



Central image detection with VLBI

Zhang[†] Ming

Xinjiang Astronomical Observatory,
Chinese Academy of Sciences

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Strong lensing nomenclature

- **Structure formation at subgalactic scale**

- **Cusped halo**

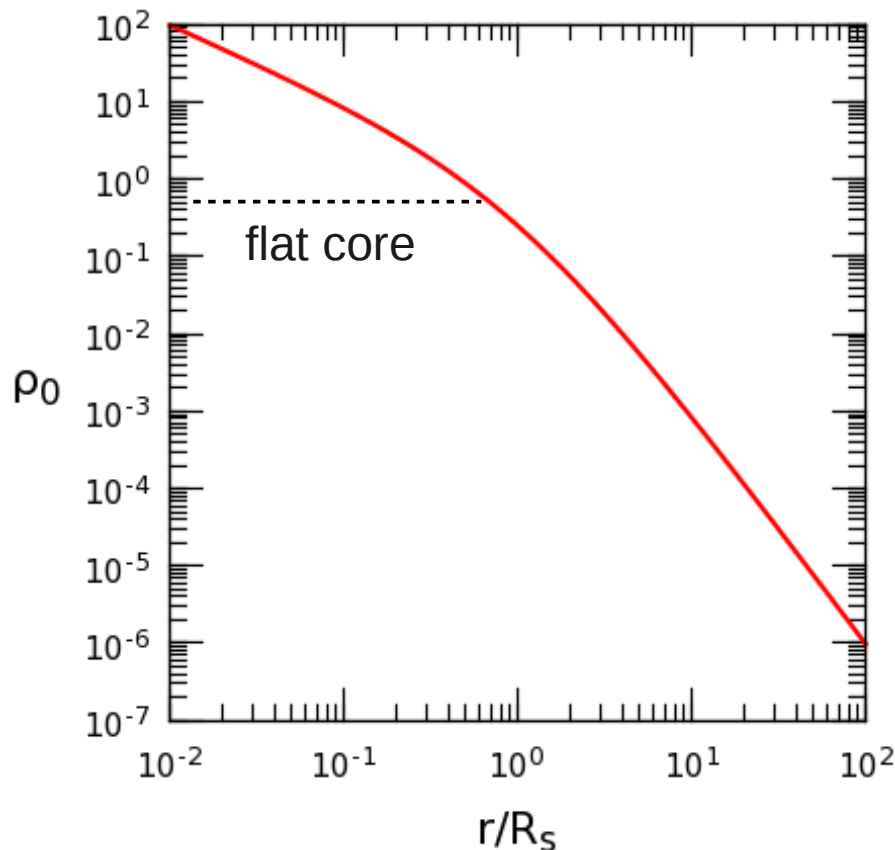
Central cusp => central image =(odd number theorem)=> the last missing odd image

- **Satellite galaxies**

Dwarf galaxies => subhalos => substructure

Λ CDM model stepping down

- From cluster to galaxy
 - NFW profile \Rightarrow double power-law profile



$$\rho(r) = \frac{\rho_0}{\frac{r}{R_s} \left(1 + \frac{r}{R_s}\right)}$$



$$\rho(r) = \frac{\rho_0}{(r/r_b)^\beta [1 + (r/r_b)^2]^{(\eta-\beta)/2}}$$

Lensing configuration

- Projected planes

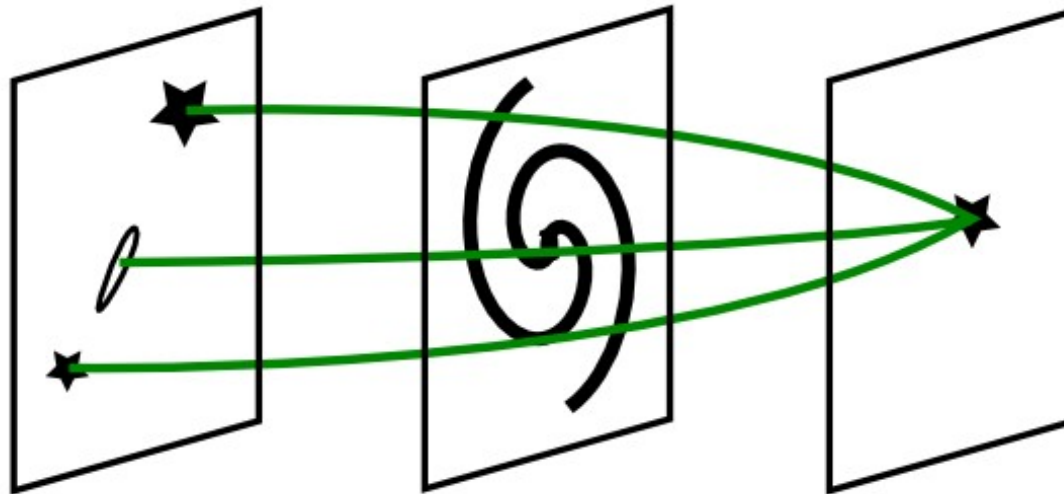


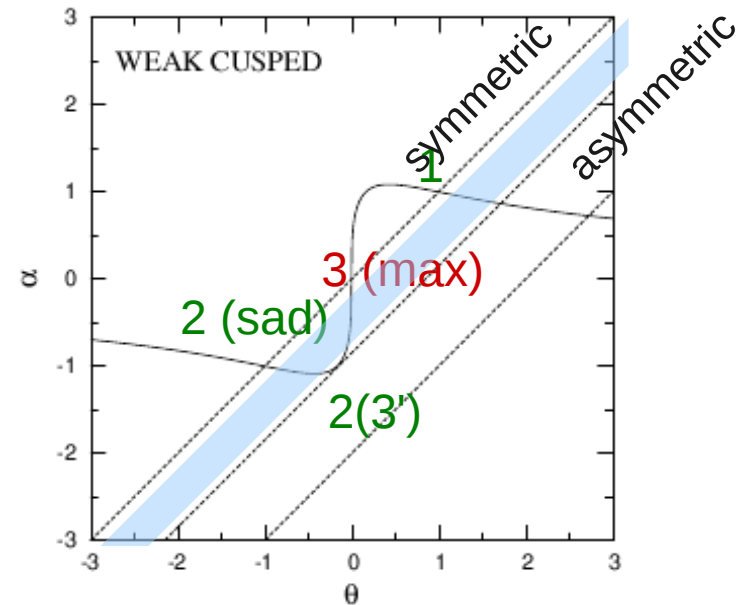
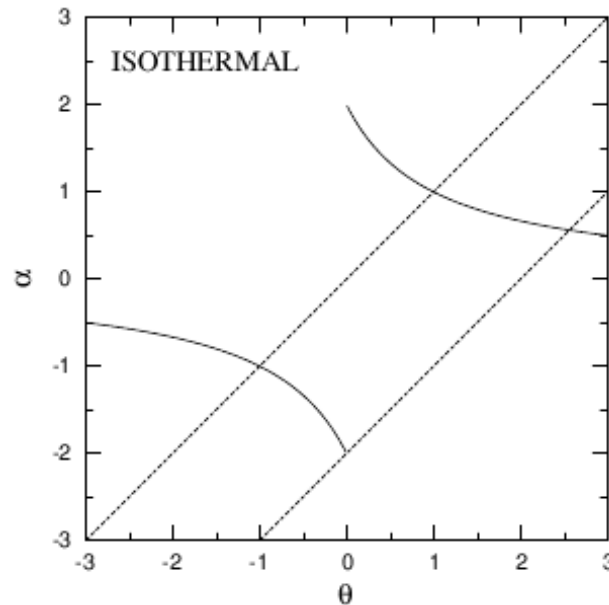
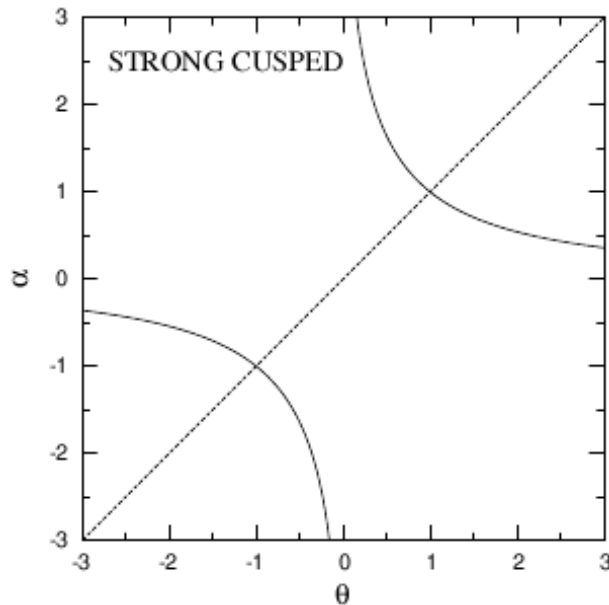
Image plane Lens plane Source plane
 (f, θ_i) (M, θ_d, z_d) (S, β, z_s)

Lens equation

$$\beta = \theta - \alpha$$

Central image generating

- **Lens equation rewrite \Rightarrow graph solutions**
 - Weak cusped profile



Approaching to sensitivity I

- **The hard ways**

Noise response $\Delta S_{ij} = \frac{1}{\eta_s} \sqrt{\frac{SEFD_i \cdot SEFD_j}{2\Delta\nu\tau_{acc}}}$

Antennas – bigger size

Baselines – more big dishes

Receivers – lower noise

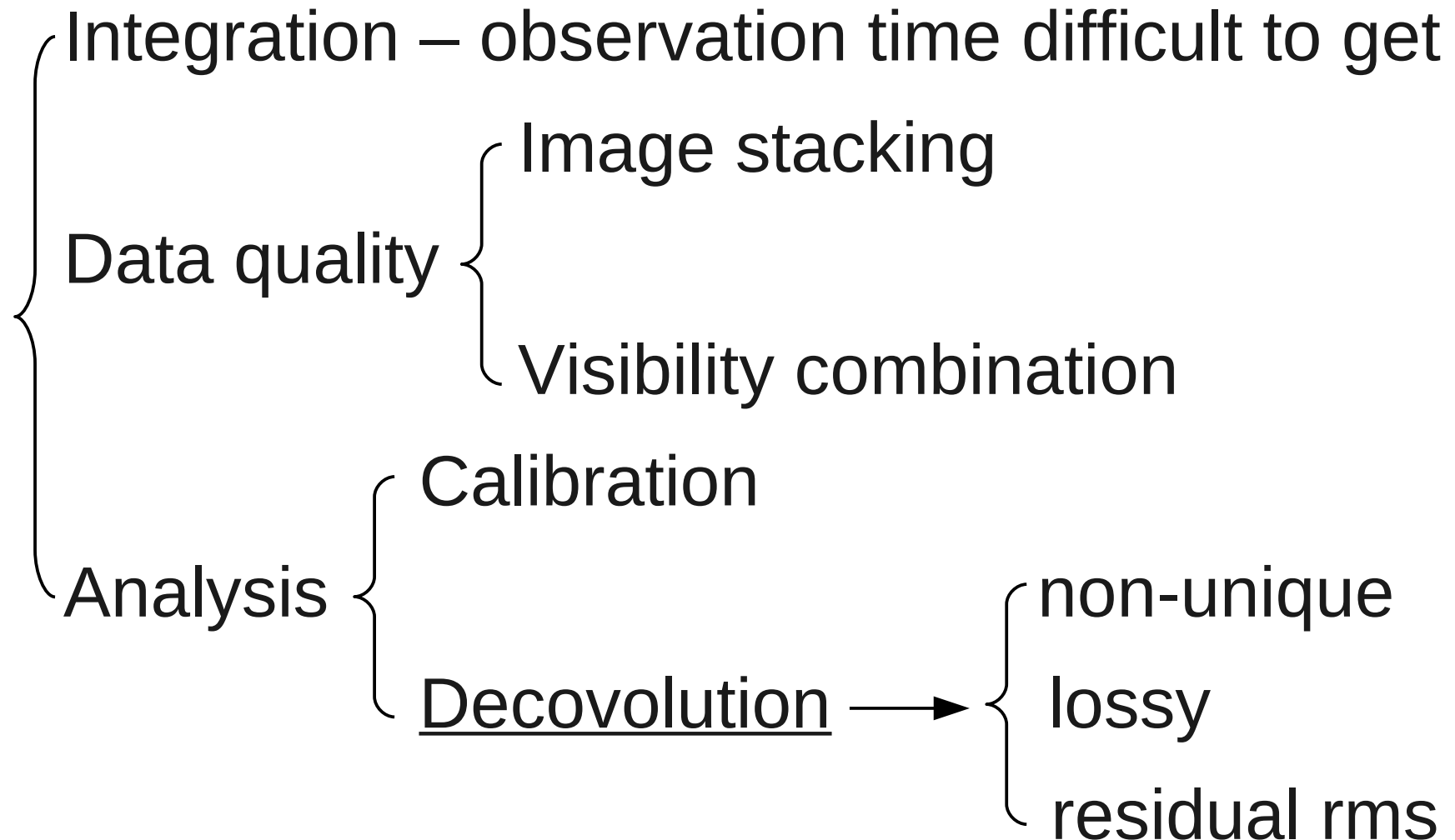
Bandwidth – wider band

Recording – more data rate

Correlating – less signal loss

Approaching to sensitivity II

- **The soft ways**



Deconvolution

- Ill-posed inverse problem

$$I^D = I * B \longrightarrow I = I^D *^{-1} B$$

- Inverting methods

$$\left\{ \begin{array}{ll} \text{Iteration} - I_n = I_{n-1} + \lambda(I^D - I_{n-1} * B) & \text{CLEAN} \\ & (\text{contraction mapping}) \quad (\text{point-like}) \\ \text{Regularization} - P = \chi^2 + \lambda \langle I | H | I \rangle & \text{MEM/MLM} \\ & H \rightarrow 0, \lambda \rightarrow 0 \longrightarrow \text{LSM} \quad (\text{extended}) \\ \text{Translation} - V = \mathcal{F}\{I\} & uv \text{ model fitting} \end{array} \right.$$

CLEAN bias

Convolution: injective mapping

=> **Deconvolution:** non-unique solutions

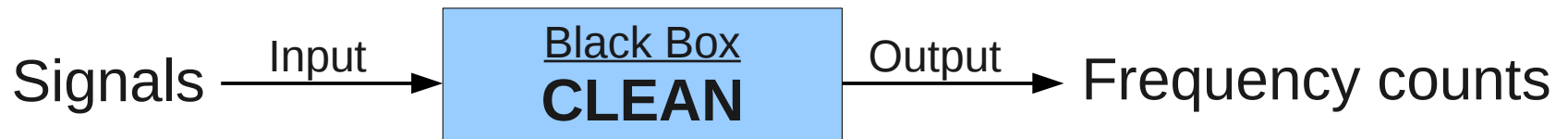
=> **CLEAN:** biased (scattered sidelobe flux
cannot be fully restored)

=> **Source strength:** weakened

=> **rms statistics:** { inconsistent
non-objective

Frequentist method

- **Signal injections**



- **Hypothesis test (Neyman construction)**

Null & Alternative: $\begin{cases} H_0 : D(S) \leq D_0, \\ H_1 : D(S) > D_0. \end{cases} \quad \rightarrow \quad CL(S_0) = P(D \geq D_0 | S_0)$

- **Prior for Bayesian**

Conditional injection:

“Luminosity function” vs. Uniformly most powerful sampling

CL $\xrightarrow[\text{theorem}]{\text{Bayesian}}$ Posterior probability: $P(S \leq S_0 | D \geq D_0)$

A central image candidate

- **JVAS B1030+074**

- Radio source

High resolution observables with VLBI

- Double-image system

Less symmetric than quad system

- High flux ratio

Very asymmetric => non-diminished central image

A real example

- **Central image detection in B1030+074**

Instrument: HSA \equiv VLBA+Gb+Y27+Ar+Eb

Band: 1.7 GHz (L)

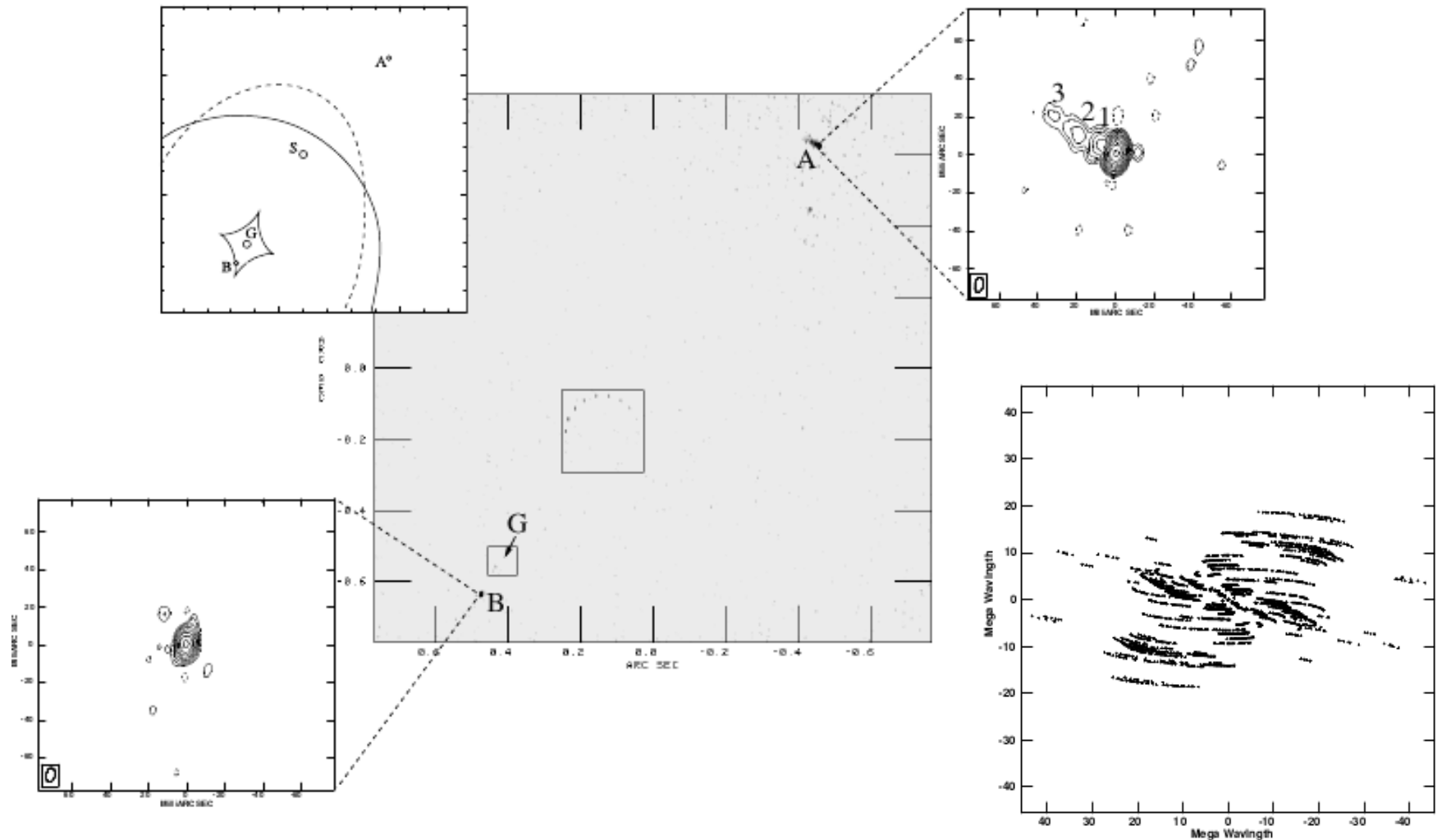
Effective integration time: \sim 4 hours

Data rate: 256 Mb/s

- **Result achieved**

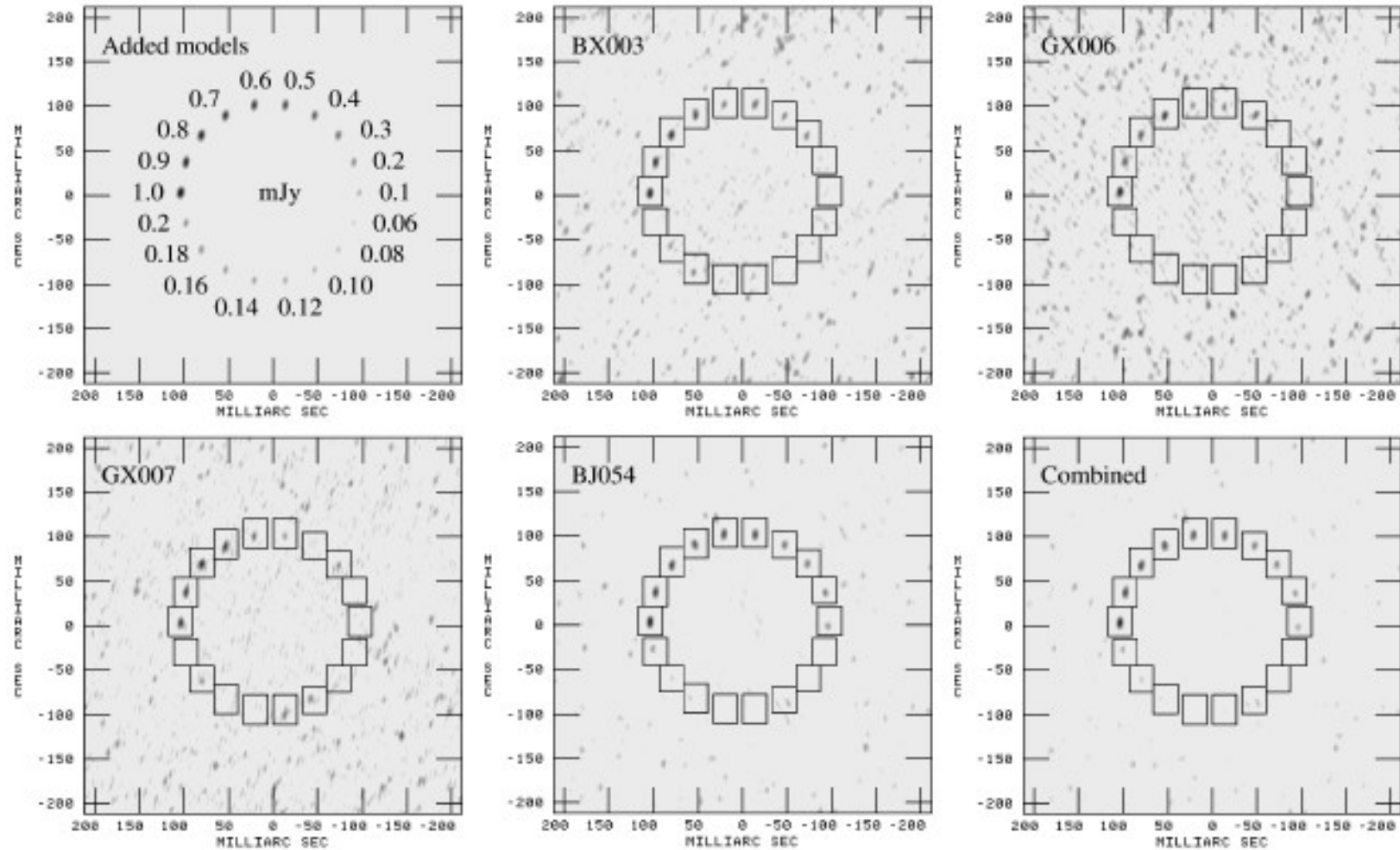
{ Sensitivity claimed: $3.5\mu\text{Jy/beam}$
Sensitivity CLEANed: $20\mu\text{Jy/beam}$
Sensitivity objective: $180\mu\text{Jy/beam}$ (CL90%)

VLBI (HSA) image



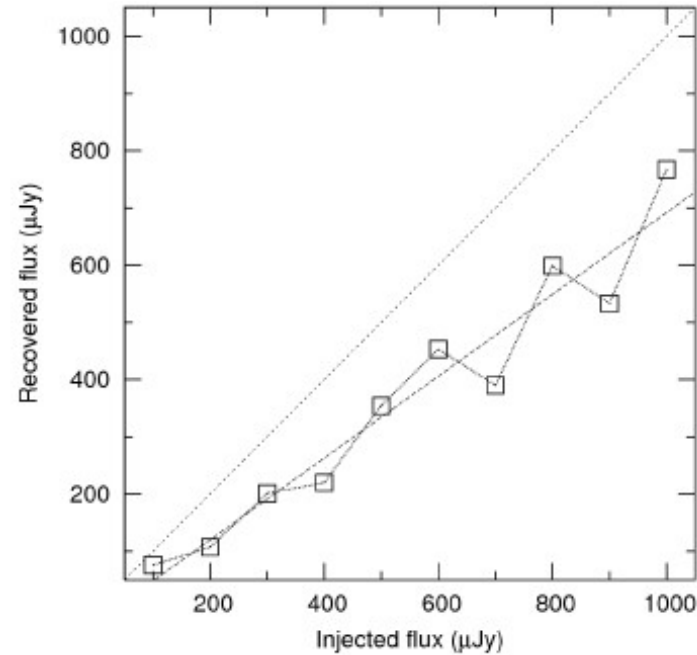
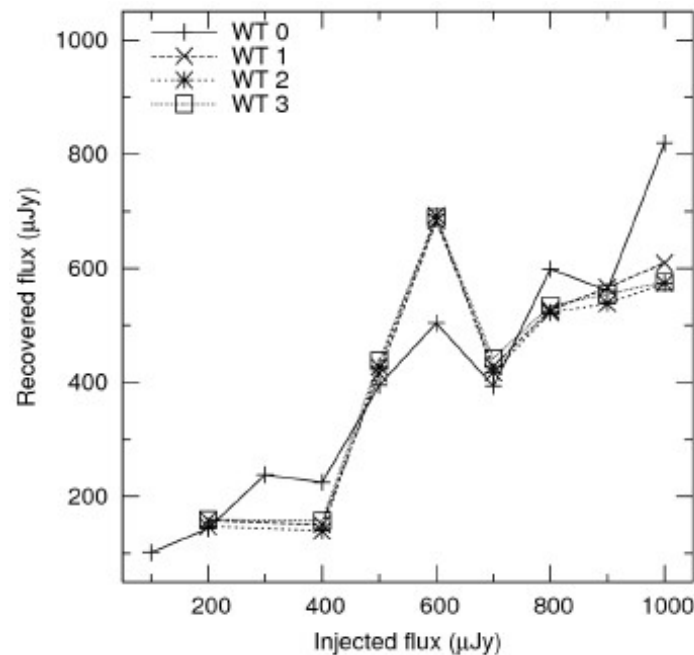
(Zhang et al. 2007)

Ring recovery test



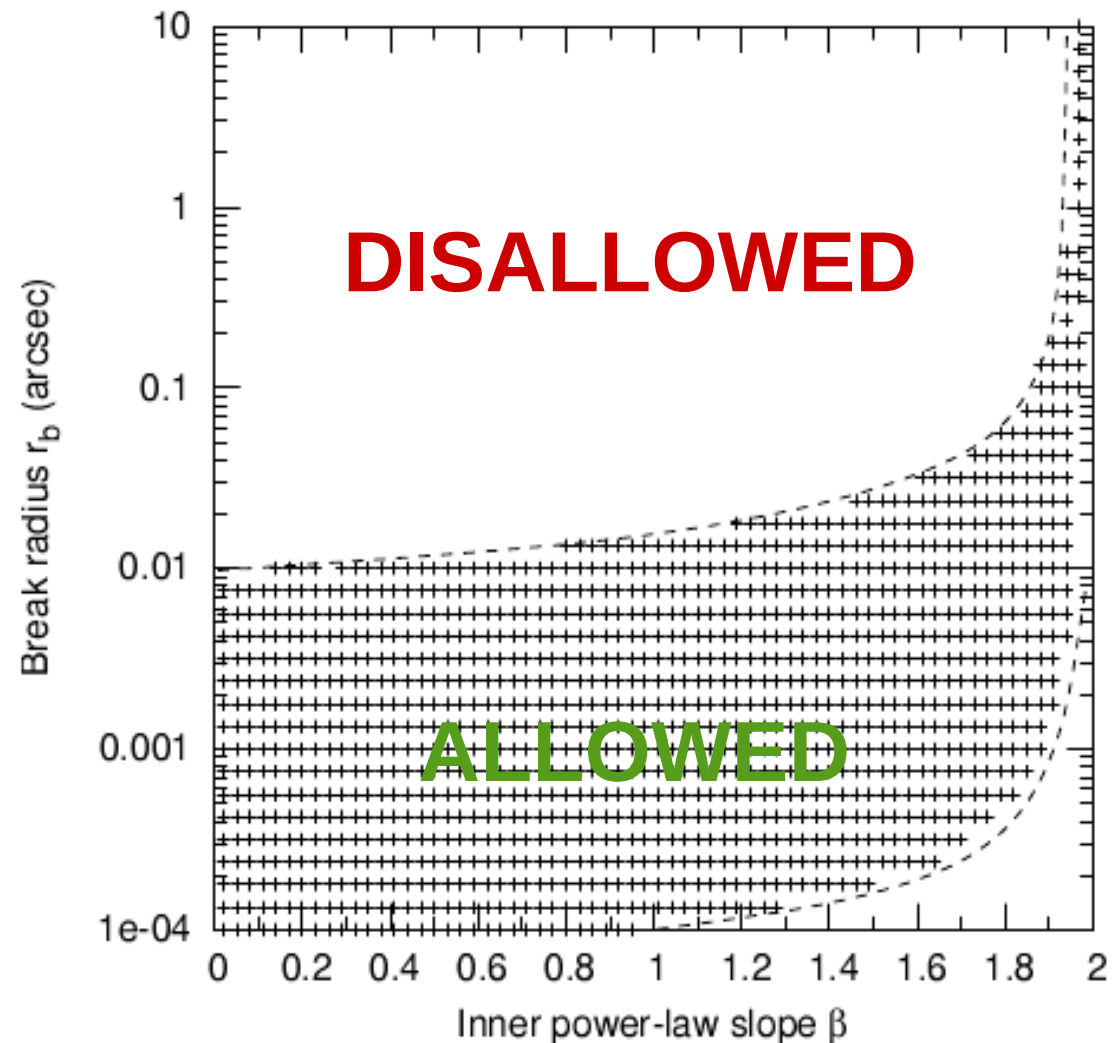
CLEAN loss and weightings

- No clear correlation to weighting schemes
- Up to 30% flux loss in CLEAN procedure

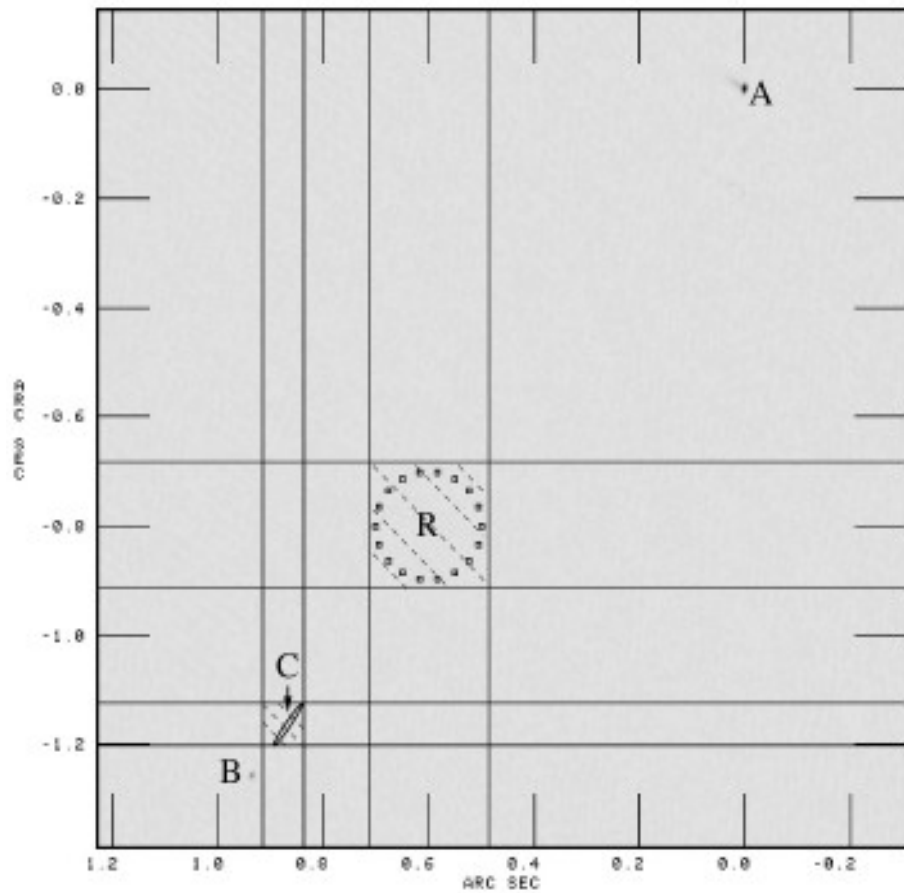


Under-constrained model

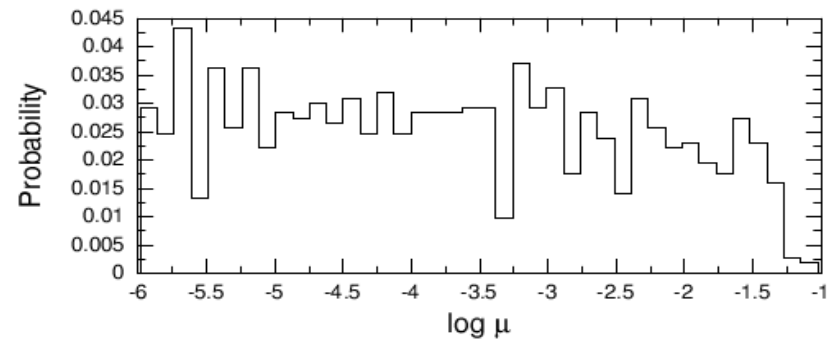
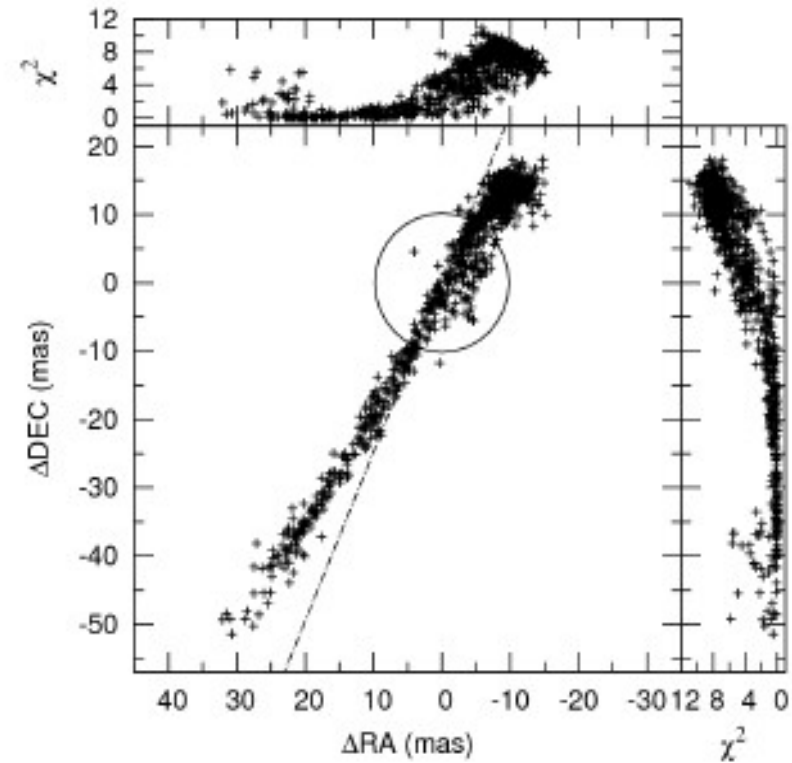
- r_b - β relation
- M_{bh} - β degeneracy
- Parameter grid
 - UMP sampling
 - Model prediction



Central image “club”

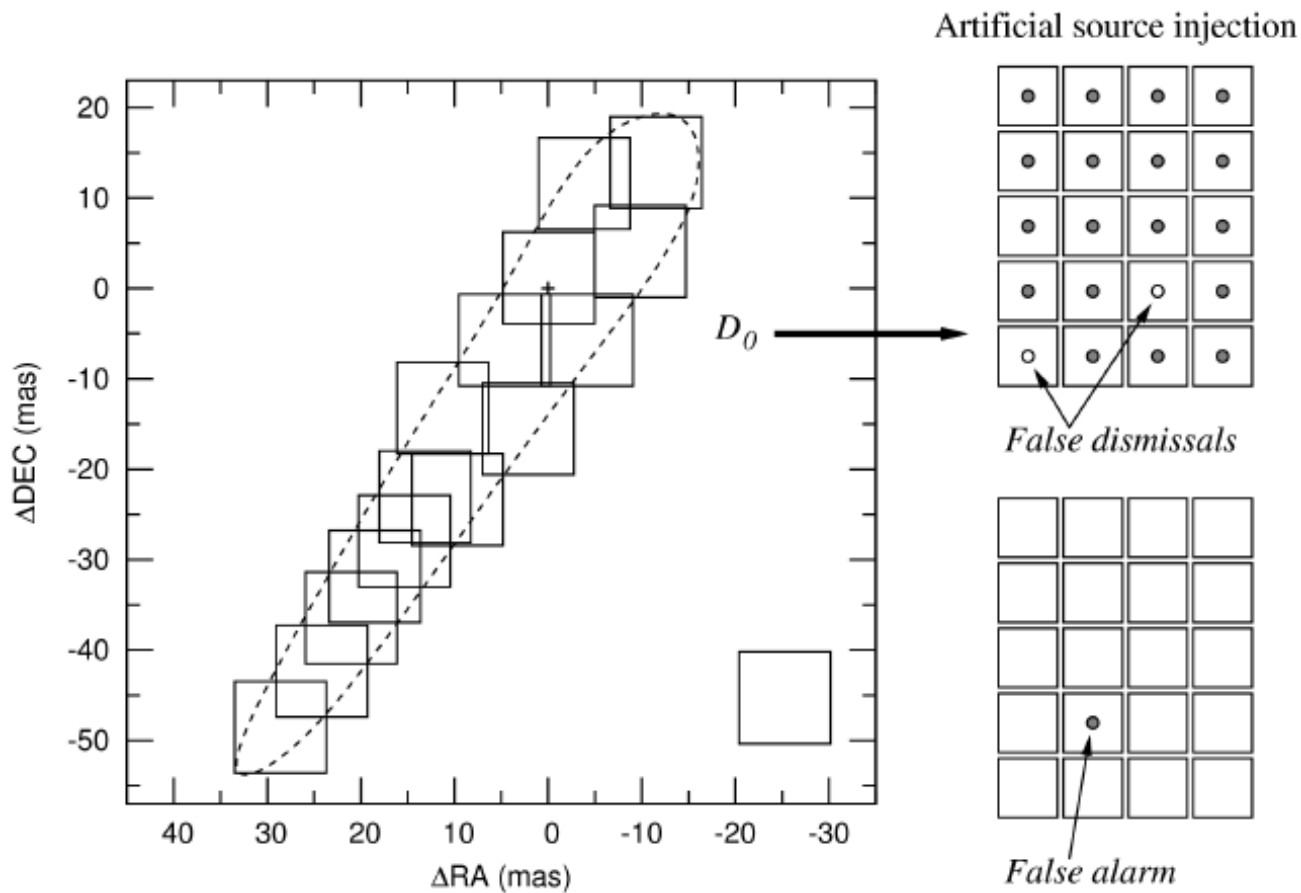


“Luminosity function”



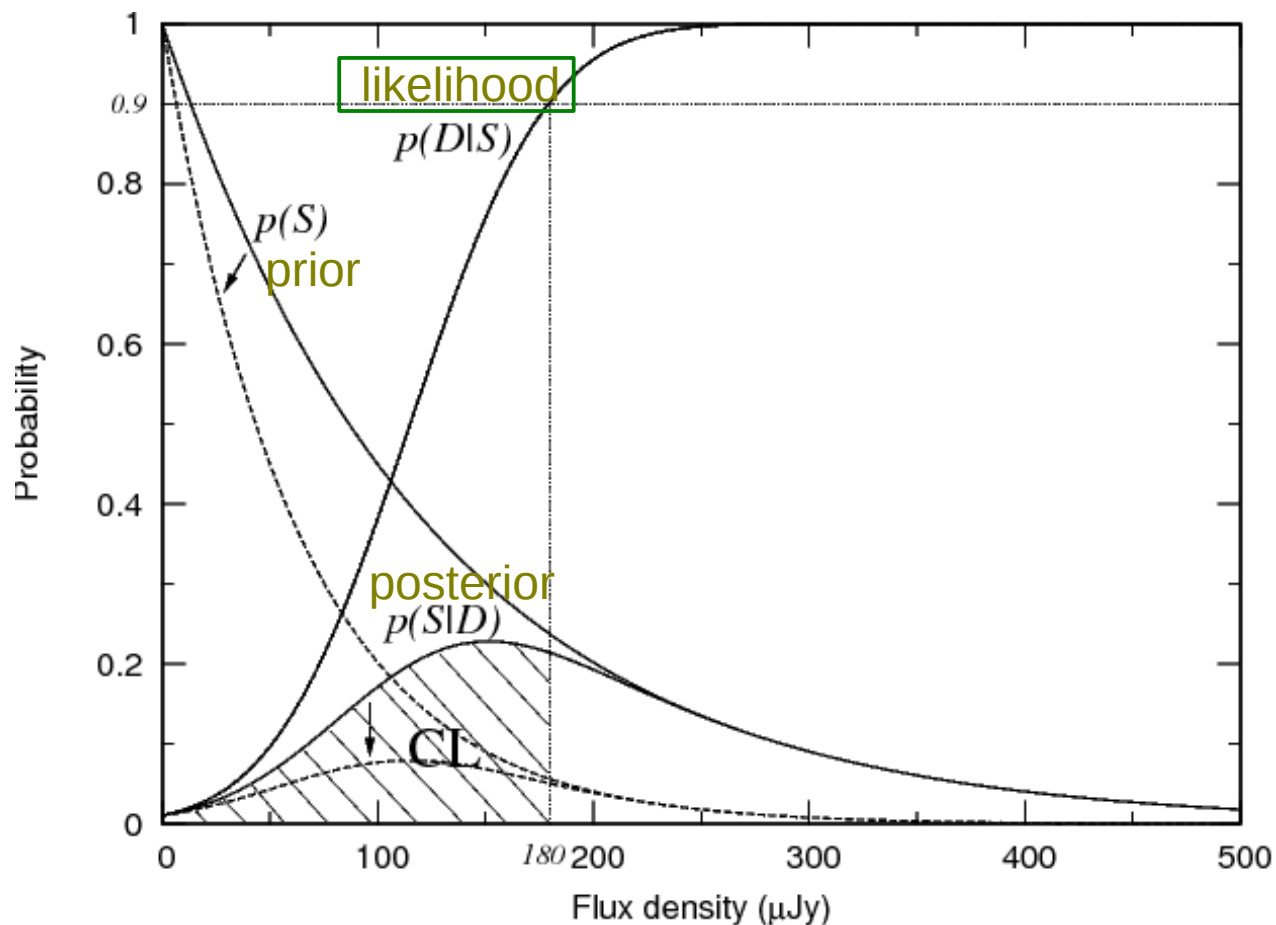
Frequentist statistics

- **90% injections recovered (18 out of 20)**



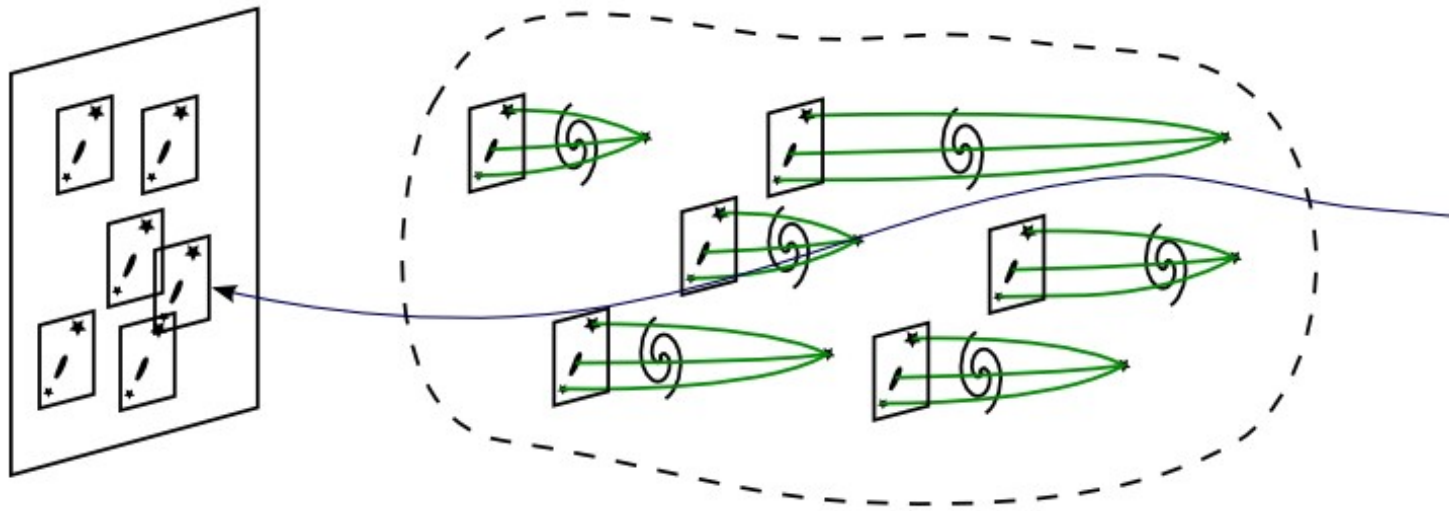
Towards Bayesian

- **Bayes' formula** $P(S|D) = \frac{P(D|S)P(S)}{P(D)}$



Detectability with a prior chain

- Galaxy-quasar lensing paths



- Mock lens simulation

$$P_{cen} = P(f_{cen} > f_{thr}, \Delta\theta_{cen,sad} > \theta_{res}, (M, \theta_d, z_d), (S, \beta, z_s))$$

$$\longrightarrow P_{cen} = P(\mu_{cen} > \mu_0)P(S > f_{thr}\mu_0)P_{len}$$

Conclusions

- Current detection/non-detection with VLBI limit is frequentist
- Detectability requires a realistic “luminosity function” of lensed central image
- N-body simulations currently cannot provide plausible priors since at subgalactic scale they need be testified first
- Observationally the real solution to central image relies on future lens samples and real detections