# A novel observable expected in lensed FRBs

S. Goureesankar,<sup>1</sup> Prasenjit Saha,<sup>2</sup> Calvin Leung,<sup>3</sup> Olaf Wucknitz<sup>4</sup>

<sup>1</sup> IISER Thiruvananthapuram, <sup>2</sup> University of Zurich, <sup>3</sup> UC Berkeley, <sup>4</sup> MPIfR



 Q0957+561
 PG1115+080

 HE1104-1805
 RXJ1131-1231

 Figures from arxiv:2401.04165

RXJ0911+0551 Q2237+030



 Q0957+561
 PG1115+080

 HE1104-1805
 RXJ1131-1231

 Figures from arxiv:2401.04165

RXJ0911+0551 Q2237+030





## Micro-Lensing by Stars within (macro-)Lensing by Galaxies



$$\sum_{\nu} S(\nu) \exp(2\pi\nu i t) \xrightarrow{\text{lensing}} \sum_{\nu} A(\nu) S(\nu) \exp(2\pi\nu i t)$$
$$A(\nu) = \sum_{k} \exp(2\pi\nu i \tau_{k}) |H(\tau_{k})|^{-1/2} \times \begin{cases} 1 \text{ for minima} \\ i \text{ for saddle points} \\ -1 \text{ for maxima} \end{cases}$$

 $\tau_k$  is the time delay of the *k*-th micro-image  $H(\tau_k)$  is the Hessian (curvature) of the  $\tau$  surface.

$$\sum_{\nu} S(\nu) \exp(2\pi\nu i t) \xrightarrow{\text{lensing}} \sum_{\nu} A(\nu) S(\nu) \exp(2\pi\nu i t)$$
$$A(\nu) = \sum_{k} \exp(2\pi\nu i \tau_{k}) |H(\tau_{k})|^{-1/2} \times \begin{cases} 1 \text{ for minima} \\ i \text{ for saddle points} \\ -1 \text{ for maxima} \end{cases}$$

 $\tau_k$  is the time delay of the *k*-th micro-image  $H(\tau_k)$  is the Hessian (curvature) of the  $\tau$  surface.

Microlensing is imprinted in auto-correlation of the lensed electric field.

### The observable



#### Complication: the Interstellar Medium

Electron density (turbulent spatial spectrum  $R^{-11/3}$ )



#### contributes to $\tau$ as $\nu^{-2}$

Follows Armstrong et al. 1995ApJ...443..209A

























7









#### Summary

The well-known:

- One in  $\sim 10^{-3}$  FRBs will be lensed by galaxies (clusters) to multiple images on the arcsec (arcmin) scales, with delays of weeks (years).
- Each image will be further microlensed collectively by stars into micro-images on micro-arcsecond scales, with delays on the microsecond scale.
- If they could be detected, potential applications range from stellar mass function to cosmological parameters.

#### Summary

The well-known:

- One in  $\sim 10^{-3}$  FRBs will be lensed by galaxies (clusters) to multiple images on the arcsec (arcmin) scales, with delays of weeks (years).
- Each image will be further microlensed collectively by stars into micro-images on micro-arcsecond scales, with delays on the microsecond scale.
- If they could be detected, potential applications range from stellar mass function to cosmological parameters.

The new:

- Micro-images of will produce a distinctive signature in the auto-correlation of the FRB signal.
- Plasma scattering by the ISM is the likely limitation.