

SKA I-AA-low: CD/EoR Science, Requirements and Request for (no/some) Change

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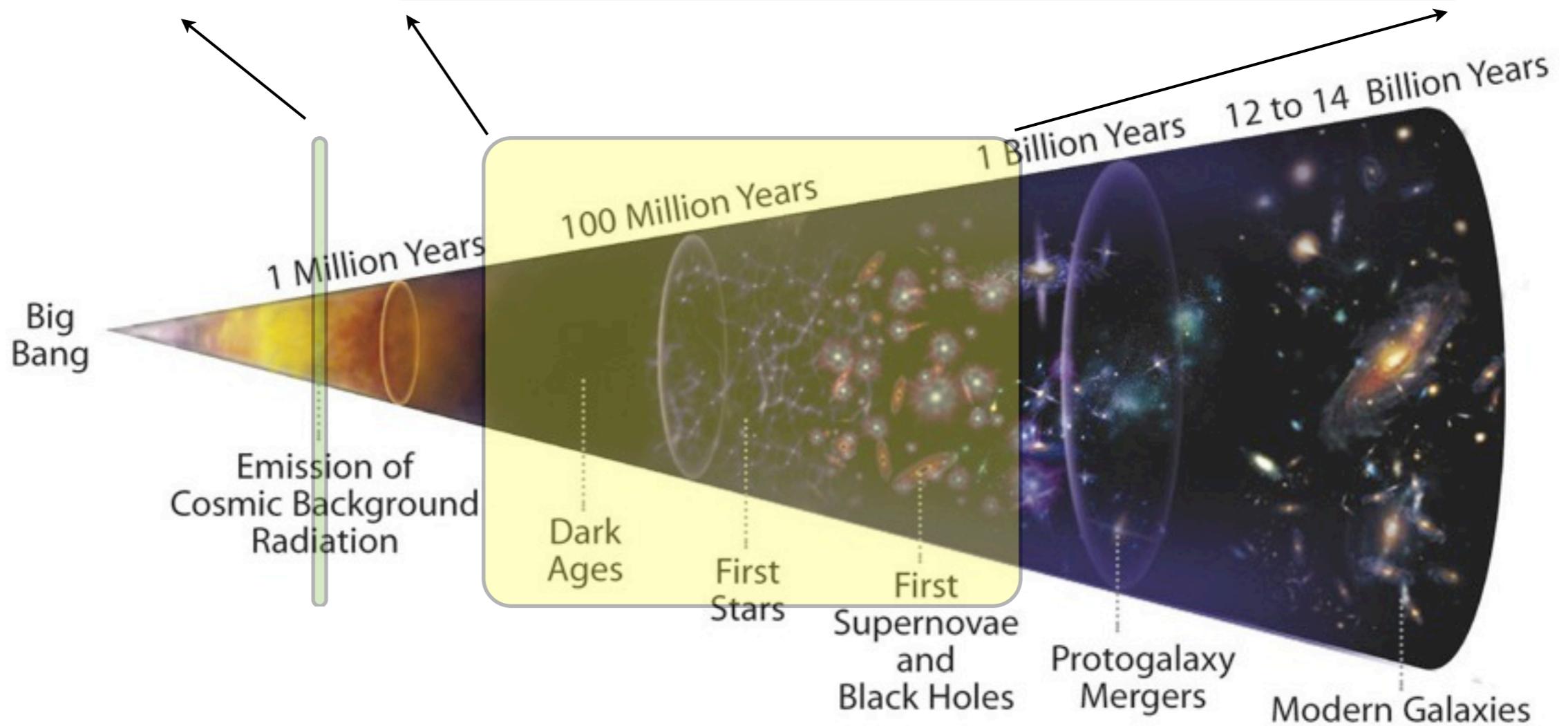
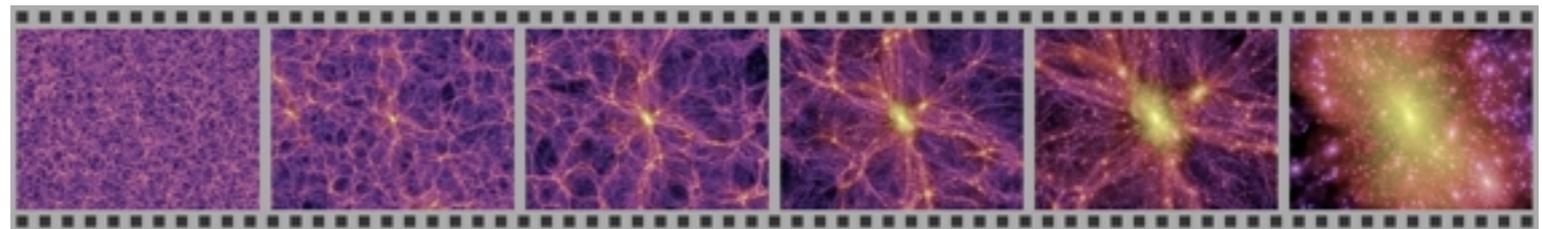
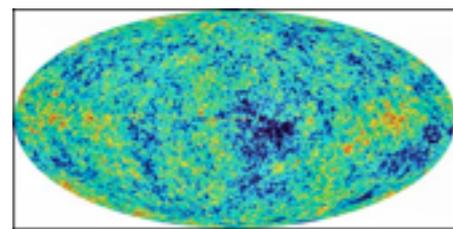
F. Abdalla, J. Aguirre, K. Ahn, A. Parsons, I. van Bemmelen, G. Bernardi, F. Briggs, A.G. de Bruyn, T.-C. Chang, L. Greenhill, G. Mellema, M. Morales, U.-L. Pen, J. Pritchard, M. Santos, B. Semelin, T. Tsutomu, R.L. Webster

- Cosmic-Dawn/EoR Science Requirements
- Implications on the design of SKA(-I)
- Rf(no)C of the current baselines design

Dark Ages, Cosmic Dawn & EoR

CMB displays a single moment of the Universe. Its initial conditions at $\sim 400,000$ yrs

HI emission from the Dark Ages, Cosmic Dawn & EoR traces an evolving “movie” of baryonic structure formation. ($< 10^9$ yrs)



Short Summary of Constraints on the EoR

Most evidence points at substantial reionization (still) occurring at $z < 10$, but its cause/source is unknown: better tracers are needed (i.e. HI itself)

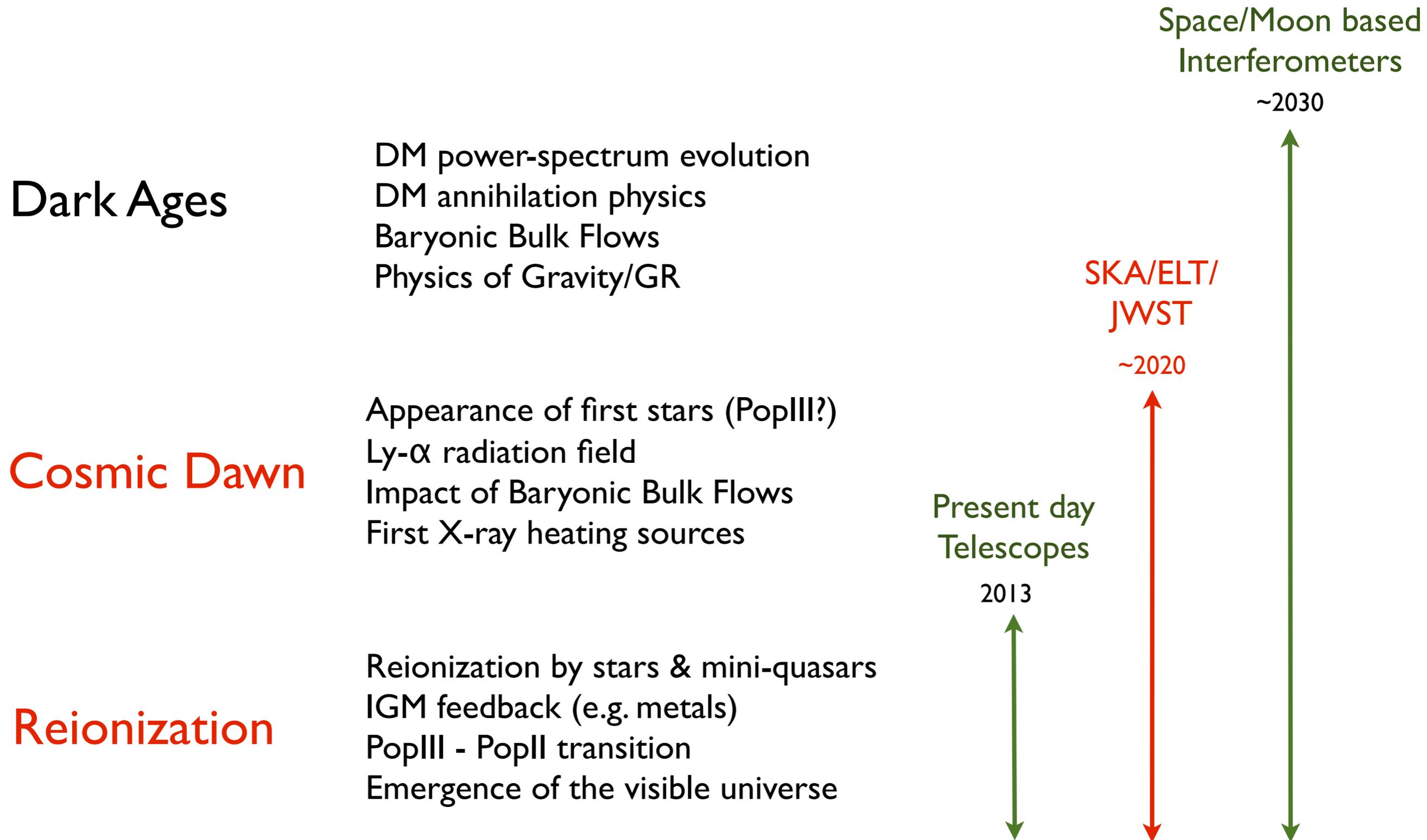
- Scattering optical depths from CMB observations
Ionized medium causes CMB polarization: $z_{\text{eor}} \sim 10$
- High- z galaxies
IR drop-outs give SFR/LF to $z \sim 10$: SFR rises fast below $z \sim 10$ but there are not enough UV photons to re-ionize the Universe >>> Puzzle!
- High- z QSOs
Gunn-Peterson troughs suggest $\sim 10\%$ neutral HI at $z \sim 7$, i.e. the end of reionization occurs close to the highest z QSO/galaxies that we observe
- High- z GRBs
GRBs traces massive star formation. Currently rare events, but $z \sim 8.2$ GRB has been seen and could be a direct tracer of the SFR.
- Temperature of the IGM
Extrapolation of the high- z IGM temperature suggest late reionization

Changes in our understanding of the CD/EoR eras, since 2004

- Since the SKA Science Book (2004) a dramatic change in our understanding of how the CD/EoR has unfolded (*) “Reionization and the Cosmic Dawn with the SKA”, Mellema, Koopmans et al., 2013, Exp.Ast.
 - **CMB scattering optical depth** gives $z_{\text{EoR}} \sim 10$ rather $z_{\text{EoR}} \sim 20$, bringing the Cosmic Dawn into reach of ground-based radio telescope i.e. SKA.
 - **First discoveries of objects in the EoR:** drop-outs, Ly-alpha emitters, QSOs, GRBs, SNaE up to $z \sim 10$.
 - **New physical phenomena:** e.g. HI bulk-flows at high- z (impact during CD)
 - **Much improved simulations** (larger and more complete physics).
- Guided by these latest results, an updated EoR and Cosmic Dawn science case was written* and recommended - given (although limited) input from current experiments - what the SKA-low design should be in order to study the CD/EoR using both power-spectra AND tomography

What makes SKA special?

It allows study of the Cosmic Dawn & Tomography of the EoR!



Hydrogen Brightness Temperature

The quantity that can be measured with SKA along a given line of sight is given by:

$$\begin{aligned}
 \delta T_b &= \frac{T_S - T_R}{1+z} (1 - e^{-\tau_\nu}) \\
 &\approx \frac{T_S - T_R}{1+z} \tau \\
 &\approx 27 x_{\text{HI}} (1 + \delta_b) \left(\frac{\Omega_b h^2}{0.023} \right) \left(\frac{0.15}{\Omega_m h^2} \frac{1+z}{10} \right)^{1/2} \\
 &\quad \times \left(\frac{T_S - T_R}{T_S} \right) \left[\frac{\partial_r v_r}{(1+z)H(z)} \right] \text{ mK,}
 \end{aligned}$$

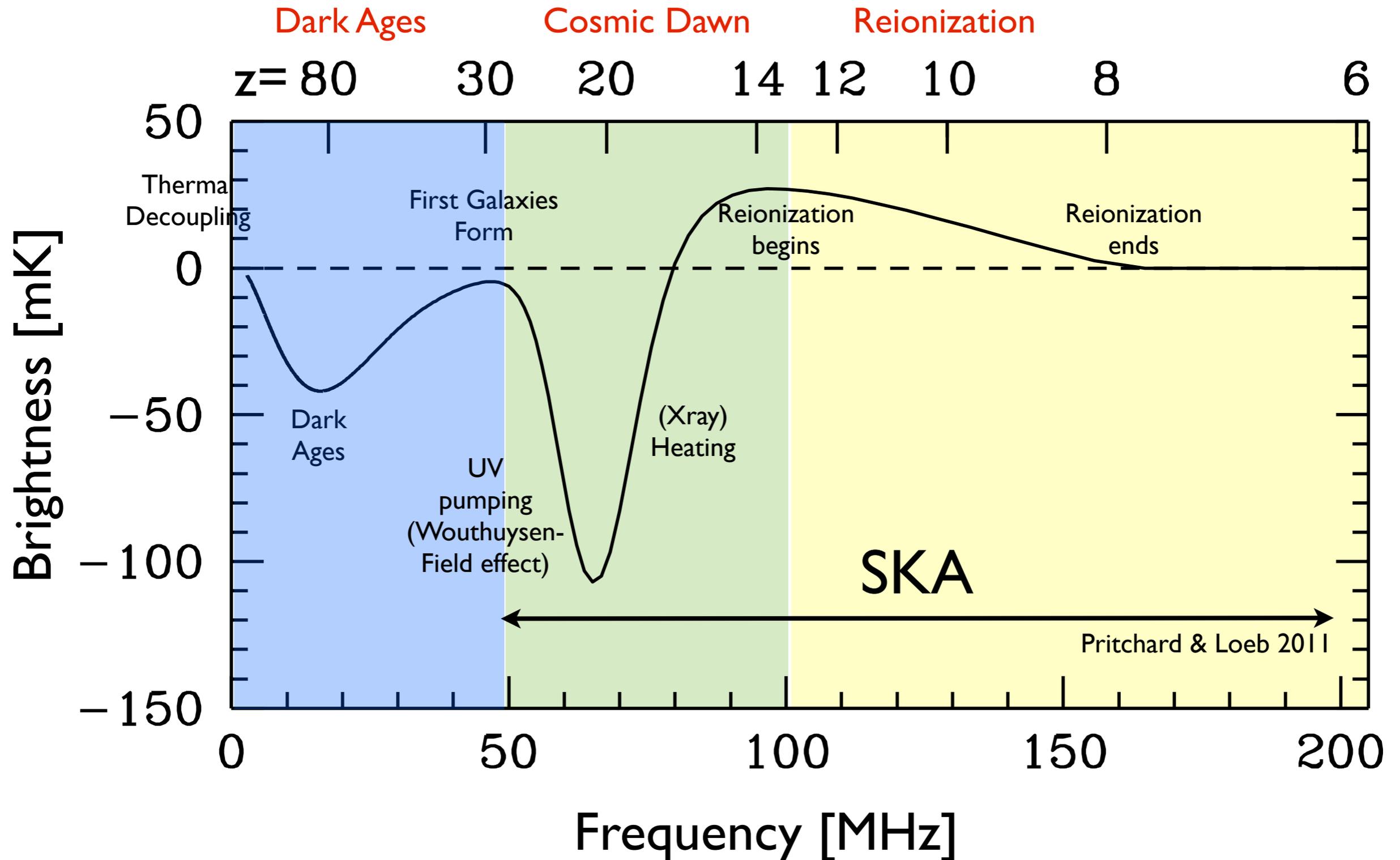
The equation is annotated with blue arrows pointing to various terms:

- Cosmology** points to $\Omega_b h^2$ and $\Omega_m h^2$.
- Ionization** points to x_{HI} .
- (G)astrophysics** points to δ_b .
- Peculiar velocities/Bulk-flows** points to $\partial_r v_r$.

The HI 21-cm intensity is set by a complex interplay between **cosmology** and **(g)astrophysics**.

Hydrogen Brightness Temperature

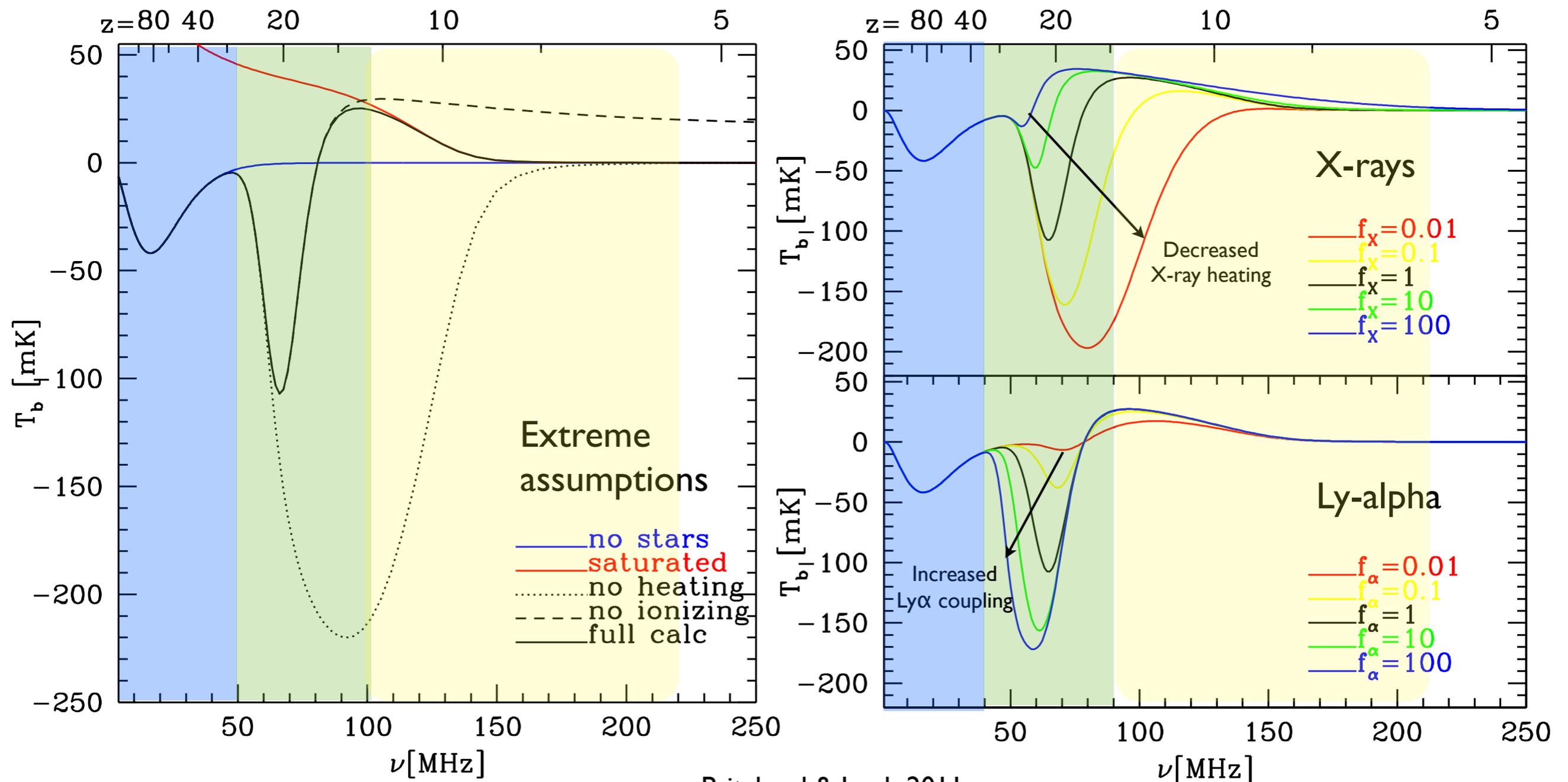
Global Signal



Hydrogen Brightness Temperature

Global Signal

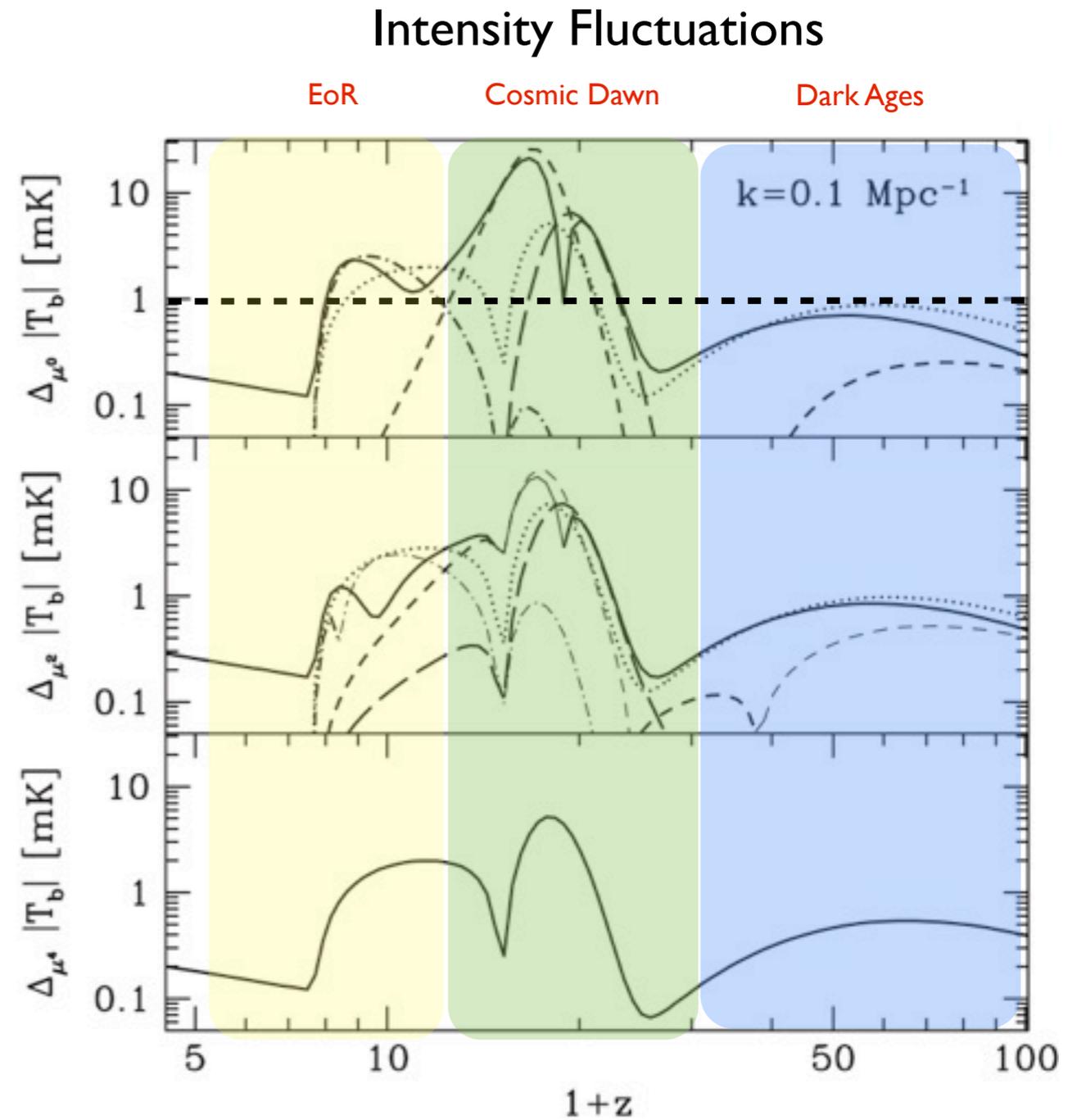
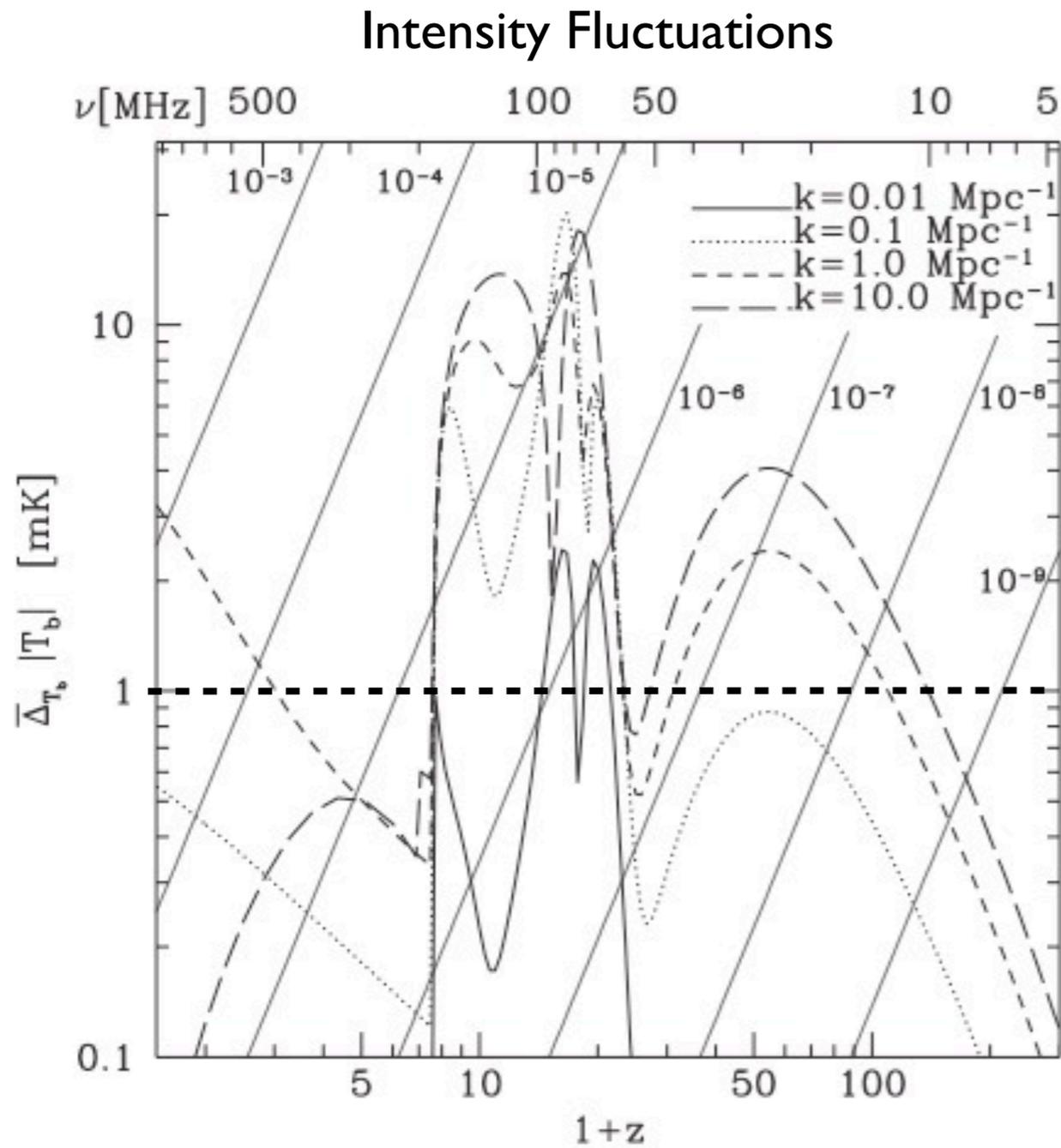
The history of T_b can vary; hence measuring T_b as function of redshift/time, provides a handle on SF, Ly- α coupling (WVF), (X-ray) heating, etc.



Pritchard & Loeb 2011

Hydrogen Brightness Temperature

Power-Spectrum

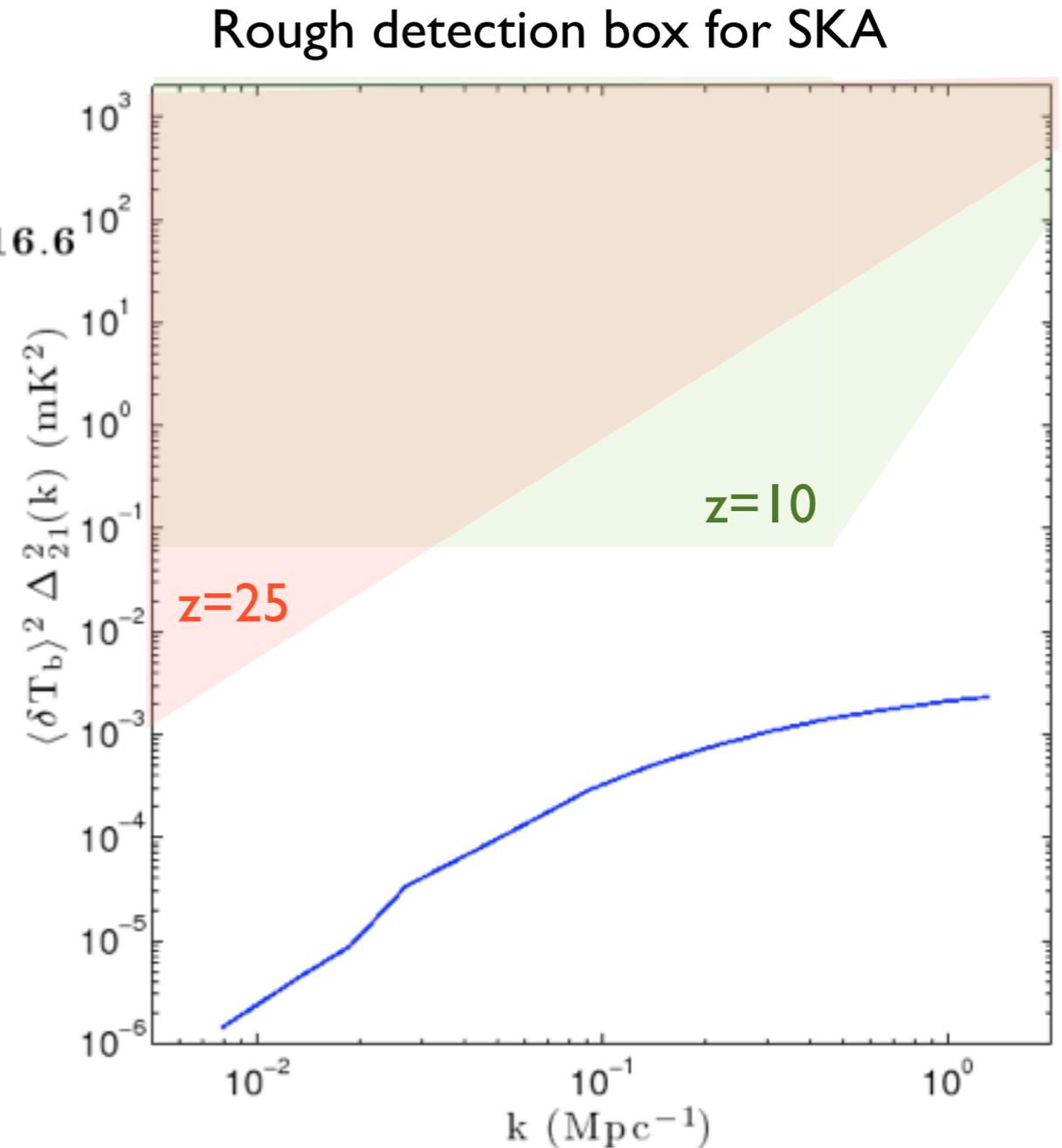
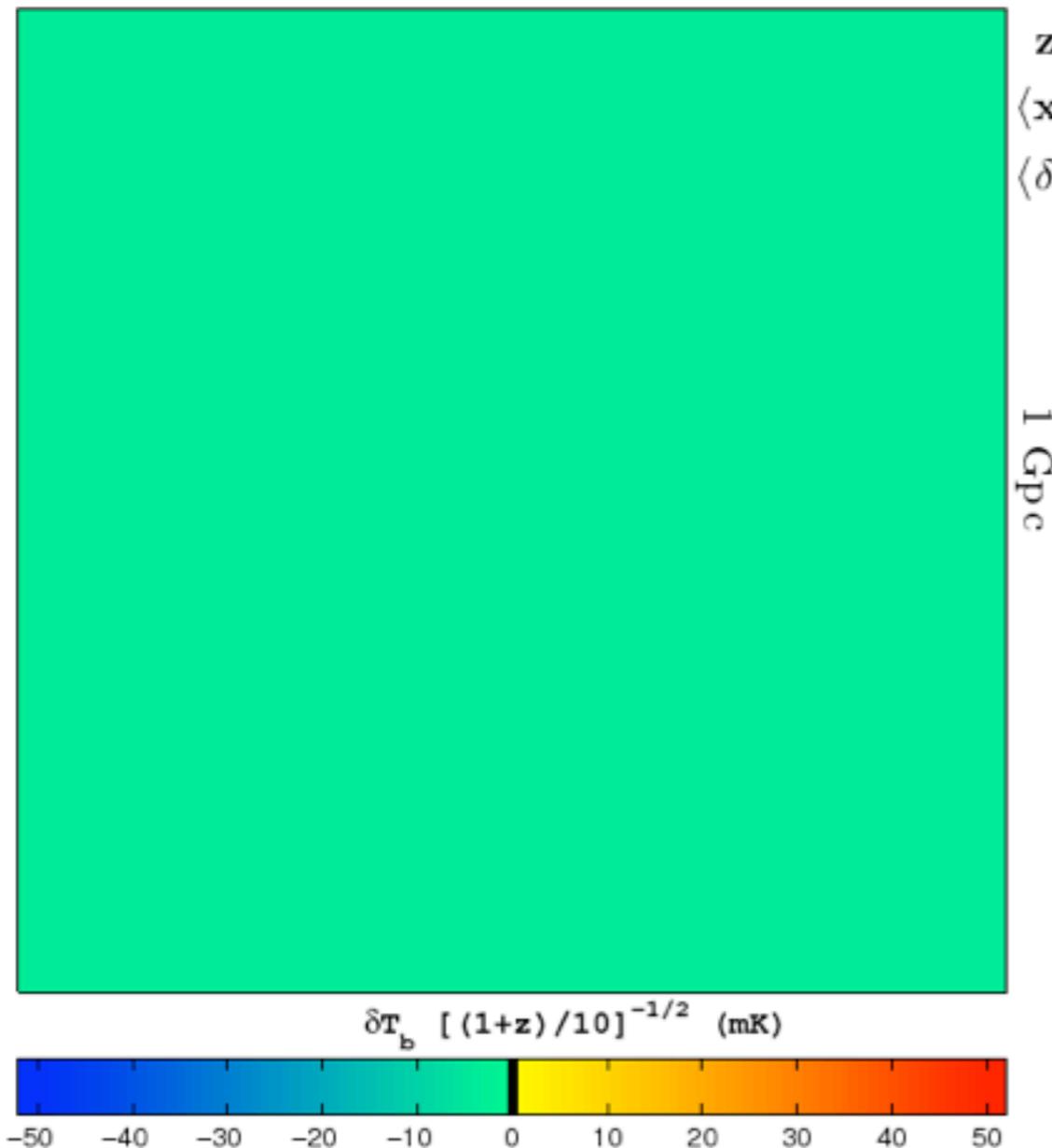


Pritchard & Loeb 2009; see also Santos et al. 2008, 2010, 2011

Hydrogen Brightness Temperature

Tomography & Power-spectrum

Credit: Mesinger



Sensitivity limits are scale dependent but $\Delta_{\text{noise}}^2 \sim \text{few mK}^2$ is where current instruments aim for in ~ 1000 hrs. SKA can go to $\Delta_{\text{noise}}^2 \sim 0.1 \text{ mK}^2$

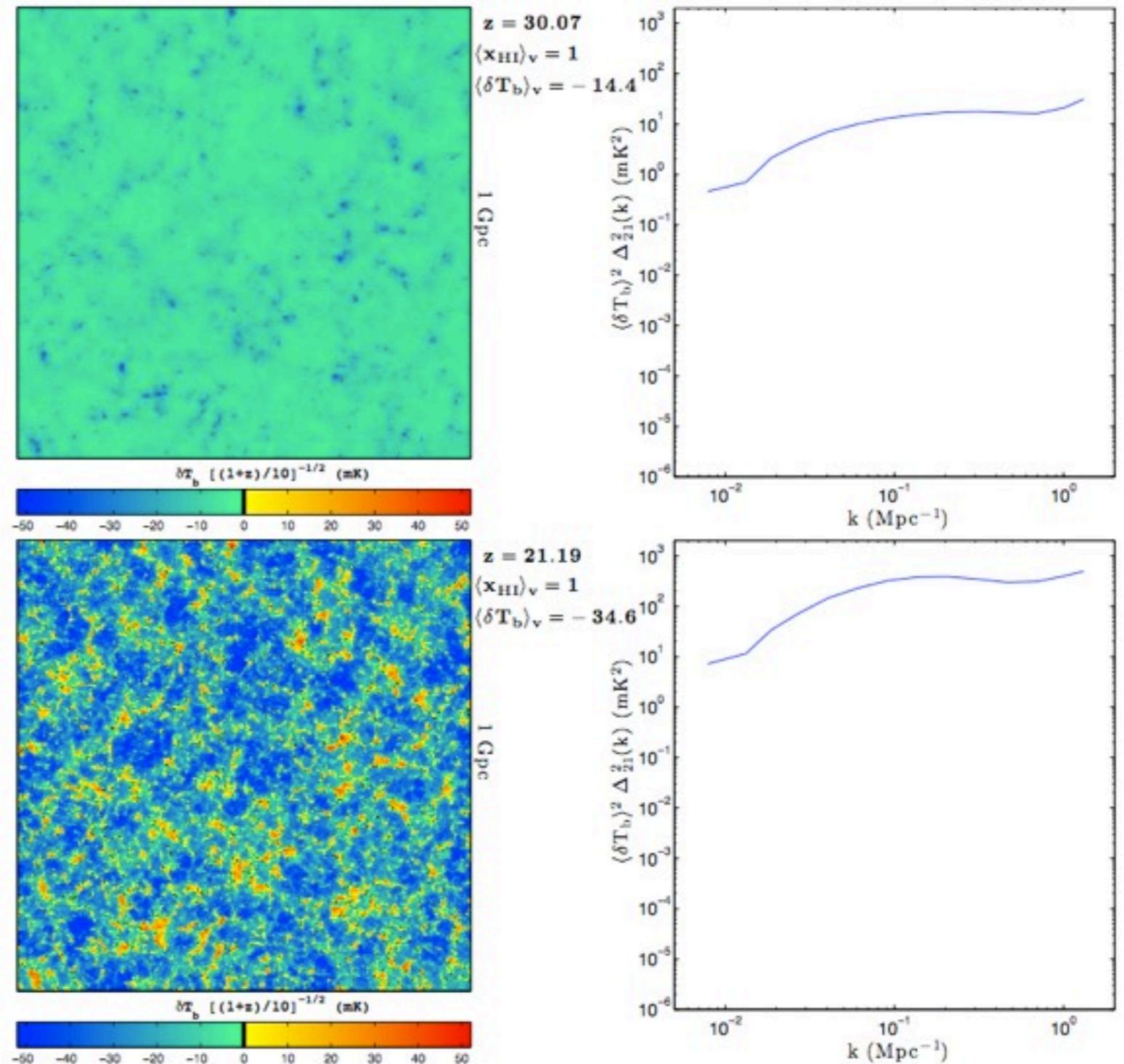
Hydrogen Brightness Temperature

Tomography & Power-spectrum

Cosmic Dawn

The first stars form in $\sim 10^8 M_{\text{sun}}$ haloes and start coupling the spin temperature (locally) to the cold gas temperature (W-F). After some time X-ray sources(?) heat the gas and cause the spin-temperature to rise again.

At high- z HI is seen in absorption with fluctuations sourced by baryonic density fluctuations. Some time later locally the gas is heated by X-rays and locally couples to the spin-temp. causing patches in absorption and emission, sourcing T_b fluctuations.



Mesinger 2010

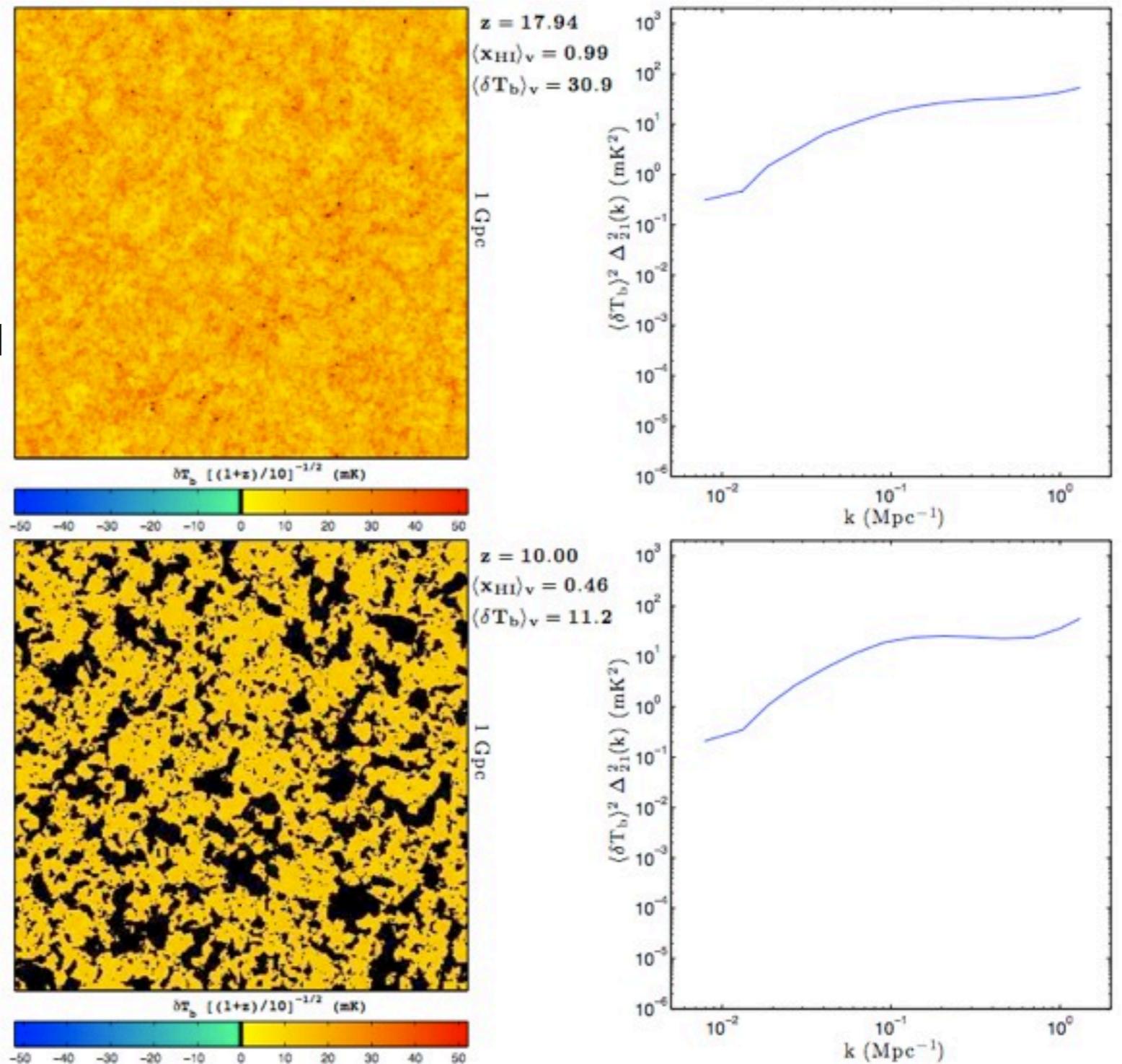
Hydrogen Brightness Temperature

Tomography & Power-spectrum

Reionization

After a while X-ray heating is completed and HI is only seen in emission and is still mostly neutral. Fluctuations are sourced again by density fluctuations and peculiar velocities.

Finally ionization sets in and causes bubbles to occur. The strong contrast between bubbles and neutral patches is another sources of T_b fluctuations.



Mesinger 2010

SKA I: Transformational or not?

For SKA I to be *transformational* and not a statistical HI detection instrument like its pathfinders MWA, PAPER, LOFAR, GMRT, it should be able to:

- (1) Study the **Cosmic Dawn** (to $z \sim 25$) via **tomography** on large scale and via power-spectra on smaller scales.
- (2) Enable **tomography** on all scales (few arcmin-degrees) during the full **Epoch of Reionization** ($z \sim 6-15$).

Top-level Science Requirements

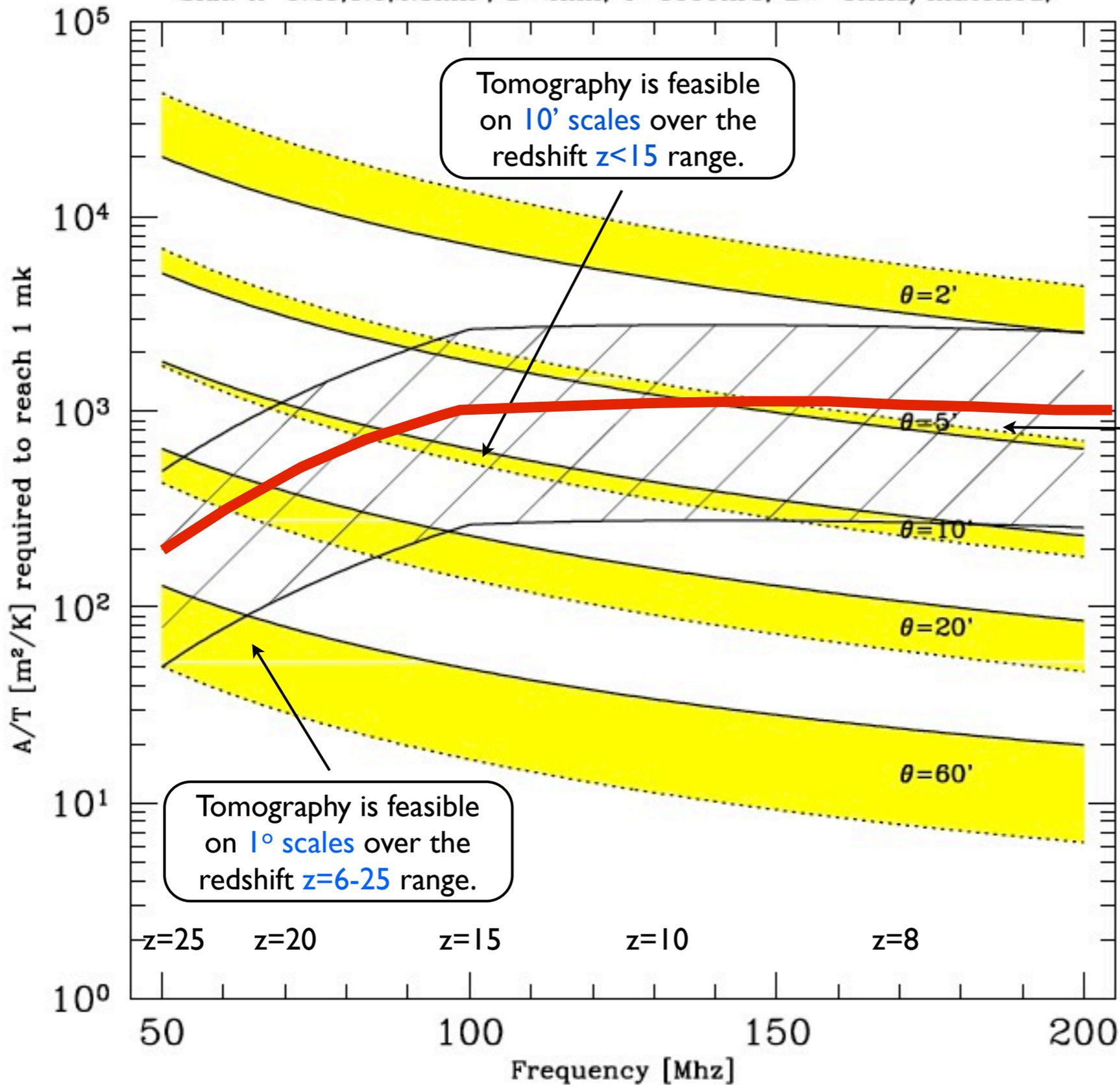
- Redshift/Freq. Range:
 - **$z \sim 25-6$** - trace the Cosmic Dawn prior to EoR and the EoR till full reionization ($z \sim 5-6$) [motiv.: CMB-pol, G-P].
- Angular scales for power-spectrum & tomography:
 - **arcminute - degrees** - Allow PS measurement on degree scales over the full freq. range and tomography on degree scale at $z=25$ and on all scales $>5'$ at $z=10$.
- Brightness temperature:
 - **$dT_b \sim 1 \text{ mK rms}$** between bubbles; $\sim 10 \text{ mK}$ on/off bubbles [set by state-of-the art simulations plus CMB/G-P limits]

In excellent agreement with

THE SQUARE KILOMETRE ARRAY DESIGN REFERENCE MISSION: SKA PHASE 1

Document number SCI-020.010.020-DRM-002
Revision..... 3
Author SKA Science Working Group
Date 2012-05-28
Status Requirements Baseline

SKA: $A=0.25, 1.0, 2.5 \text{ km}^2$, $D=2 \text{ km}$, $T=1000 \text{ hrs}$, $BW=1 \text{ MHz/matched}$,



SKA Tomography

Tomography is feasible on 5' scales over the redshift $z < 8$ range.

EoR: $z < 15$

In 1000hr with a $BW=1 \text{ MHz}$ or matches to angular scales, one can do tomography to the required level of $\sim 1 \text{ mK}$ on scale $> \sim 10'$

Cosmic Dawn: $15 < z < 25$

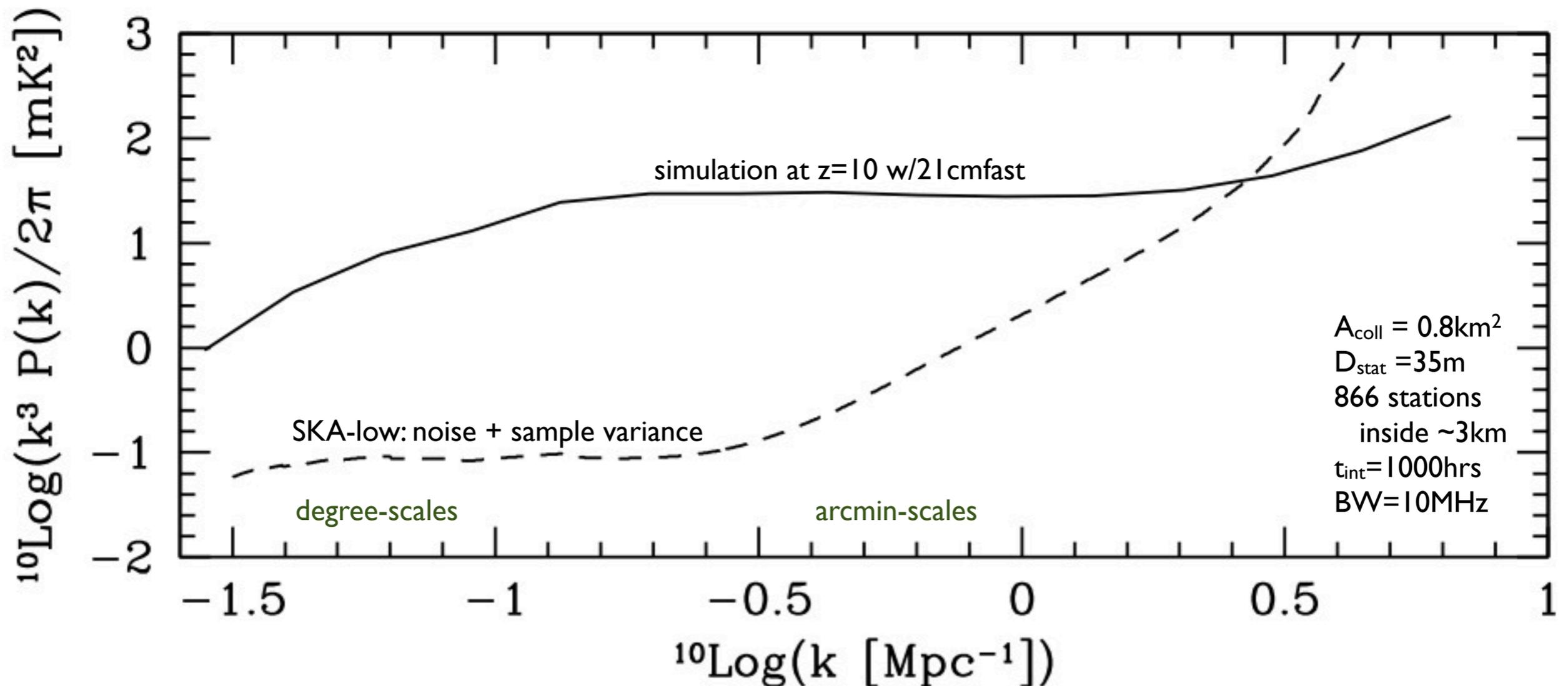
Idem, on scales $> \sim 1^\circ$.

Measuring the EoR HI- T_b Power-Spectrum at $z=10$

Assuming the current SKA baseline design

SKA1 SYSTEM BASELINE DESIGN

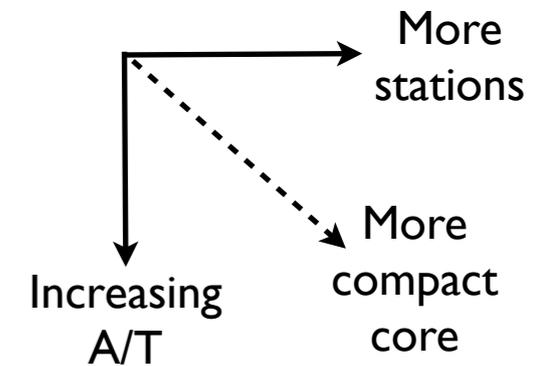
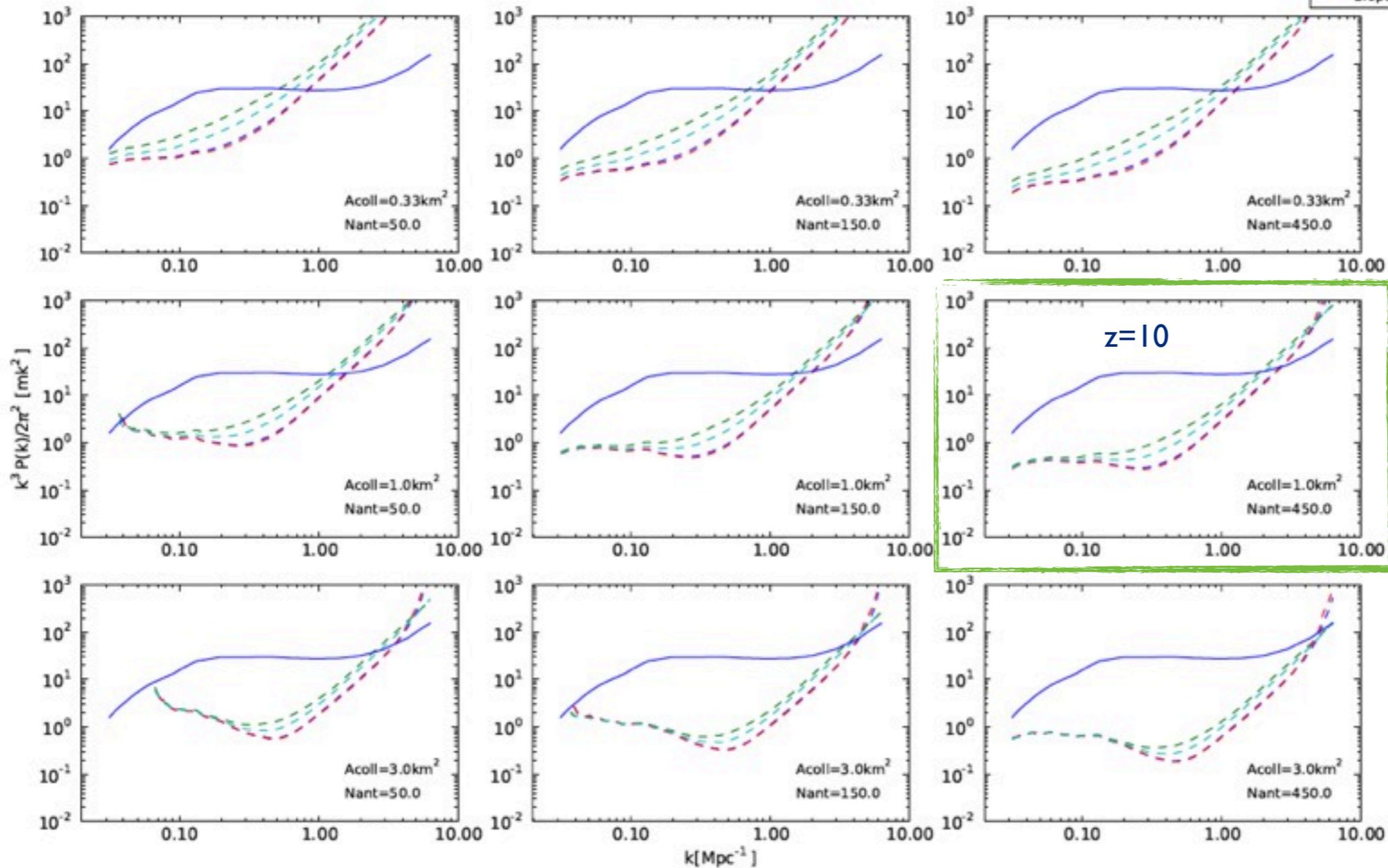
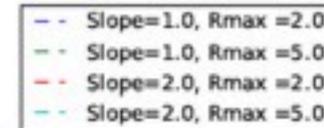
Document number SKA-TEL-SKO-DD-001



SKA Power-Spectrum Sensitivity for Single Beam

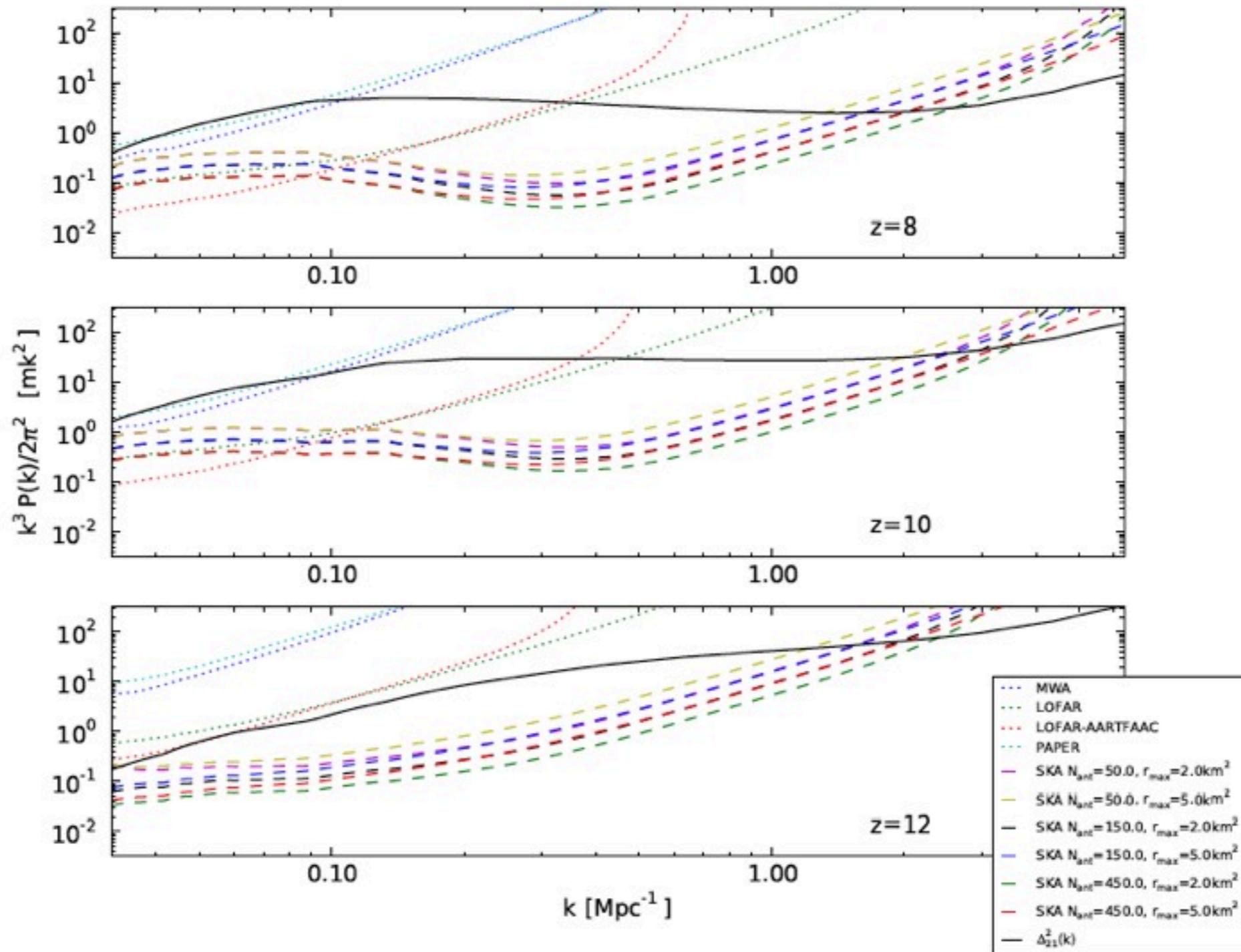
$$\Delta_{\text{Noise}}^2 = \left(\frac{2}{\pi}\right) k^{3/2} [D_c^2 \Delta D_c \times \Omega_{\text{FoV}}]^{1/2} \left(\frac{T_{\text{sys}}}{\sqrt{Bt_{\text{int}}}}\right)^2 \left(\frac{A_{\text{core}} A_{\text{eff}}}{A_{\text{coll}}^2}\right)$$

Different core diameters and station densities



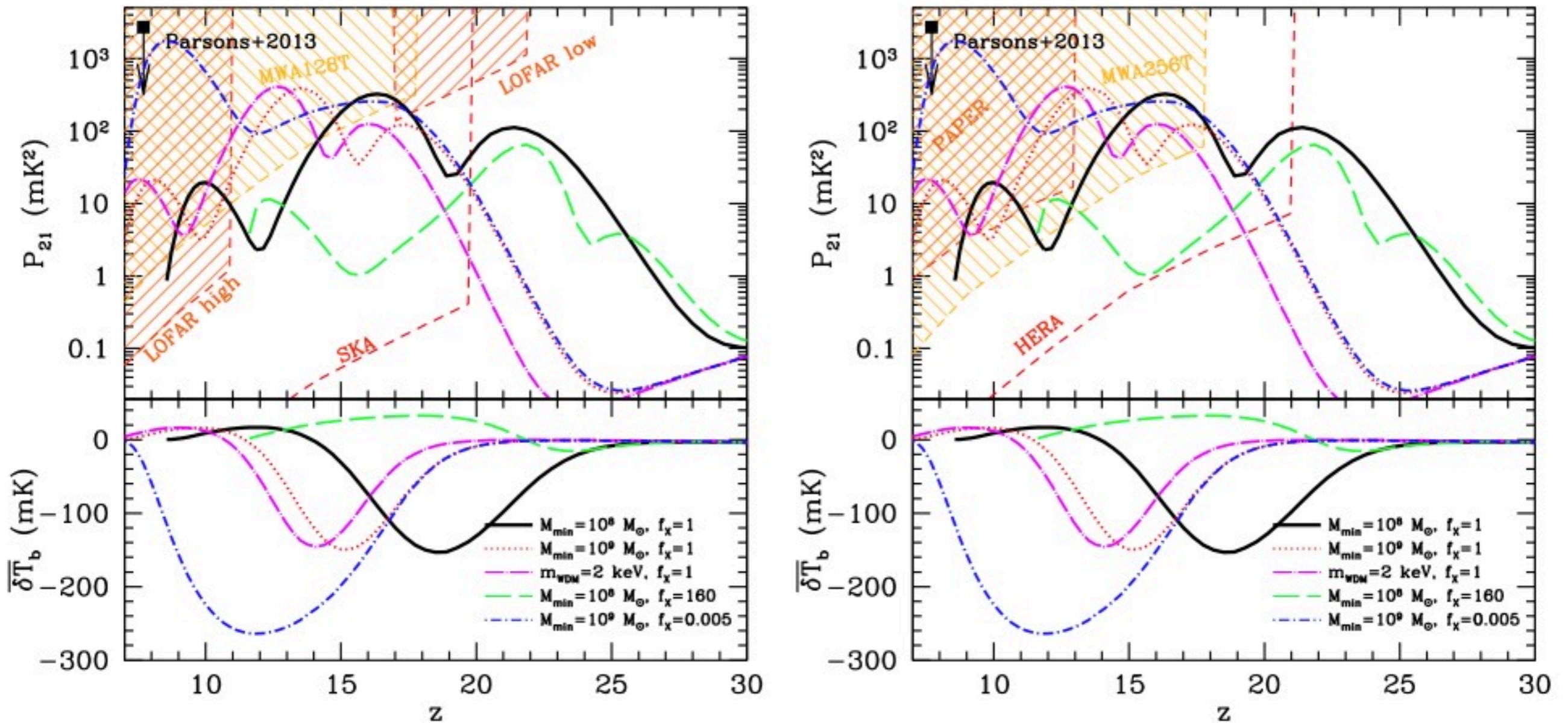
SKA versus Current Arrays

$$\Delta_{\text{Noise}}^2 \propto \left(\frac{A_{\text{core}} \sqrt{A_{\text{eff}}}}{A_{\text{coll}}^2} \right) \propto \left(\frac{A_{\text{core}}}{N_{\text{stat}}^2 A_{\text{eff}}^{3/2}} \right) \propto \left(\frac{A_{\text{core}}}{\sqrt{N_{\text{stat}}} A_{\text{coll}}^{3/2}} \right).$$



SKAI-AA-low Power-spectrum sensitivity (current baselines design)

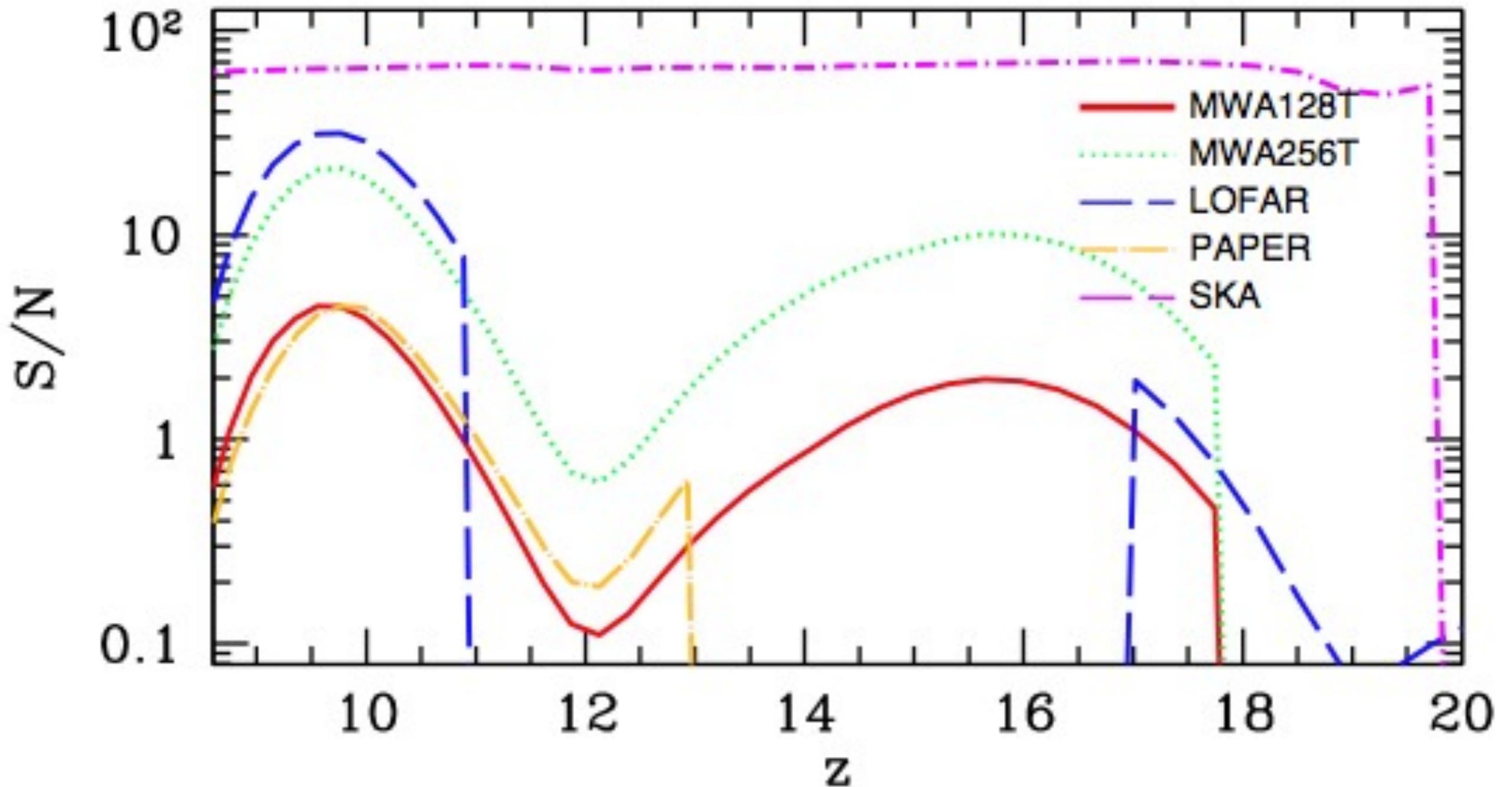
Sensitivity of SKAI versus pathfinders (2000hrs)



Mesinger et al. 2013

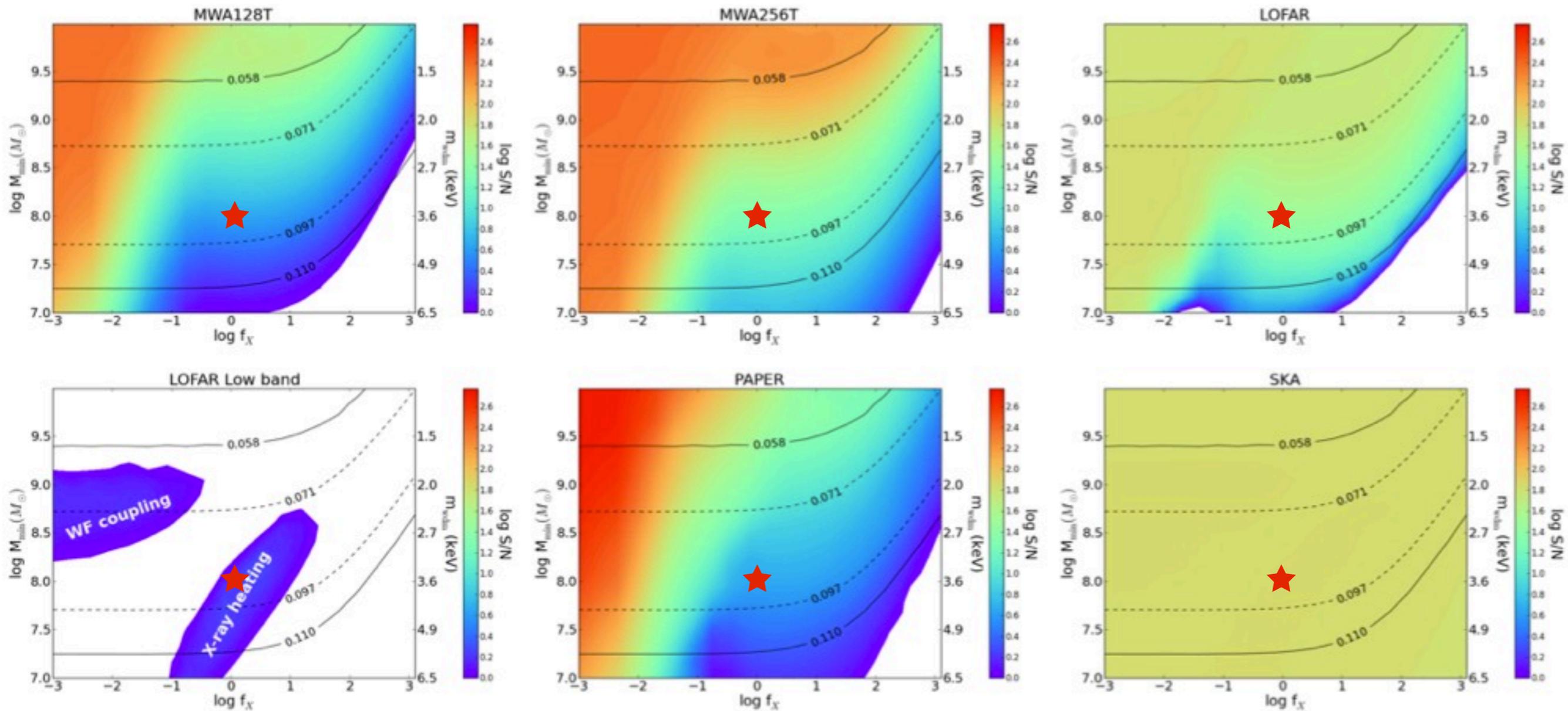
SKAI-AA-low Power-spectrum sensitivity (current baselines design)

Sensitivity of SKAI versus pathfinders (2000hrs)



SKAI-AA-low Power-spectrum sensitivity (current baselines design)

S/N for different heating and halo models (nominal $M_{\min} = 10^8 M_{\text{sun}}/f_X = 1$ model is a red star)



S/N > 100 with SKAI for
all models

Mesinger et al. 2013

Impact on the Design of SKA-low

FoV/Station size

- CD/EoR simulations suggest that scales $\sim 1'$ to ~ 1 degree can show $dT_b \sim 1$ mK fluctuations. Limiting the sample variance and loss in structure in tomography requires at least $\text{FoV} \gg 1$ degree.
- A larger FoV/smaller station for fixed A_{coll} , leads to a better uv-coverage, which helps instantaneous calibration.
- A too large FoV/too small station, might lead to a sky that is only calibratable around bright sources \Rightarrow analogy with MC-AO systems!
- Multi-beaming can only partly recover scales $>$ station beam, but can build up power-spectrum sensitivity on scale inside the beam and do tomography.
- Too many small stations cost much more correlator/computing power

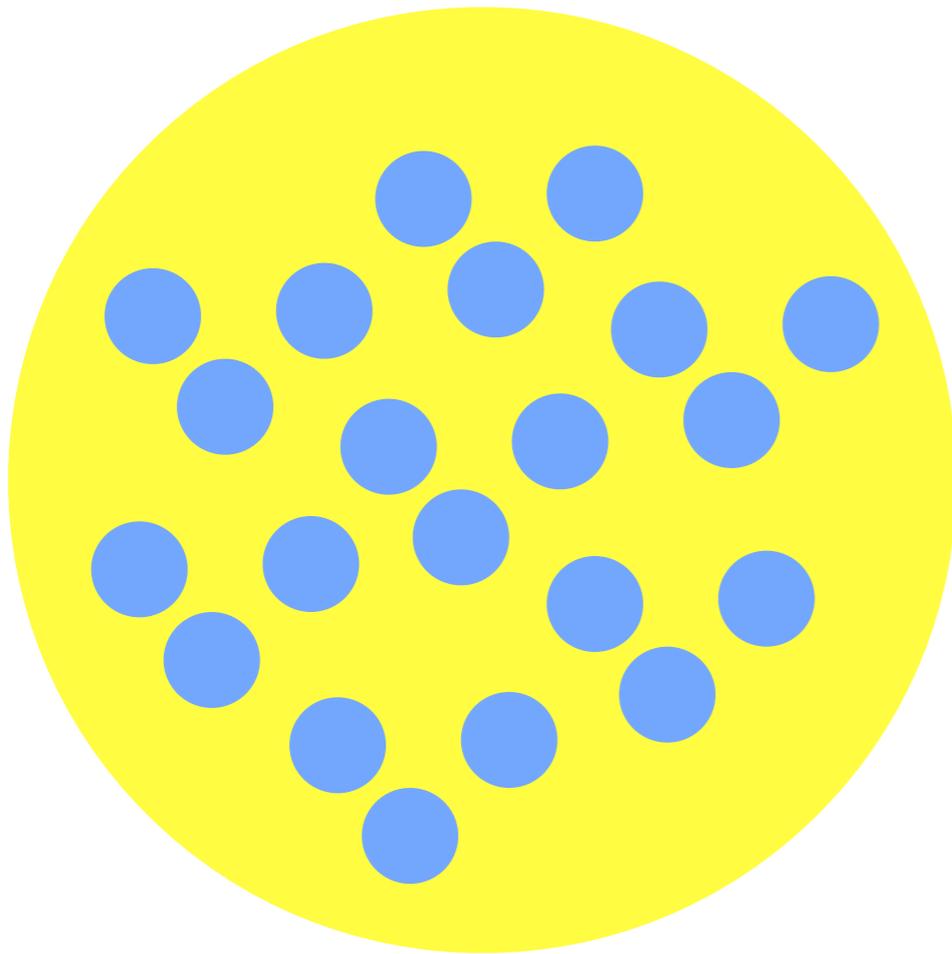
SCIENCE REQUIREMENTS

Long Baselines

- Calibration using long baselines reduces model degeneracies. The sky is “simpler” at long baselines, whereas the science is at short baselines. Hence the danger of covariance between calibration and EoR parameters is reduced
- Information content in uv plane is much larger when going from say 3 km diameter array to a 45 km diameter array; by factor $(D^2_{\text{core}} \times (4 + N_{\text{stat,outer}}) / (4D^2_{\text{core}})) \sim 1 + (1/4) \times N_{\text{stat,outer}} \sim 10\times$. Much more if uv-plane is filled.
- Modeling of high-DR slightly resolved sources improves dramatically. One is sensitive to $\text{FWHM}/\sqrt{[S/N]}$ for any source. Especially bright sources need exquisite modeling
- Confusion “noise” on short baselines can be reduced by subtracting sources observed at higher spatial resolution prior to MW-FG removal.
- An imprint of the array equal to the FoV of a core station allows the ionosphere to be modeled in 3D through 3D tomography.

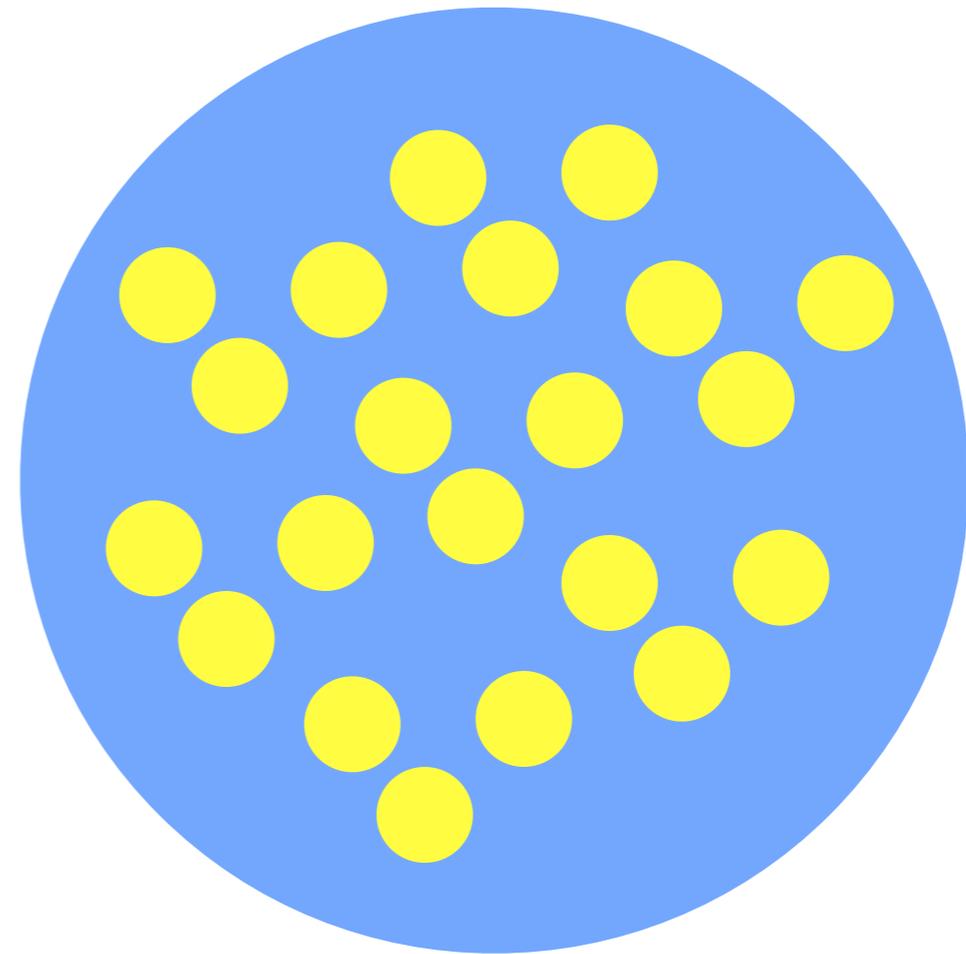
UV-plane Information Content per Channel

uv-space



Maximum # of independent pieces of information = $(D_{\text{core}}/D_{\text{stat}})^2$
[This is true even for $\gg 1$ visibility per uv-cell]

sky



Maximum # of independent pieces of information = $(D_{\text{core}}/D_{\text{stat}})^2$
= $(\lambda/D_{\text{stat}})^2/(\lambda/D_{\text{core}})^2$
[you can map the full sky, but it will be correlated!]

The sky does not contain more information than the uv-plane (i.e. its Fourier conjugate)

[i.e. the Nyquist–Shannon sampling theorem]

Current Baseline Design provides:

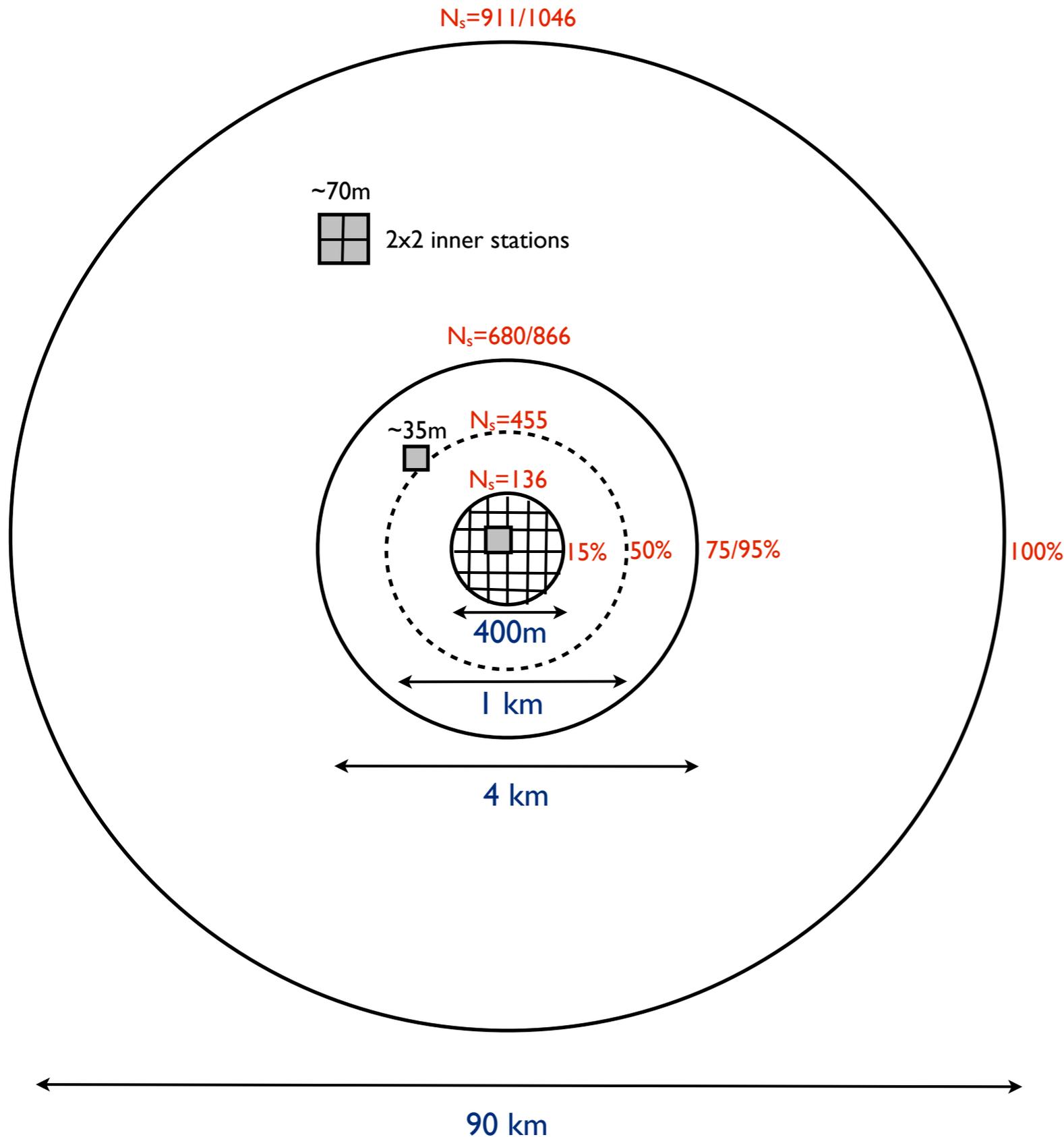
- $A/T \sim 1000 \text{ m}^2/\text{K} > 100\text{MHz}$, down to $\sim 150 \text{ m}^2/\text{K} @ 50\text{MHz}$:
i.e. $A_{\text{coll}} = 1\text{km}^2$ Consensus. Tomography needs it, although power-spectra maybe not, but SKA1 should take the next steps beyond current pathfinders in 10 years!
- $\nu_{\text{low}} = 50 \text{ MHz}$ lower frequency limit
Consensus. Many new interesting physics seems to take place starting at $z \sim 25$; risk is higher but reward of detection is very high as well.
- $D_{\text{stat}} \sim 35 \text{ meter}$ station size in the core
Seems sweet-spot for FoV and computational effort. Multi-beaming can not make up loss in FoV if $D \gg 35\text{m}$. (non-EoR) Stations outside core could be larger.
- Baselines up to $\sim 90 \text{ km}$:
Needed for calibration and compact-FG using different baselines than those for EoR science. Understand the sky/ionosphere. Information content is small on short baselines. i.e. short-baseline problems are more visible on long-baselines.

Request for (no) Change

Overall (see RfC document + science assessment workshop outcome) the CD/EoR ST is content with the current BLD, but requests some minor modifications/changes and also makes several other recommendations.

- No RfC in frequency range, resolution or optimal frequency
Required to cover the CD/EoR eras.
- No RfC in A_{eff} as function of radius, apart from maybe minor rearrangements
Required to reach 1-mK Tb levels from 5' to 1° (from $z=6$ to $z=25$)
- No RfC on long baselines of 90 km
Required for sky, instrument and ionospheric calibration.
- Recommends to put central $D=400\text{m}$ core on a regular grid (redundancy/FFT).
Enables rapid calibration, saves time/comput. costs, possibly enables FFT-type telescope
- Recommends signal fibers to central bunker for flexible beam forming and correlation
Enables flexible beam-forming as function of experiment/freq./etc.

General Geometry SKAI-AA-low



- Filled inner $R=200\text{m}$ core with elements on a regular grid
- “Stations” of 35m out to $R=2\text{km}$ (50% $< 1\text{km}$, 75%/95% $< 2\text{ km}$)
- Larger (2x2 or 3x3?) clusters of 35m stations out to $R=45\text{ km}$
- Elements and stations in core placed on regular/repeating grid for redundancy/FFT-type processing
- Maximize instantaneous uv-cover. inside the core as much as possible
- Signals of each element in the core goes to a central bunker for hierarchical beam-forming (freq., case, baseline dependent)
- Stations $< 2\text{ km}$ for CD/EoR science and $> 2\text{km}$ mostly for sky, instrument and ionospheric calibration
- Freq. coverage 50-250+ MHz.

What is detrimental to CD/EoR studies and should certainly not be done for SKA I.

- Reduce A_{eff} (or A/T) in the core significantly below the current baseline design: SKA(I) would reduce to a power-spectrum instrument and tomography during the EoR will be difficult if not impossible. CD studies will become hard.
- Reduce the frequency coverage or shift to higher frequencies:
The Cosmic Dawn starts at $z \sim 25-30$, i.e. $\sim 50\text{MHz}$; not going to those freq. will close that window for SKA(I). No other instrument can do this in the future.
- Reduce long baselines to $<90\text{ km}$: Experience with LOFAR has shown that longer baselines ($\sim 100\text{km}$) are extremely powerful for creating a sky model, for calibration, for ionospheric corrections and for diagnosing the overall system performance and data-quality.
- Do beam-forming “on-site” and build “the beam” in to the hardware system/layout of the receiver elements: Severely limits the flexibility in the system to adjust to novel/future science cases.

Thank you!