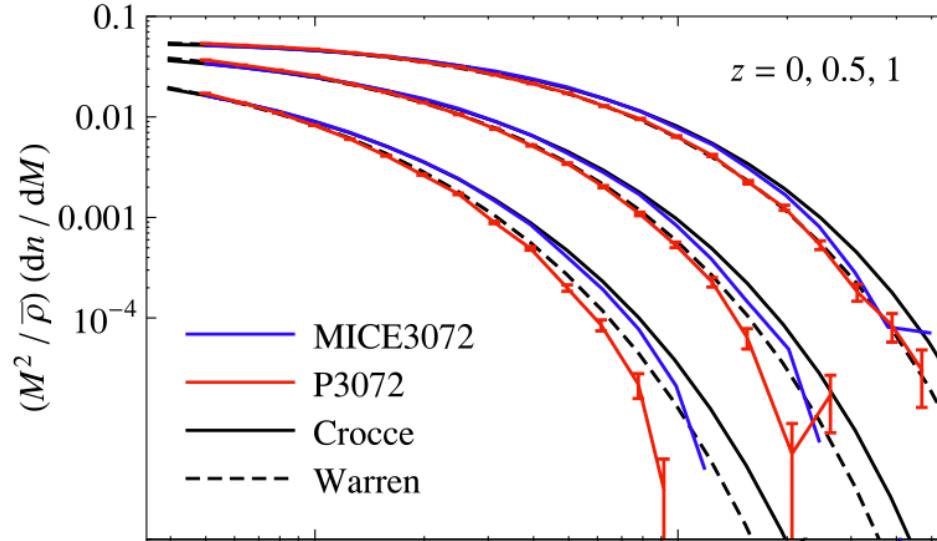
Overview

- Fast and large volume simulations of neutral hydrogen (HI) distribution
- Test instrument simulation and analysis pipeline to measure the HI emission



PINOCCHIO: Dark Matter Halo Simulation

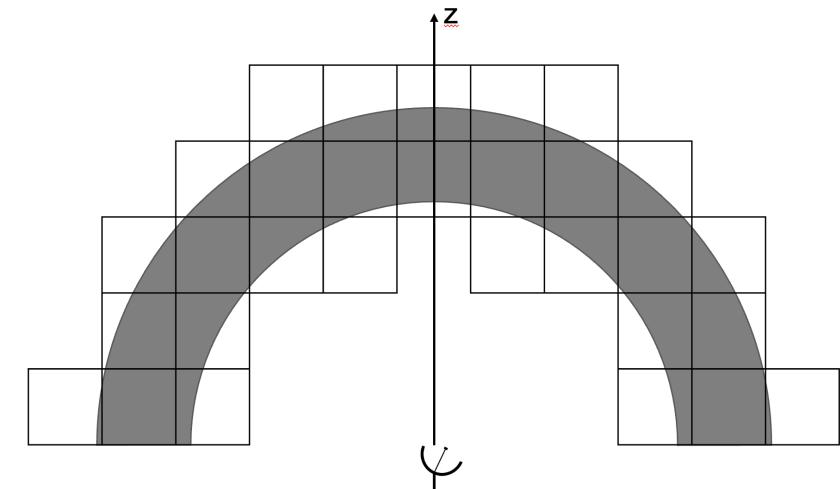
- Monaco et al. (2002, 2013), Taffoni et al. (2002), Munari et al. (2017)
- Lagrangian Perturbation Theory
- Collapsed points grouped into halos, hierarchical growth
- Catalog of dark matter halos
- Much faster than N-body



Monaco et al. 2013

Current Setting of DM Simulations

- 500 Mpc/h box size
 - 2048^3 simulation particles
 - ≥ 10 particles per halo $\leftrightarrow \geq 1.27 \times 10^{10} M_{\odot}/h$
- } → 20 – 30% HI mass missing
-
- Lightcone settings:
 - Frequency range: 700 – 800 MHz \leftrightarrow Redshift 0.77 – 1.03
 - Half sky
 - Euler Cluster of ETHZ (CPU) with MPI parallelization
 - 1032 cores over 39 nodes
 - 2.75 TB RAM, 332 CPU h runtime



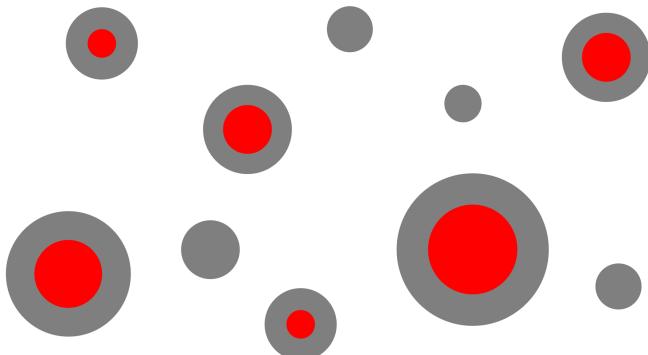
Halo Model for Cosmological HI

HI-halo mass relation fitted to observations:

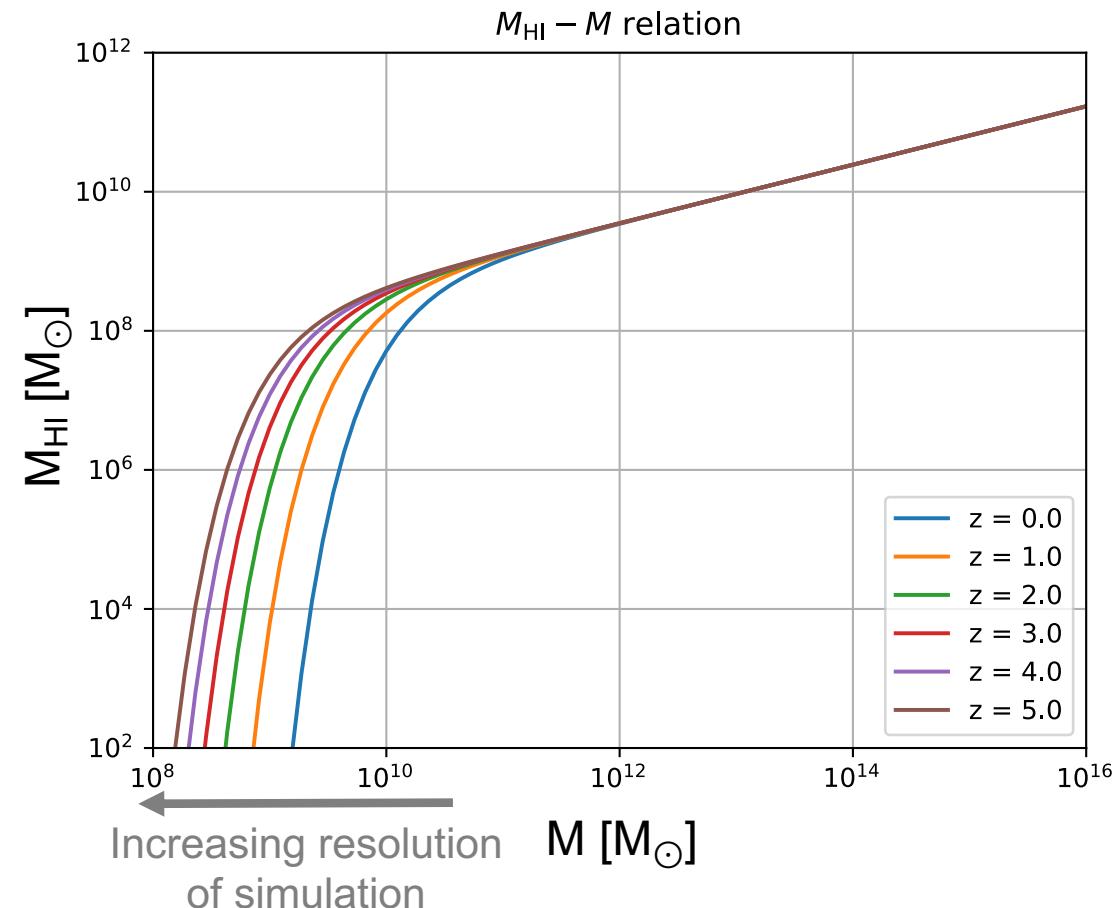
$$M_{\text{HI}}(M, z) = \alpha f_{\text{H,c}} M \left(\frac{M}{10^{11} h^{-1} M_{\odot}} \right)^{\beta} \exp \left[- \left(\frac{v_{c,0}}{v_c(M, z)} \right)^3 \right]$$

Padmanabhan et al. 2017

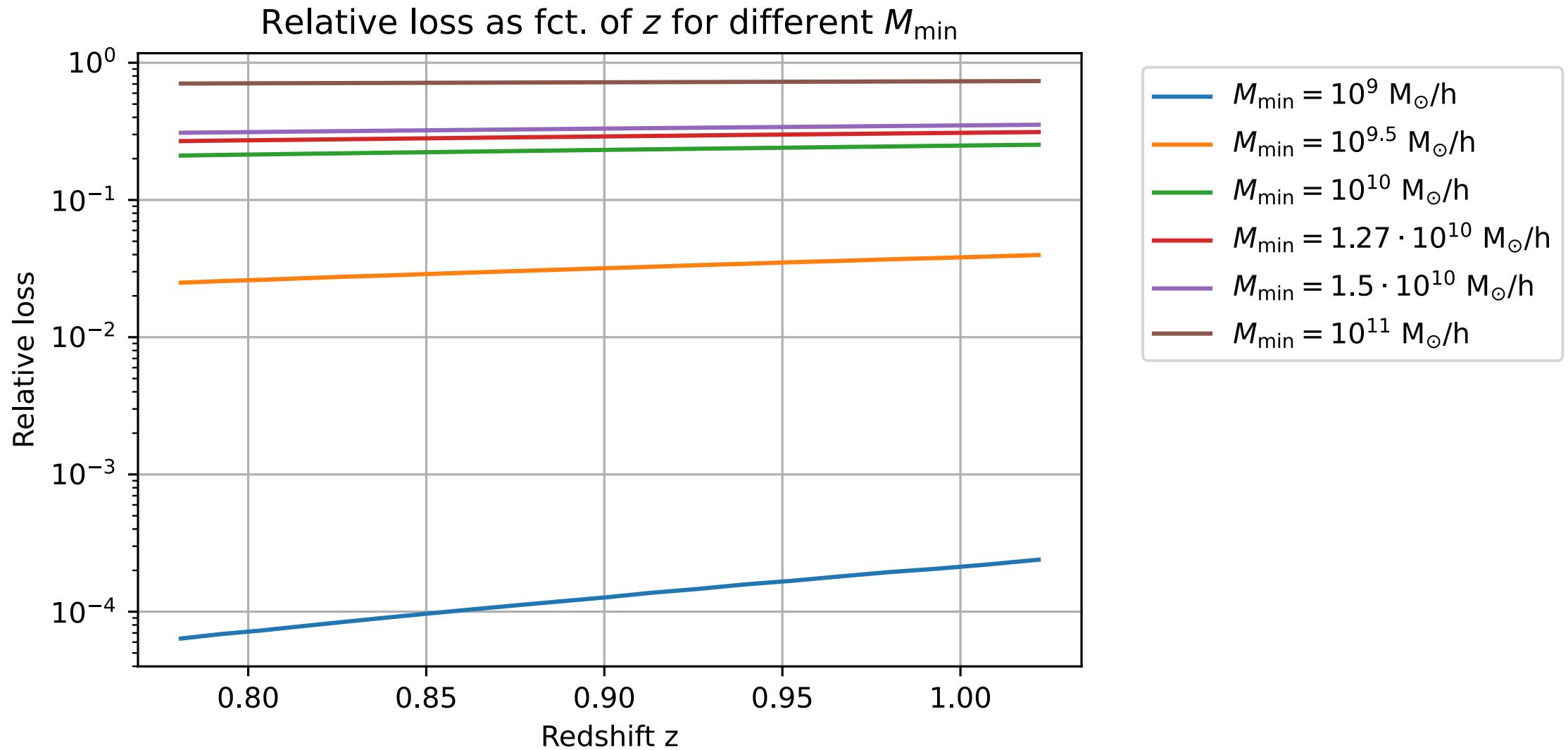
Dark Matter
Neutral Hydrogen



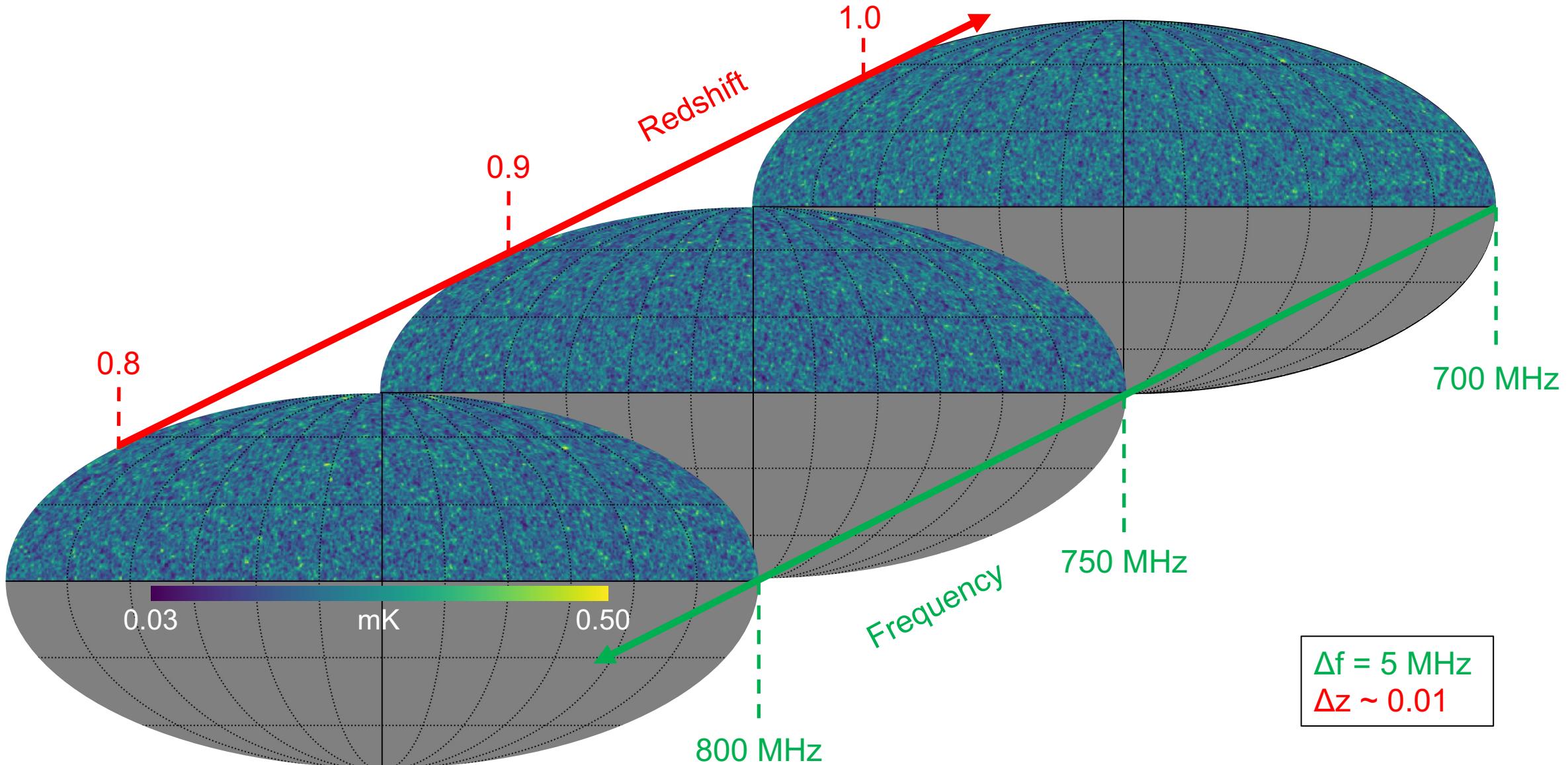
- More massive halos contain more HI
 - **But:** Many more small halos than large ones
- Important not to neglect small halos.



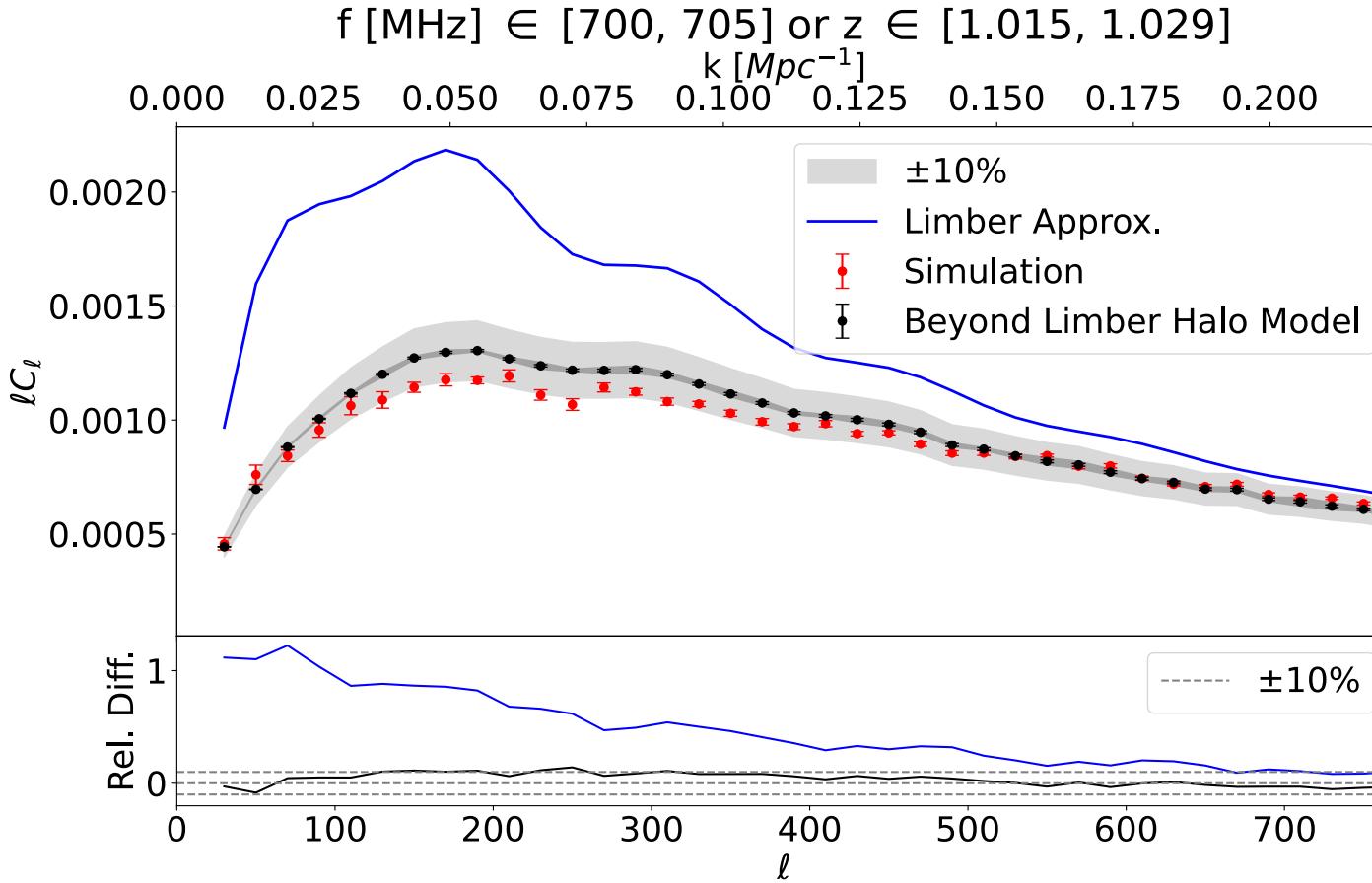
Relative Loss of Total HI Mass



Brightness Temperature Maps



HI Angular Power Spectrum



Simulation:

$$\delta_{HI} = (T_{HI} - \bar{T}_{HI})/\bar{T}_{HI}$$

$$\langle \delta_{HI,\ell m} \delta_{HI,\ell' m'}^* \rangle = \delta_{\ell\ell'}^D \delta_{mm'}^D C_{\ell,HI}$$

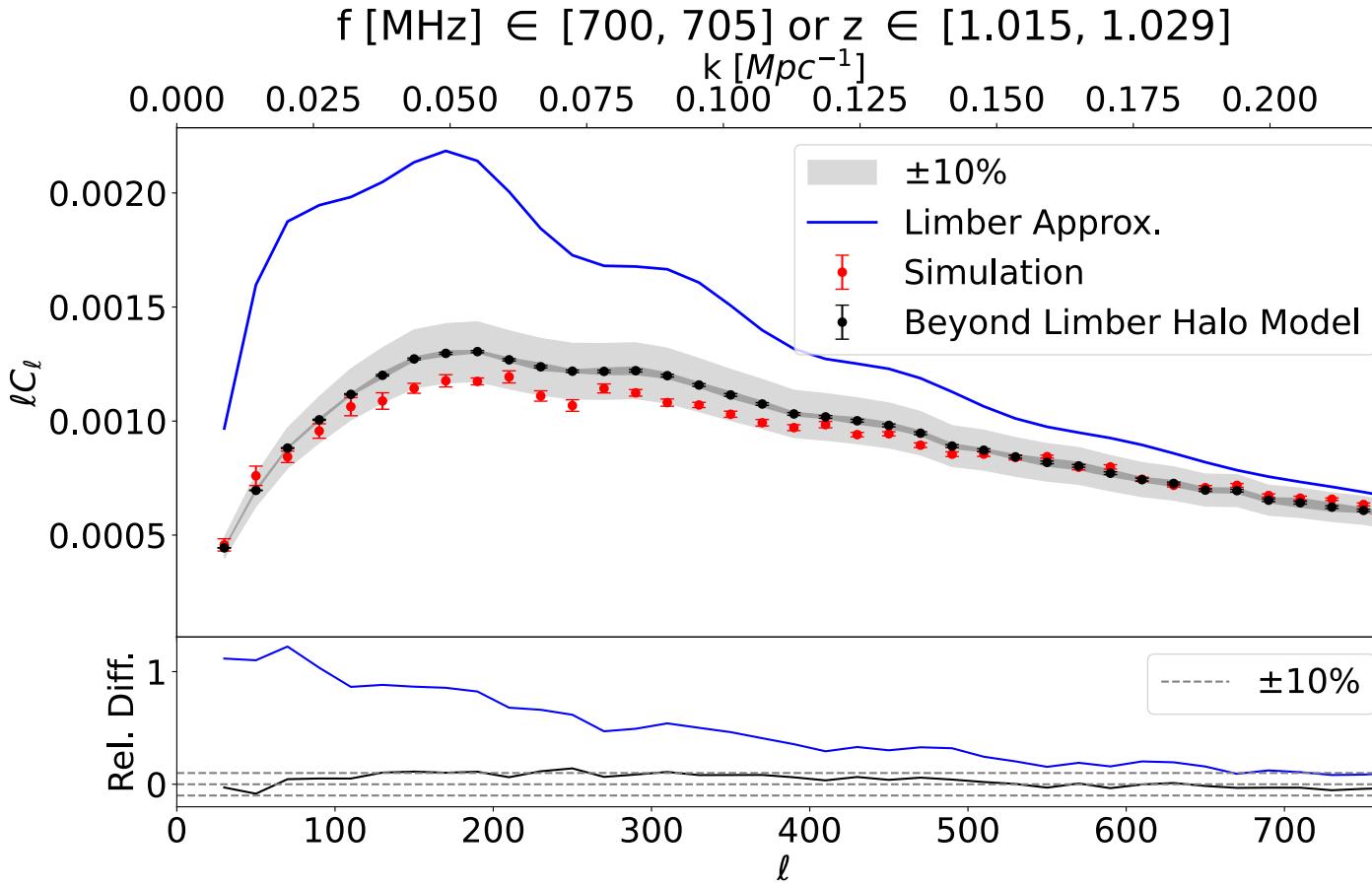
Limber Approximation:

$$C_{\ell,HI} \approx \int dz \frac{c}{H(z)} \frac{W^2(z)}{r(\chi(z))^2} P_{HI} \left(\frac{\ell + 1/2}{r(\chi(z))}, z \right)$$



Refregier et al. 2017

HI Angular Power Spectrum



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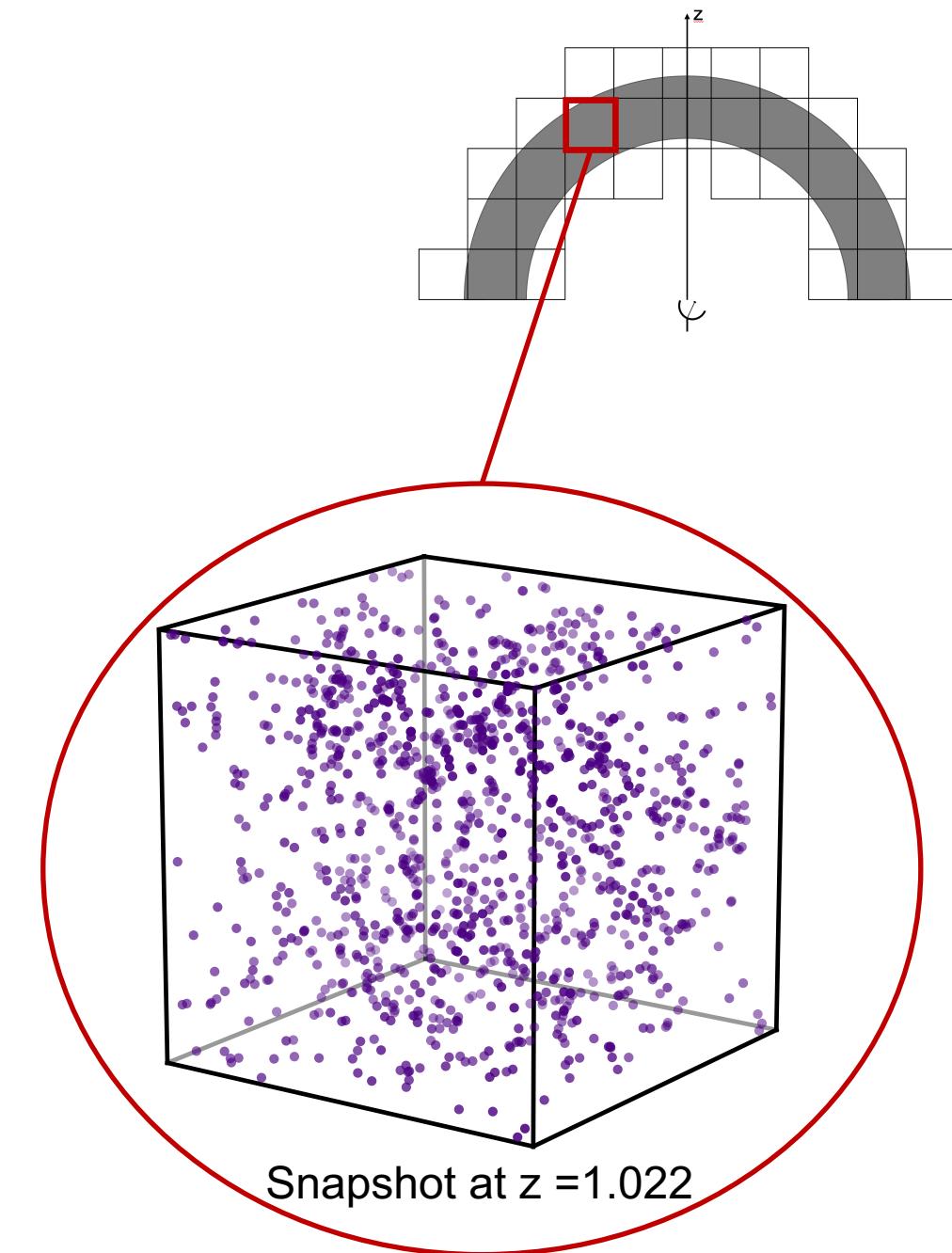
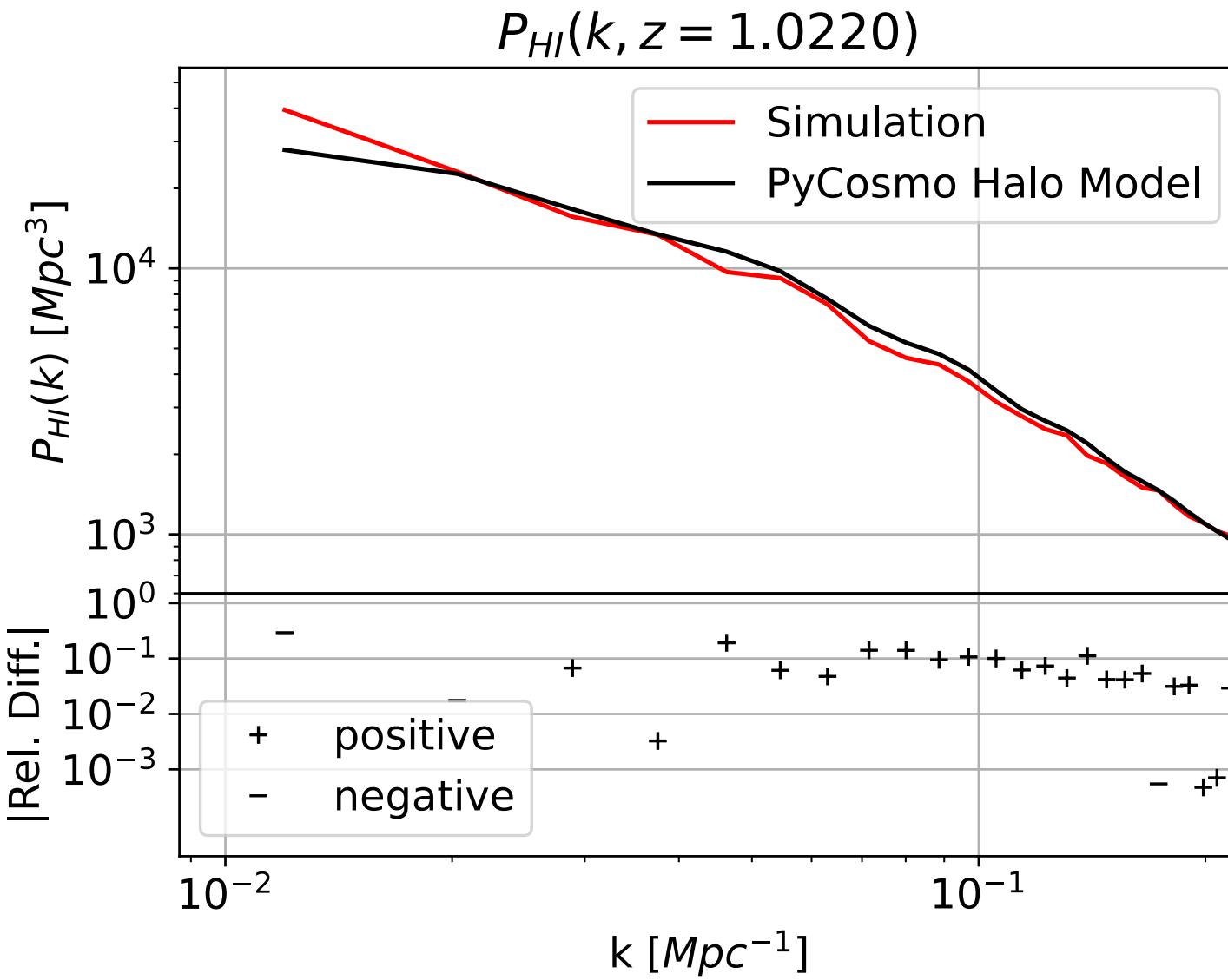
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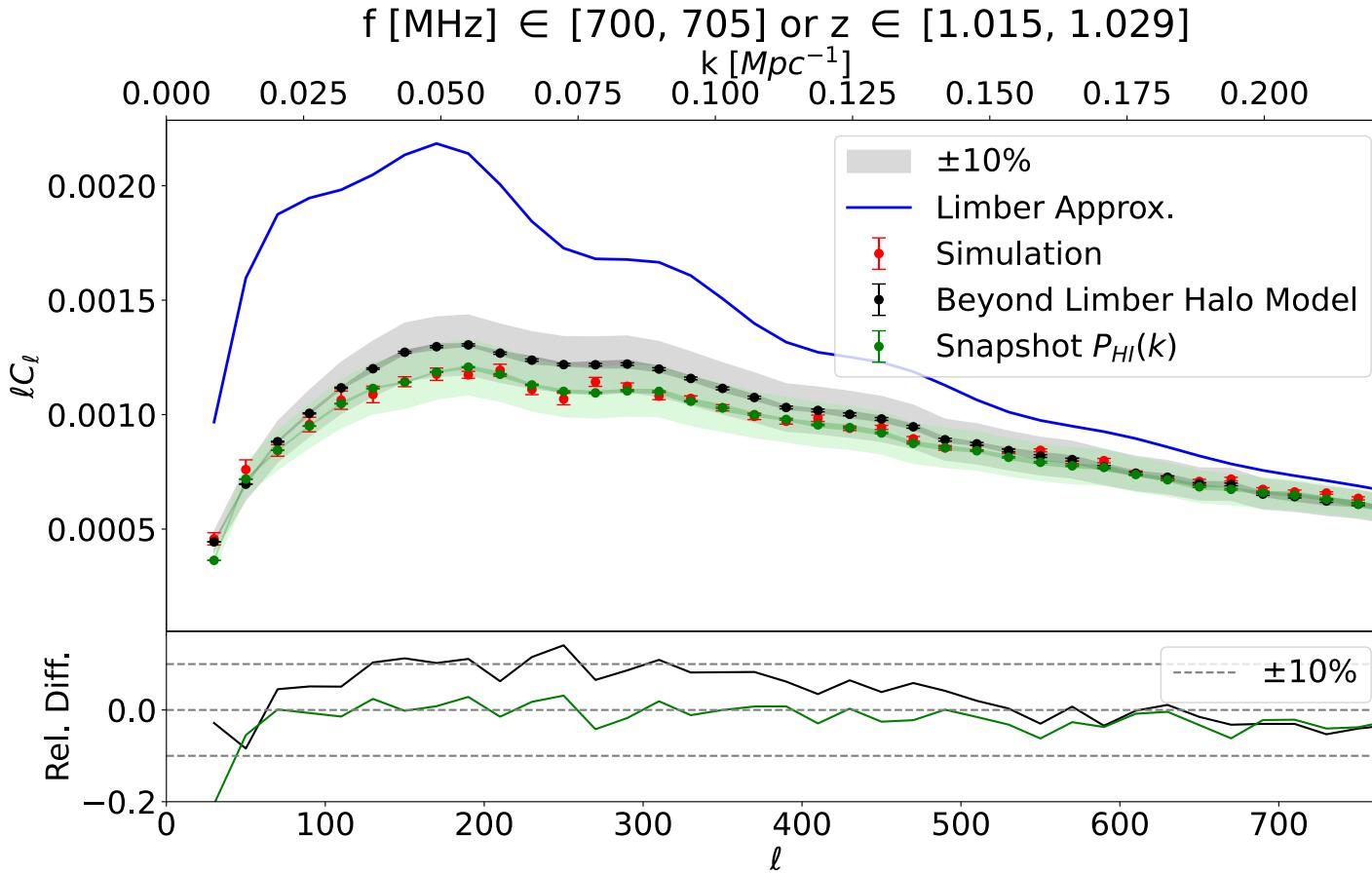
Full Expression:

$$C_{\ell,HI} = \frac{2}{\pi} \int k^2 dk \int_0^\infty d\chi W(\chi) j_\ell(k\chi) \sqrt{P_{HI}(k, z(\chi))} \\ \times \int_0^\infty d\chi' W(\chi') j_\ell(k\chi') \sqrt{P_{HI}(k, z(\chi'))}$$

HI Power Spectrum



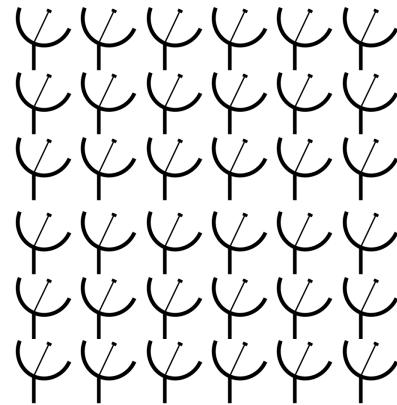
HI Angular Power Spectrum



Full Expression:

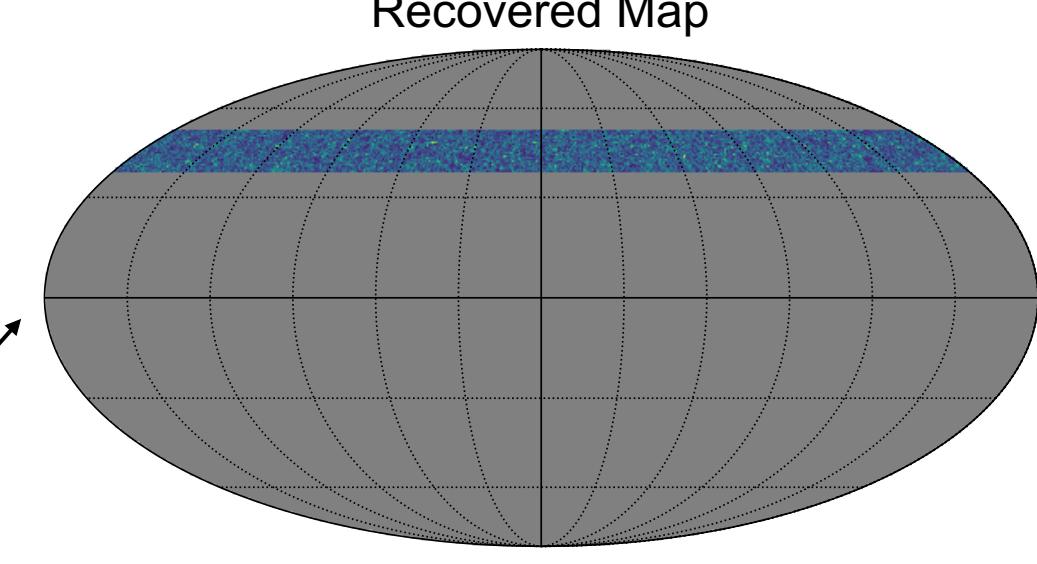
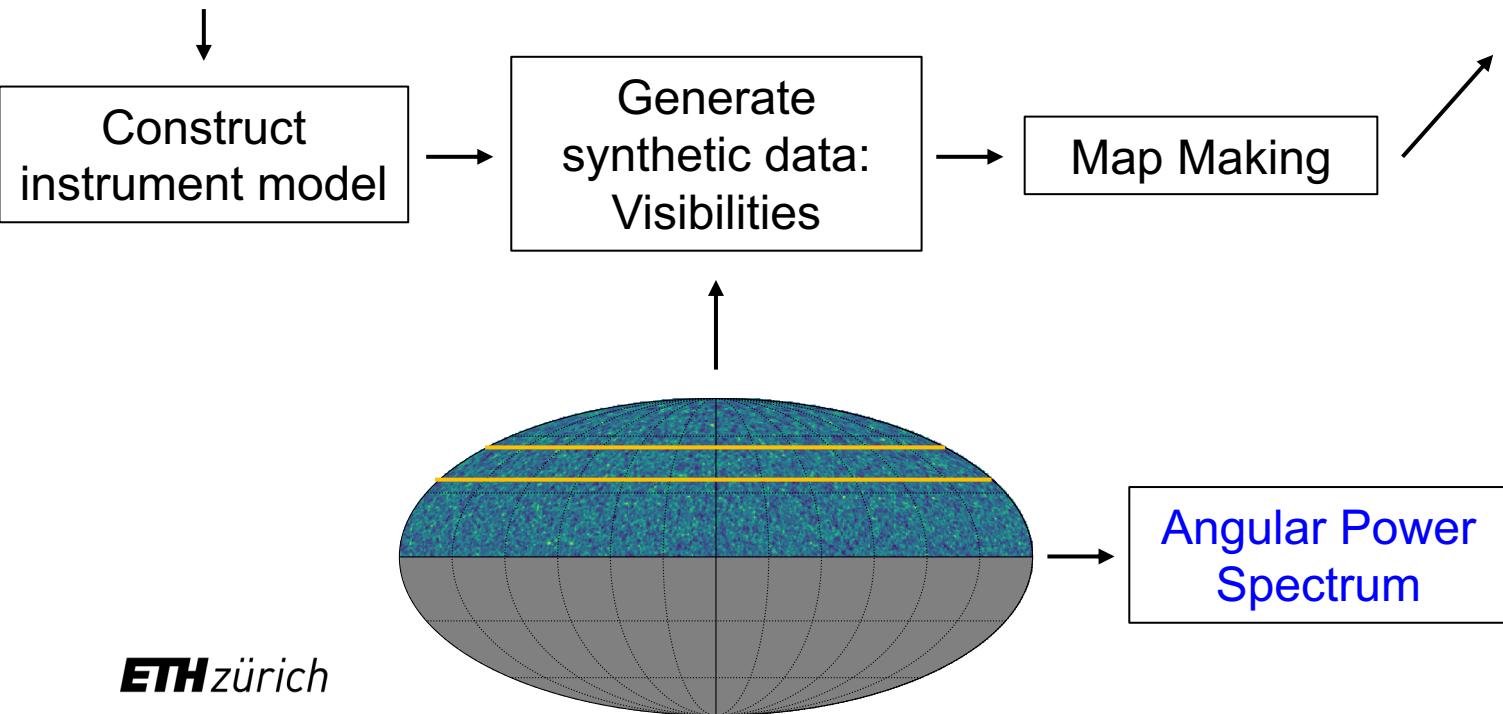
$$C_{\ell,HI} = \frac{2}{\pi} \int k^2 dk \int_0^\infty d\chi W(\chi) j_\ell(k\chi) \sqrt{P_{HI}(k, z(\chi))}$$
$$\times \int_0^\infty d\chi' W(\chi') j_\ell(k\chi') \sqrt{P_{HI}(k, z(\chi'))}$$

Instrument Simulation and Analysis Pipeline



Number of dishes: 36 (6 x 6 grid)
Operating mode: Drift-scan
Dish diameter: 6 m
Dish separation: 6 m
Primary Beam Type: Gaussian
Telescope Latitude: 45°

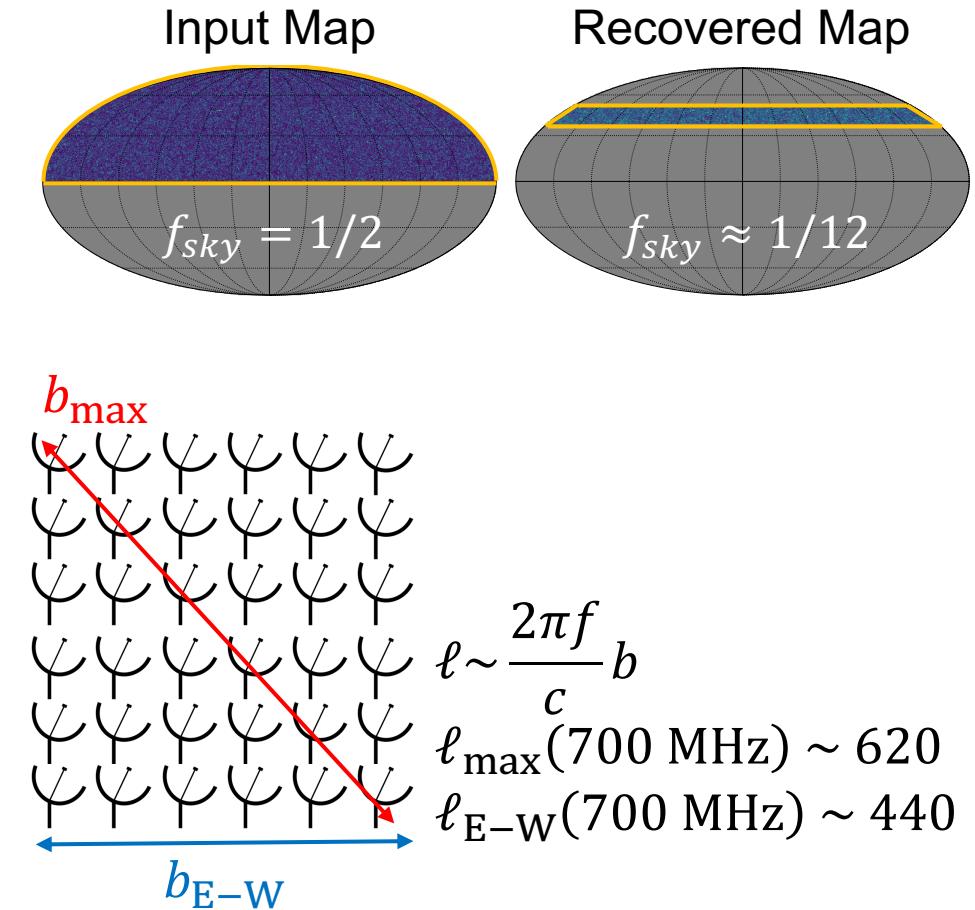
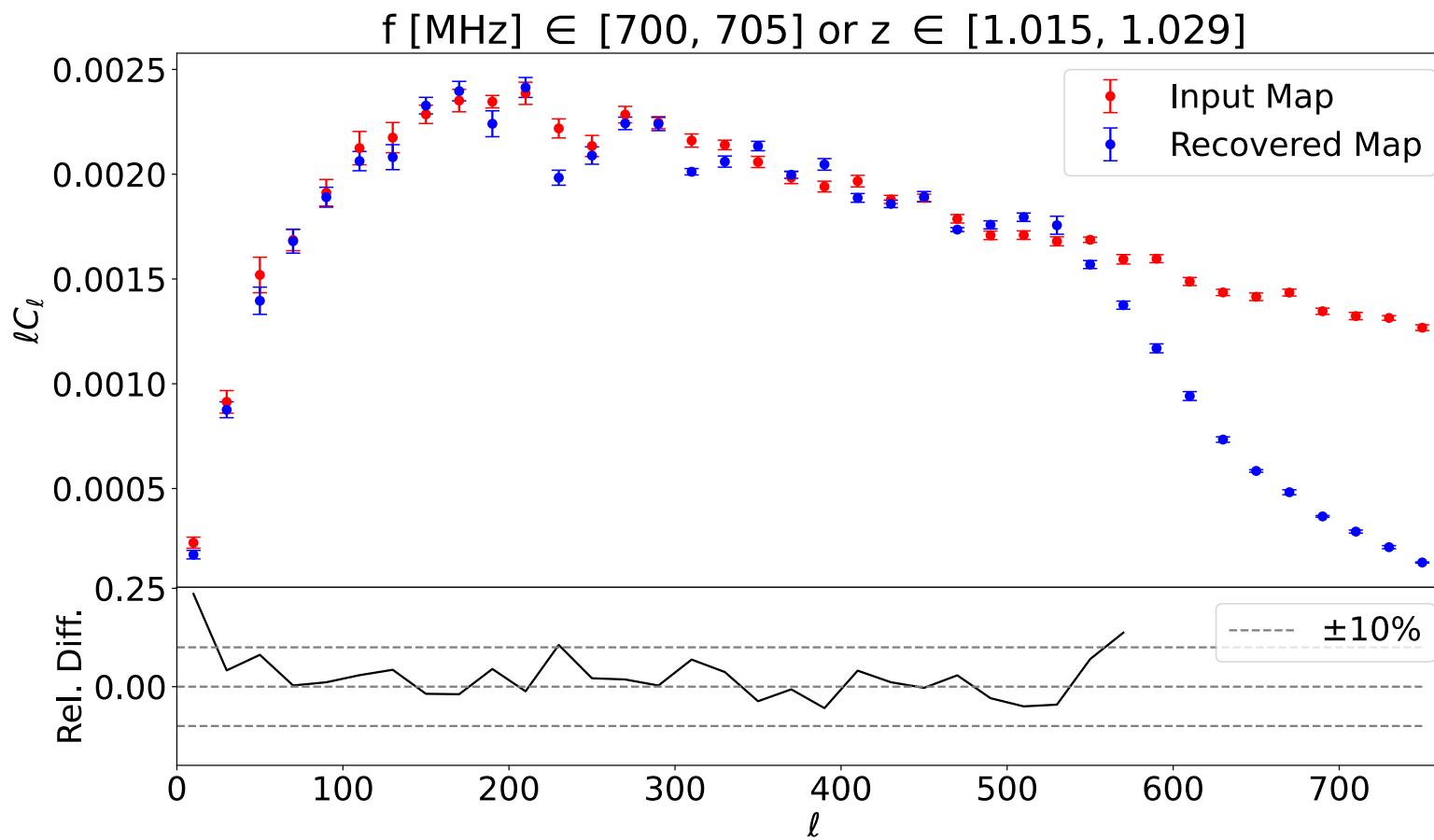
Simplified HIRAX array configuration



0 mK 0.5806

Angular Power Spectrum

Recovered HI Angular Power Spectrum



Summary

- Simulation pipeline of HI maps for intensity mapping
- Apply it to HIRAX and SKA/MeerKAT
- Theoretical predictions of power spectrum
- Future developments:
 - Increase mass resolution
 - Vary cosmology and astrophysics (HI-Halo mass relation)
 - Consider foregrounds, noise and RSD
 - Cross-correlations with other probes

Hitz et al. (in prep.)

Backup Slides

PyCosmo HI Halo Model: Angular Power Spectrum

$$C_{\ell, \text{HI}} \approx \int dz \frac{c}{H(z)} \frac{W^2(z)}{r(\chi(z))^2} P_{\text{HI}}\left(\frac{\ell + 1/2}{r(\chi(z))}, z\right)$$

$$\rightarrow P_{\text{HI}}(k) = P_{1\text{h,HI}}(k) + P_{2\text{h,HI}}(k)$$

$$\rightarrow P_{1\text{h,HI}} = \frac{1}{\bar{\rho}_{\text{HI}}^2} \int dM \frac{dn(M, z)}{dM} M_{\text{HI}}^2(M) |u_{\text{HI}}(k|M)|^2$$

$$\rightarrow P_{2\text{h,HI}} = P_{\text{lin}}(k) \left[\frac{1}{\bar{\rho}_{\text{HI}}} \int dM \frac{dn(M, z)}{dM} M_{\text{HI}}(M) b(M) |u_{\text{HI}}(k|M)| \right]^2$$