



S&C Visibility Processing

Overview



- Visibility processing constructs images from output of correlator
- Very compute intensive
 - Scales as number of samples
- Memory and memory bandwidth intensive
 - Low computational intensity
 - Images can be large e.g. 12k x 12k x 12k
- Algorithms for SKA context still evolving

Measurement equations



- Unlimited field of view

$$V(u, v, w) = \int \frac{A(l, m) I(l, m)}{\sqrt{1 - l^2 - m^2}} e^{j2\pi(u l + v m + w \sqrt{1 - l^2 - m^2})} dl dm$$

- Small field of view

$$V(u, v) = \int I(l, m) e^{j2\pi(u l + v m)} dl dm$$

Approaches to visibility processing



1. Offline manual (most common)
2. Offline asynchronous pipeline
3. LOFAR model
 - quasi-synchronous centralised calibration, distributed imaging and science analysis
4. ASKAP
 - quasi-synchronous centralised calibration, imaging and science analysis
5. MeerKAT
 - quasi-synchronous centralised calibration and imaging science

Steps in processing



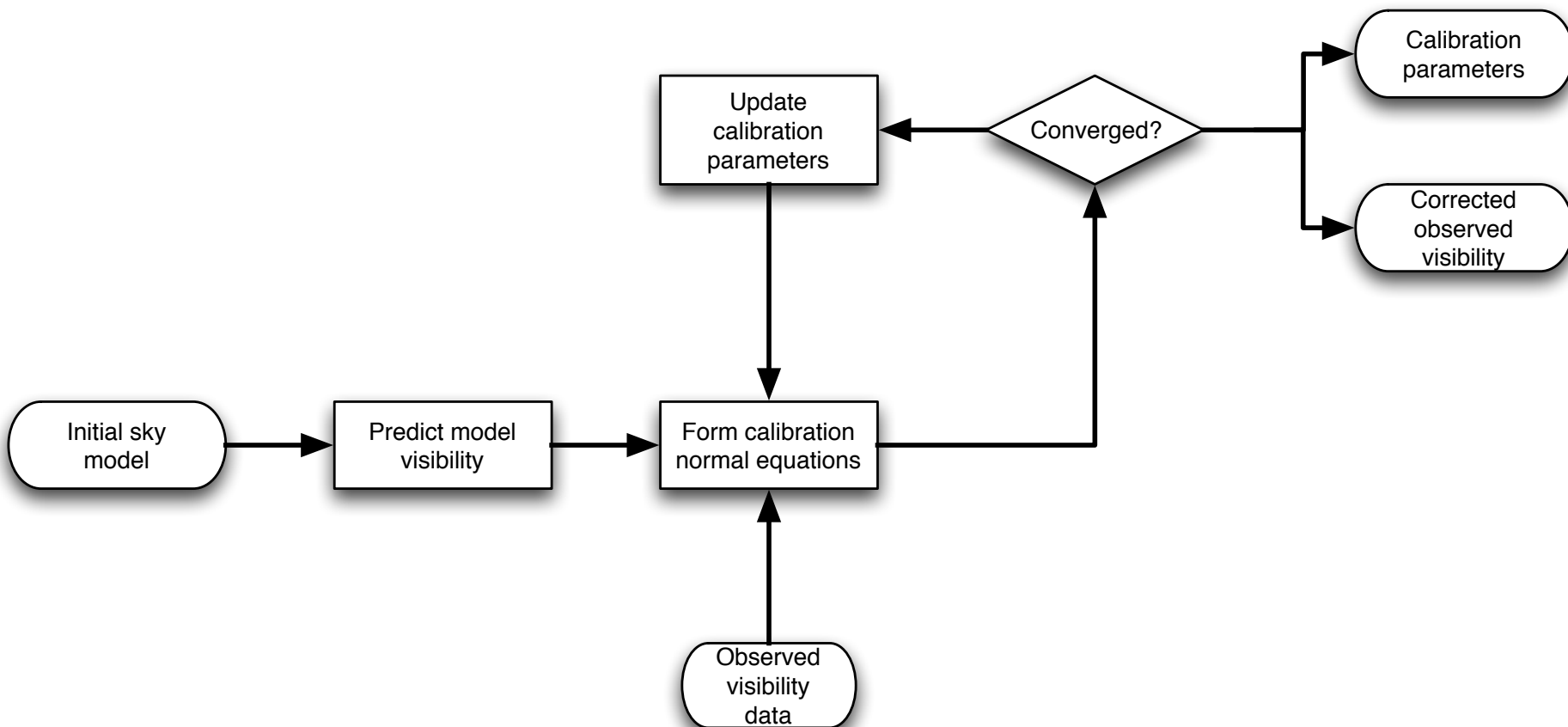
- Ingest from correlator
- Flag known bad data (e.g. RFI)
- Flag unknown bad data (e.g. new RFI)
- Calibrate
- Flag unknown bad data (e.g. weak RFI)
- Image
- Science processing e.g. find and fit sources

Calibration



- Observe known signal
 - e.g. bright point source
 - e.g. complex field (Local Sky Model)
- Fit calibration parameters
- Correct visibilities for calibration parameters
- Can iterate - self-calibration

Iterative loop



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Direction-dependent effects

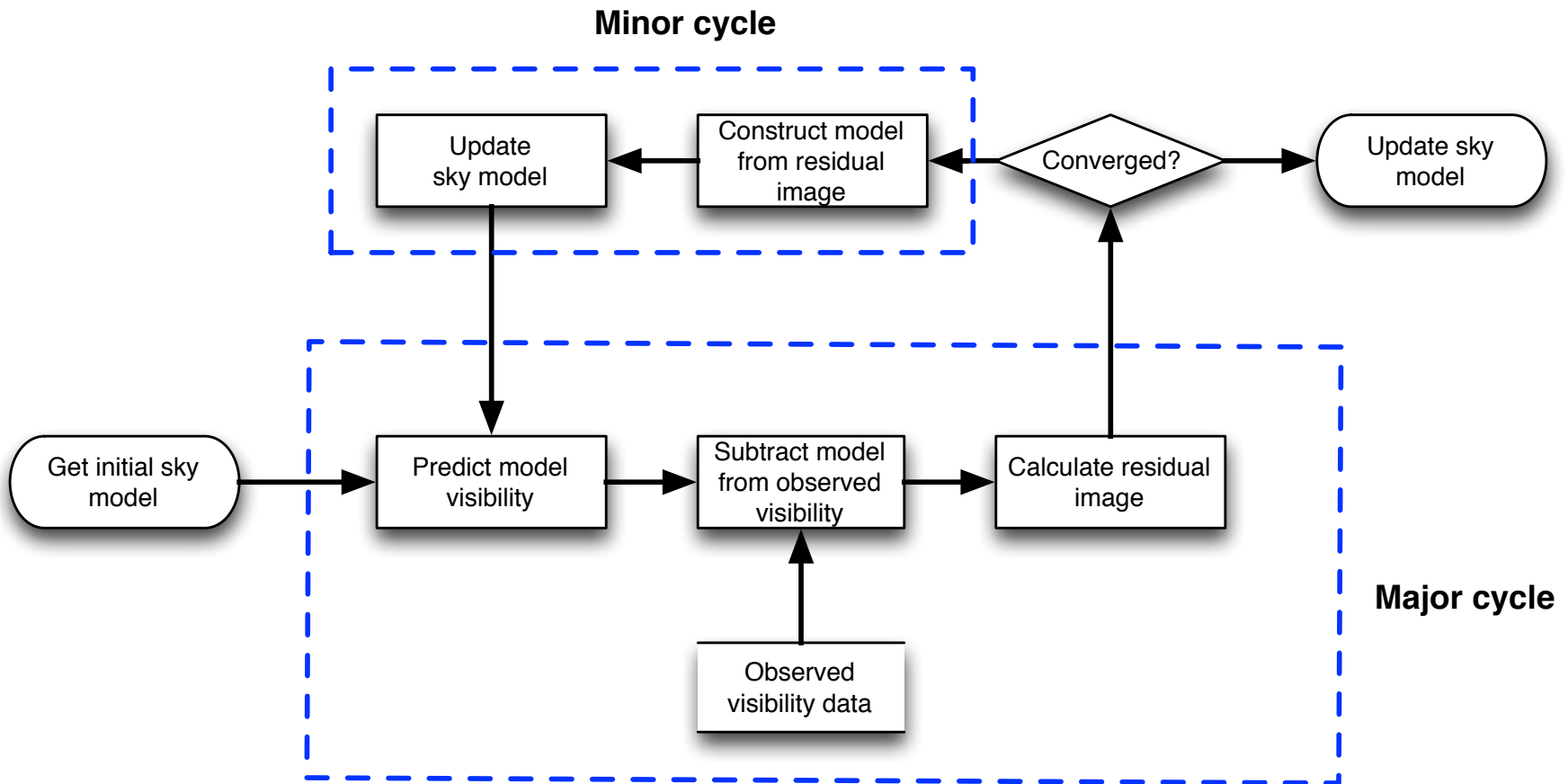


- Troublesome for wide field of view
- Examples
 - Ionosphere non-isoplanatic at low frequencies
 - Antenna primary beams
 - Antenna pointing
- Needed for high dynamic range imaging i.e. 70dB
- Difficult problem
 - Computationally expensive
 - Software and algorithms hard
 - Still under development
- LOFAR has pioneered this area
 - BBS (Black Board Selfcal)
 - MeqTrees

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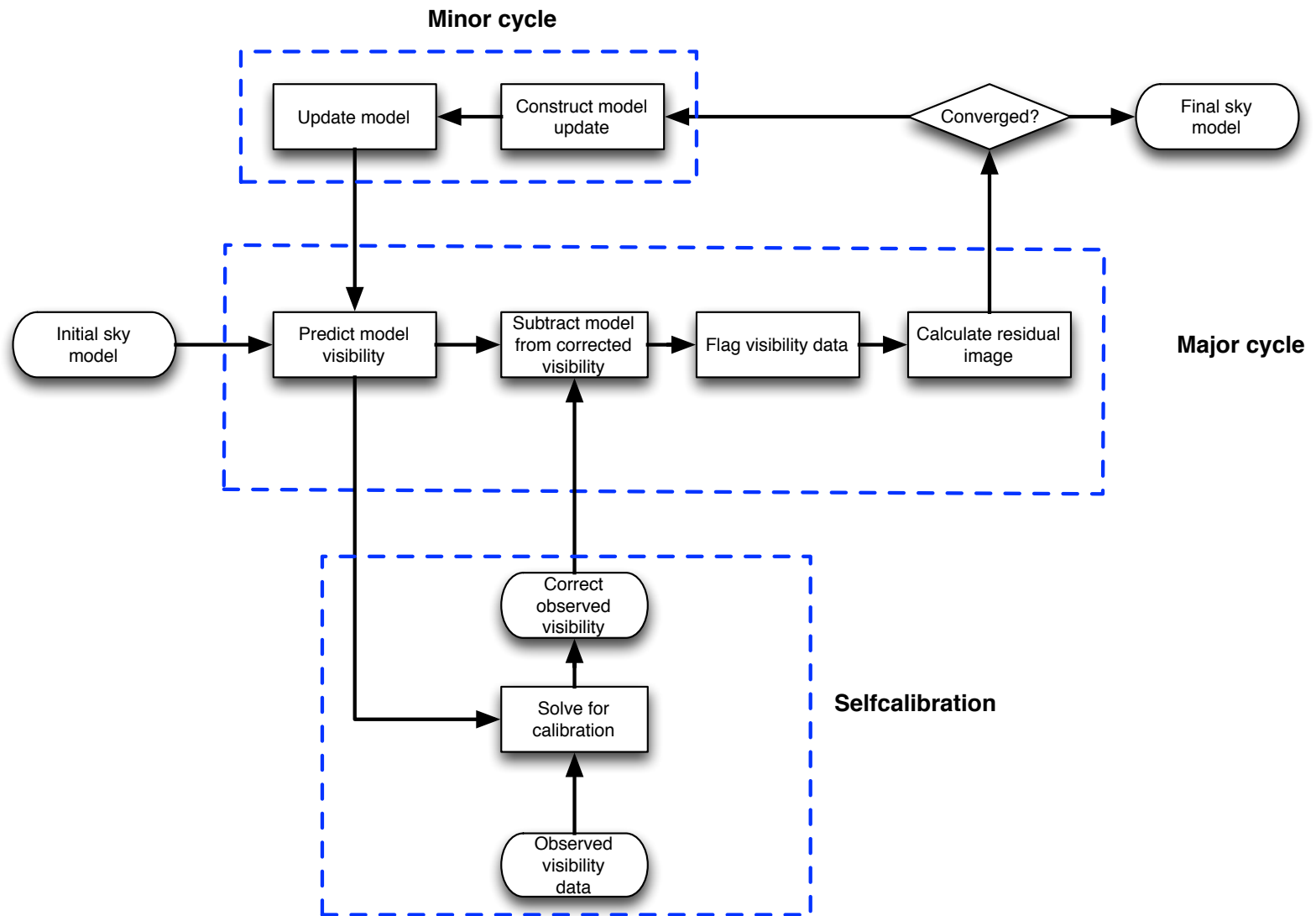
- Small fields of view: ME is invertible
 - Can derive sky brightness from inverse Fourier transform
 - Still need to deconvolve point spread function
- Large fields of view: ME is not invertible
 - Solve by iteration
 - Predict from model exactly
 - Calculate update to model approximately
 - Nearly always needed for SKA

Imaging loop



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Imaging and calibration loop



Wide field imaging

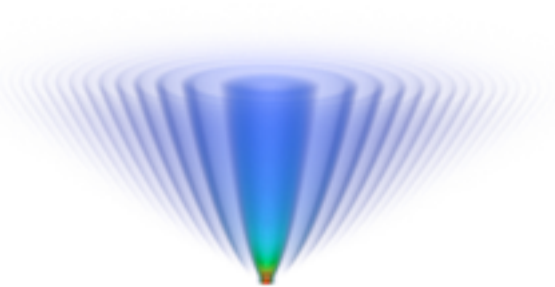


- Numerous algorithms
 - Full three dimensional transform
 - Divide image plane in small facets for which the two dimensional transform is accurate
 - Partition data into parallactic angle bins for which the array can be treated as coplanar
 - Convolution of the visibility samples by the Fresnel term prior to or after the Fourier transform.
- Each approach has merits
- No single approach optimal for all cases

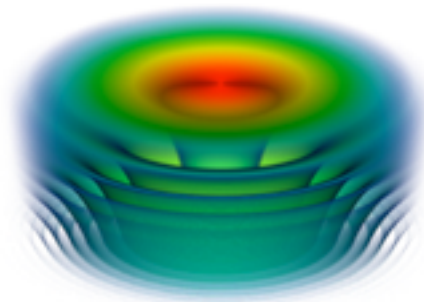
Wide field imaging



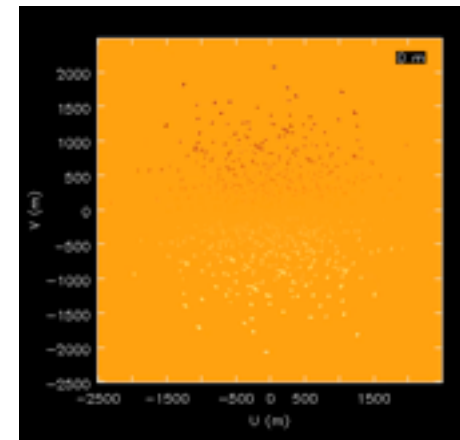
$$V(u, v, w) = \int \left[\frac{I(l, m) e^{j2\pi w(\sqrt{1-l^2-m^2}-1)}}{\sqrt{1-l^2-m^2}} \right] e^{j2\pi(u l + v m)} dl dm$$



Convolution in data space



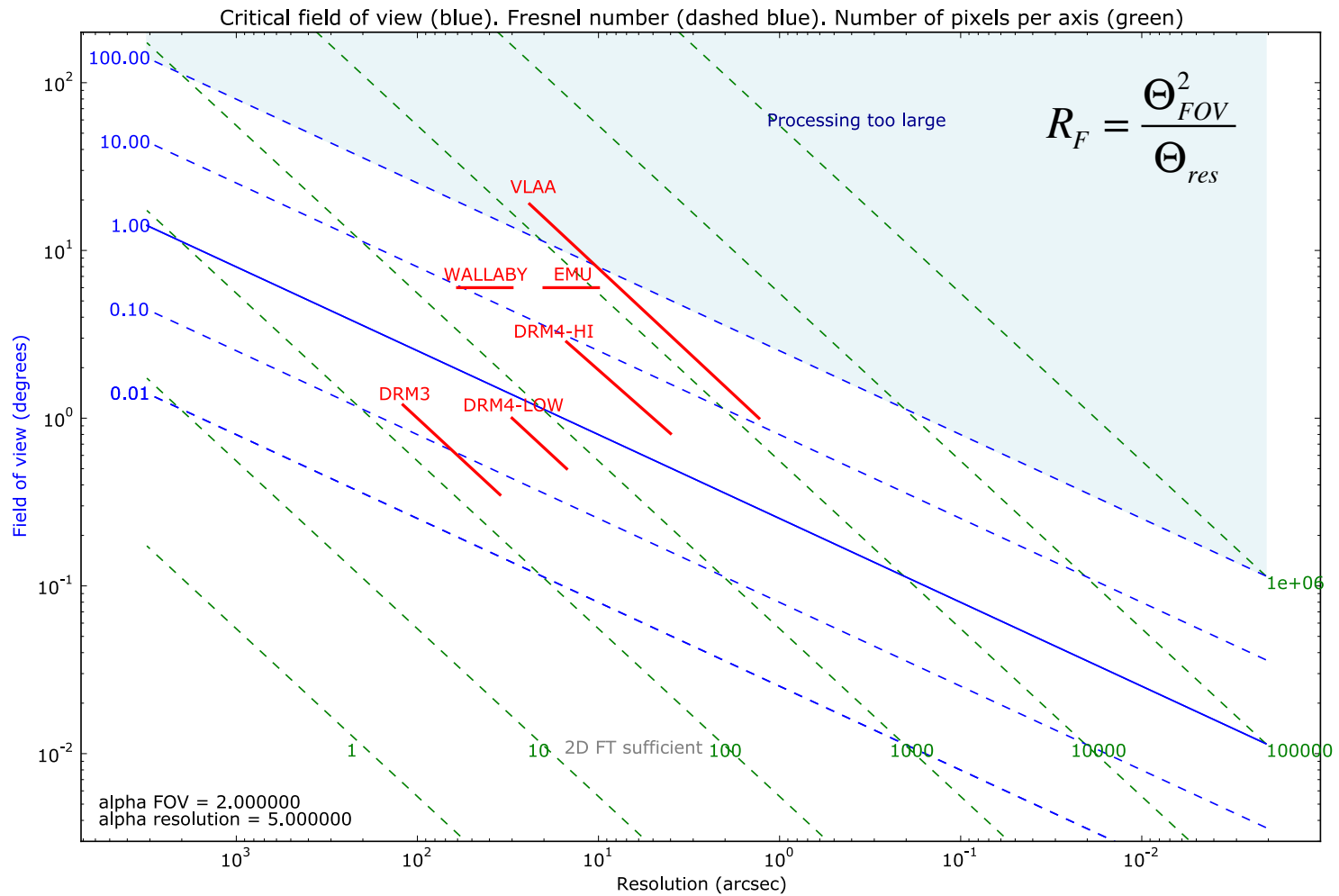
Multiplication in image space



Slices in data space

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How wide is wide?

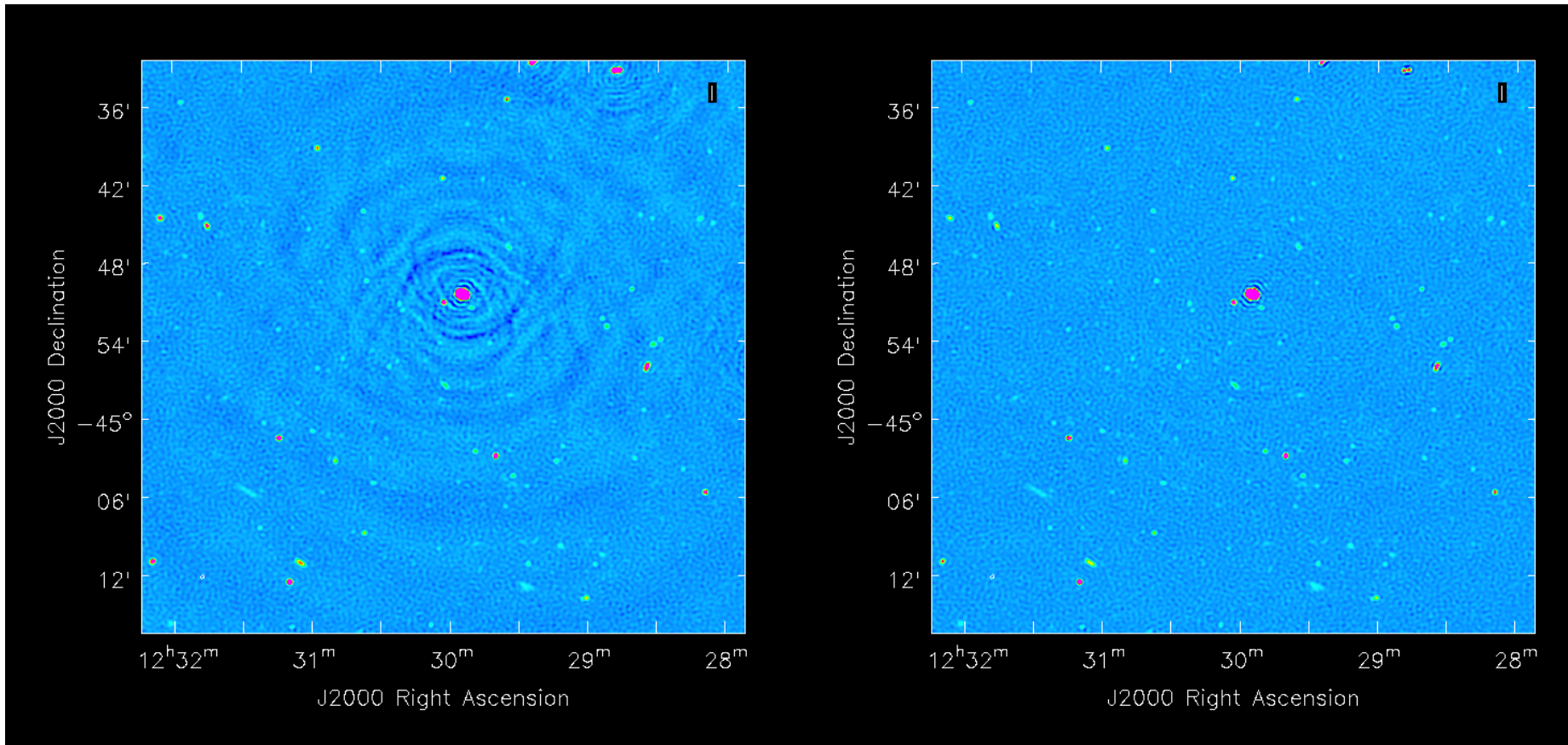


Wide band imaging



- Sources change brightness with frequency
- Must correct for high dynamic range imaging
- Best algorithm is Multi-Scale Multi-Frequency Clean
 - Memory intensive
- Compressive sampling also possible
- Likely area of more research

Example of MSMFClean



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Implementation



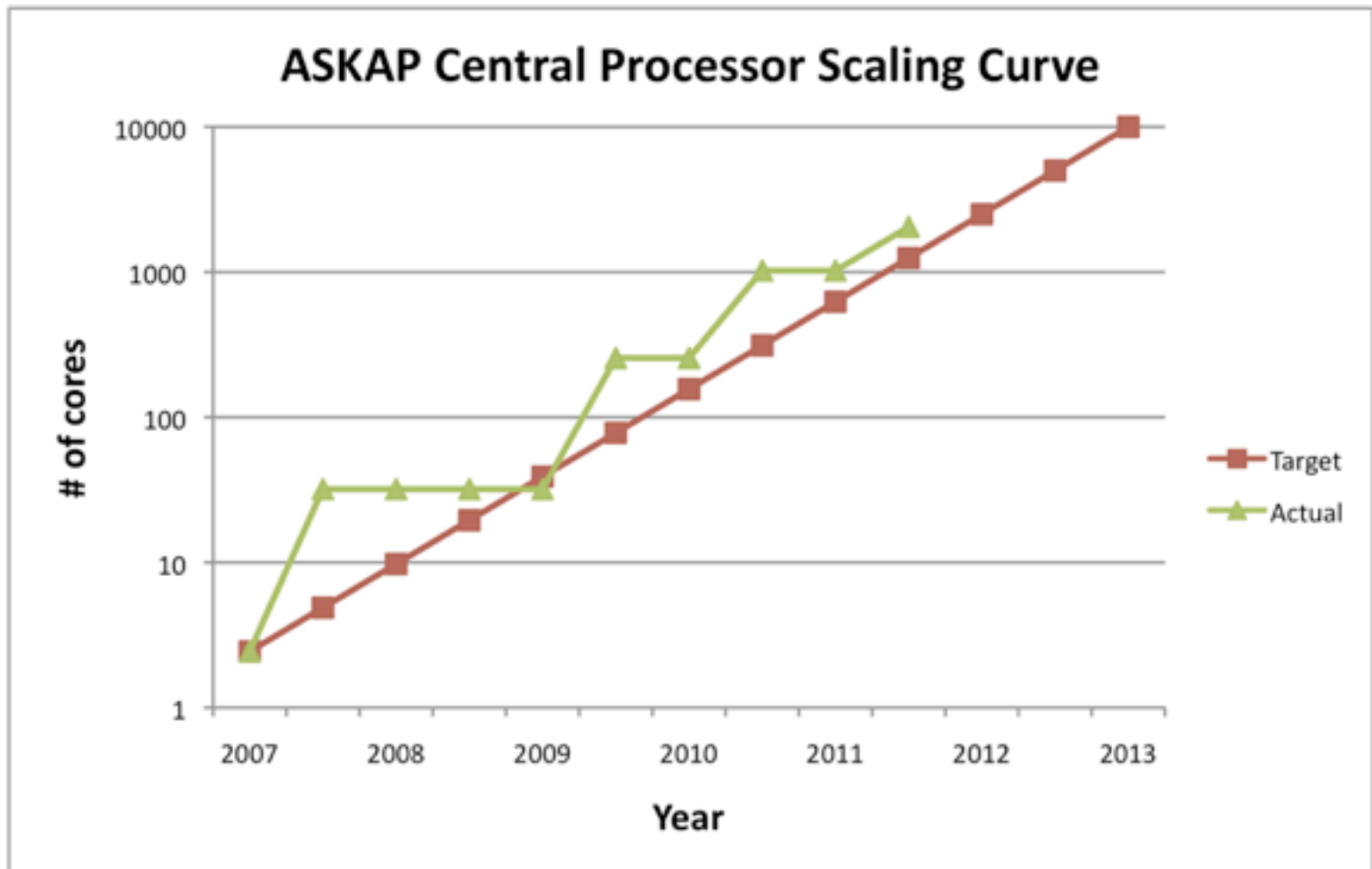
- ASKAP/LOFAR
 - C++ with 1 MPI process per core
 - Memory per core ~ 2 - 4 GB is insufficient
 - Shift soon to 1 MPI process per node
 - Eventually 100's or 1000's cores per node
- Software platforms
 - 3rd party libraries (e.g. casacore) are OO and not thread safe
 - C++ not optimum for HPC
 - I/O model must be revised for MPI Parallel IO or e.g. Lustre
- Biggest area of change

Changes in imaging during scaling work



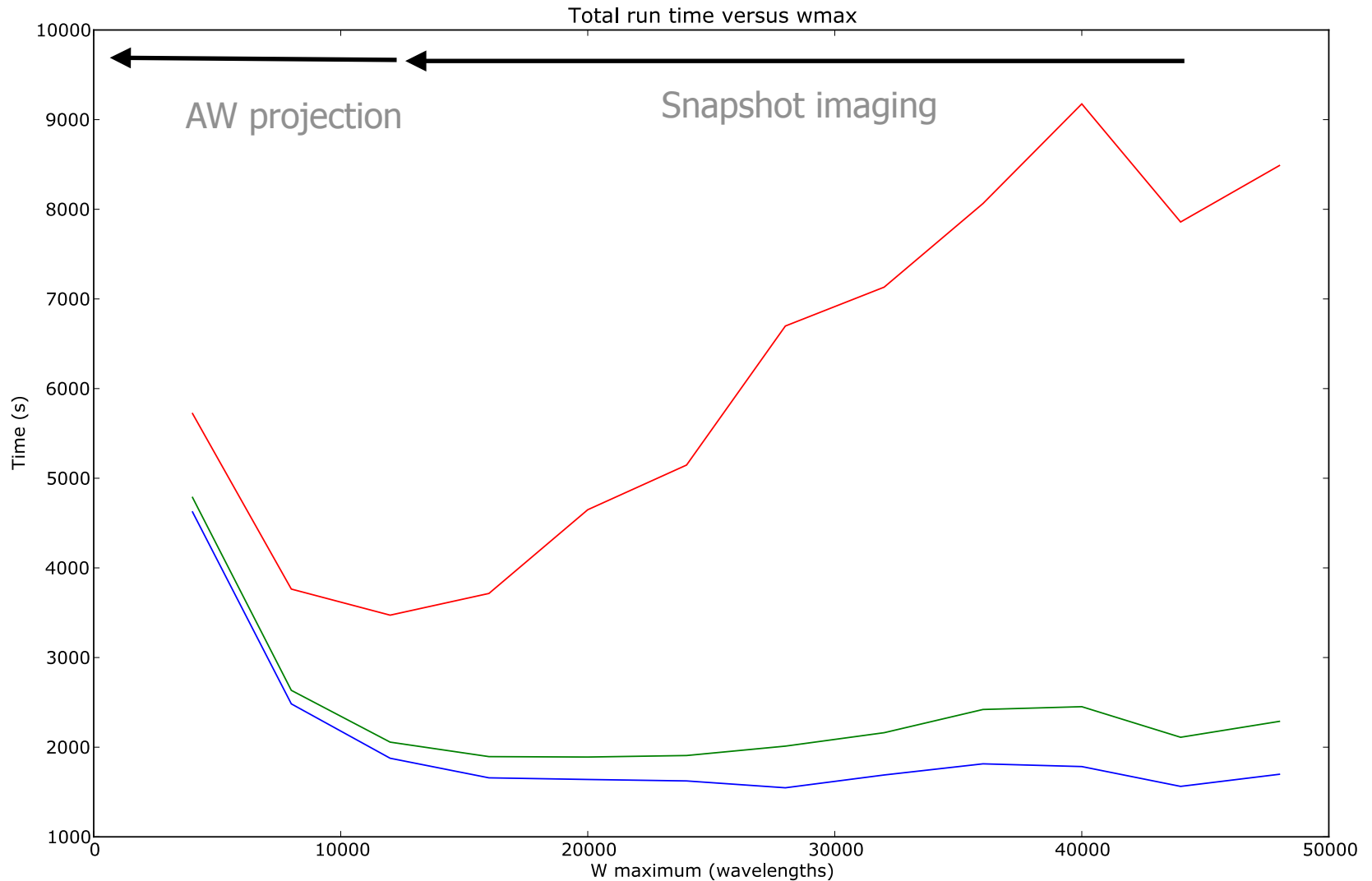
- **AWProject (2007)**
 - W projection + A projection (for primary beam)
 - Too much CPU
 - Too much memory for convolution function
- **AProjectWStack (2008)**
 - Apply W term in image space
 - Much less CPU
 - Too much memory for w stack
- **AWProject + trimmed convolution function (2009)**
 - Only apply and keep non-zero part of convolution function
 - Still too much memory for convolution function
- **AWProject + trimmed convolution function + multiple snapshot planes (2011)**
 - Fit and remove $w=au+bv$ plane every 30 - 60 min
 - Small memory for convolution function
- **Serialise normal equations piece-by-piece for MPI (2011)**
 - Cuts down short bump in memory use

Scaling over time

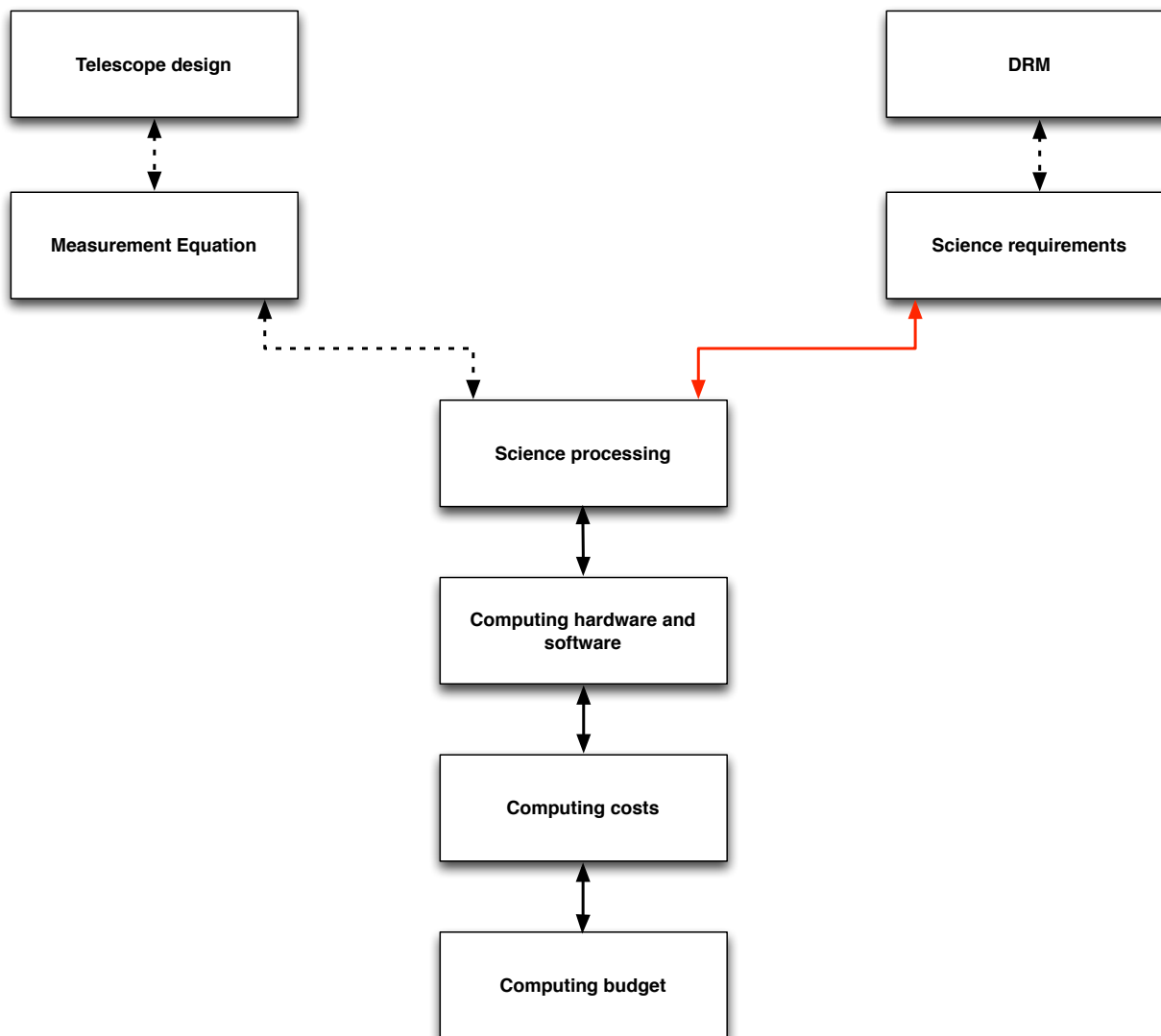


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Tuning of hybrid algorithms



Computing costs



gest radio telescope

Scaling of data rate



- Data rate very dependent on allowed smearing, antenna diameter, baseline length

| What | Symbol | Plausible range | Samples per second | Processing per sample |
|---|-------------------|------------------------|---------------------------|------------------------------|
| Amplitude loss due to time averaging | ΔA_{time} | 0.001 - 0.05 | $\Delta A_{time}^{-1/2}$ | - |
| Amplitude loss due to frequency averaging | ΔA_{freq} | 0.001 - 0.05 | $\Delta A_{freq}^{-1/2}$ | - |
| Antenna diameter | D | 30m - 80m | D^{-2} | D^{-4} |
| Maximum baseline length | B | 2 km - 100km | B^2 | B^2 |

Example scaling test



- Dish array (with SPF), 8 hour continuum integration.
- The number of channels and the integration time were each chosen to scale as baseline length and to fill Fourier space.
- 48 MPI processes were used in these runs.
- The last column shows the number of MPI processes required to finish a major cycle in one hour.
- Remember that up to 10 major cycles may be required, and another factor of three comes from the necessity to perform multi-frequency synthesis.

| Configuration | Data size GB | Major cycle min | Total memory GB | Processes required |
|----------------------|-------------------------------|----------------------------------|----------------------------------|---------------------------|
| 1km | 88 | 18 | 111 | 7 |
| 5km | 297 | 80 | 115 | 32 |
| 10km | 1100 | 3000 | 192 | 240 |

Computing budget



- Current estimates 10's to 100's PF
- Usually:
 - Fix science, determine computing cost
- In SKA
 - Fix computing budget, determine science
- How?
 - Consider other costs e.g. power, software development
 - No interest in having fastest machine
 - Spend e.g. \$20M - \$30M

Algorithm development



- Hire sufficient people for critical path development
 - CALIM shows a new generation of algorithm specialists becoming available
- Data challenges
- Maintain CALIM meetings
 - Focus more on SKA and HPC

Summary



- Scaling to Pflops
 - Algorithms will have to change
 - Software development required
- Scientific performance
 - Reaching very high dynamic range will require experience with telescope
- Coupling science to computational scale is very difficult
 - Unlikely to be able to be definitive